

Evaluation of the Statistical Properties of Mark-recapture Estimators of Grand Canyon Humpback Chub Abundance and Trend



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Acknowledgements

Hadley Wickham, Jenny Loda, Dave Miller (ISU)

Jeff Laake (NMFS)





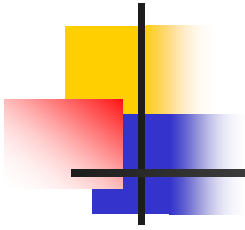
Background

- Capture-recapture (CR) data collected since 1987 under a variety of sampling designs
- Population estimation method depends on
 - Sampling design used to collect the data
 - Statistical model (= assumptions, e.g., closure, demographics)
- Bias and precision of an estimator depend on
 - Validity of the demographic and temporal dynamics assumptions that underlie each design/model
 - Quality and quantity of the data
- Computer simulation is a tool for investigation of comparative performance of different estimators under different sampling and demographic scenarios



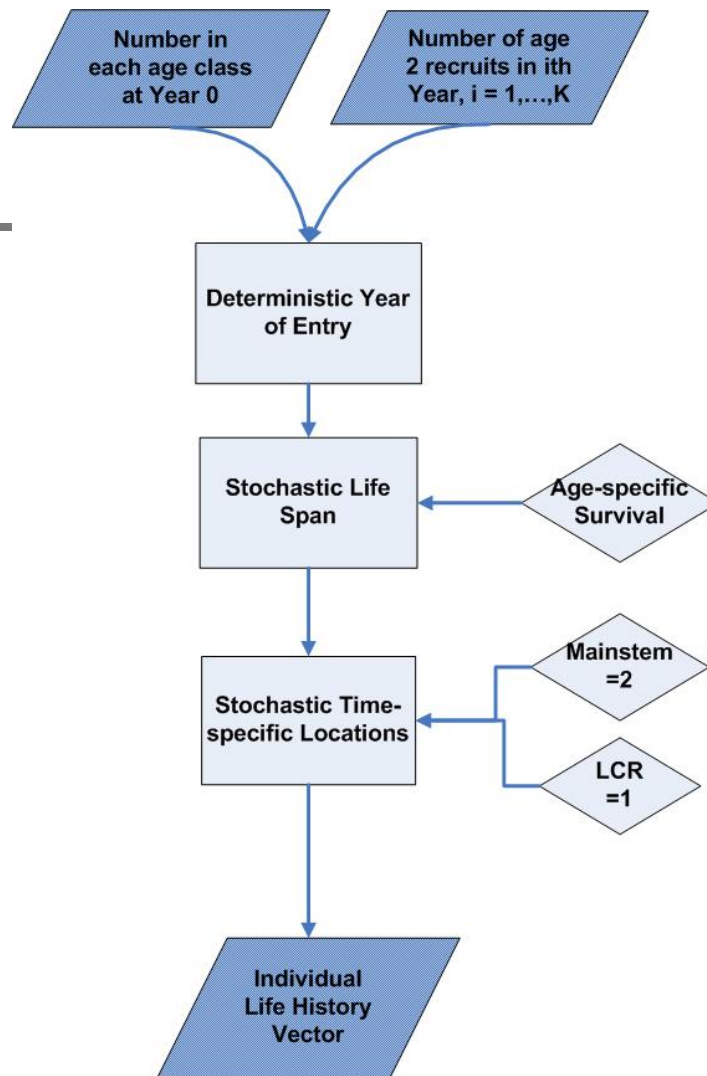
Project Objectives

- Use a Monte Carlo simulation model to evaluate the statistical performance of alternative sampling designs and estimators for age-specific population size, recruitment, and trend under different scenarios:
 - Time frame
 - Age-specific survival schedule
 - Movement dynamics
 - Capture effort → probability of capture
- Synthesize results and make recommendations



Simulation Model

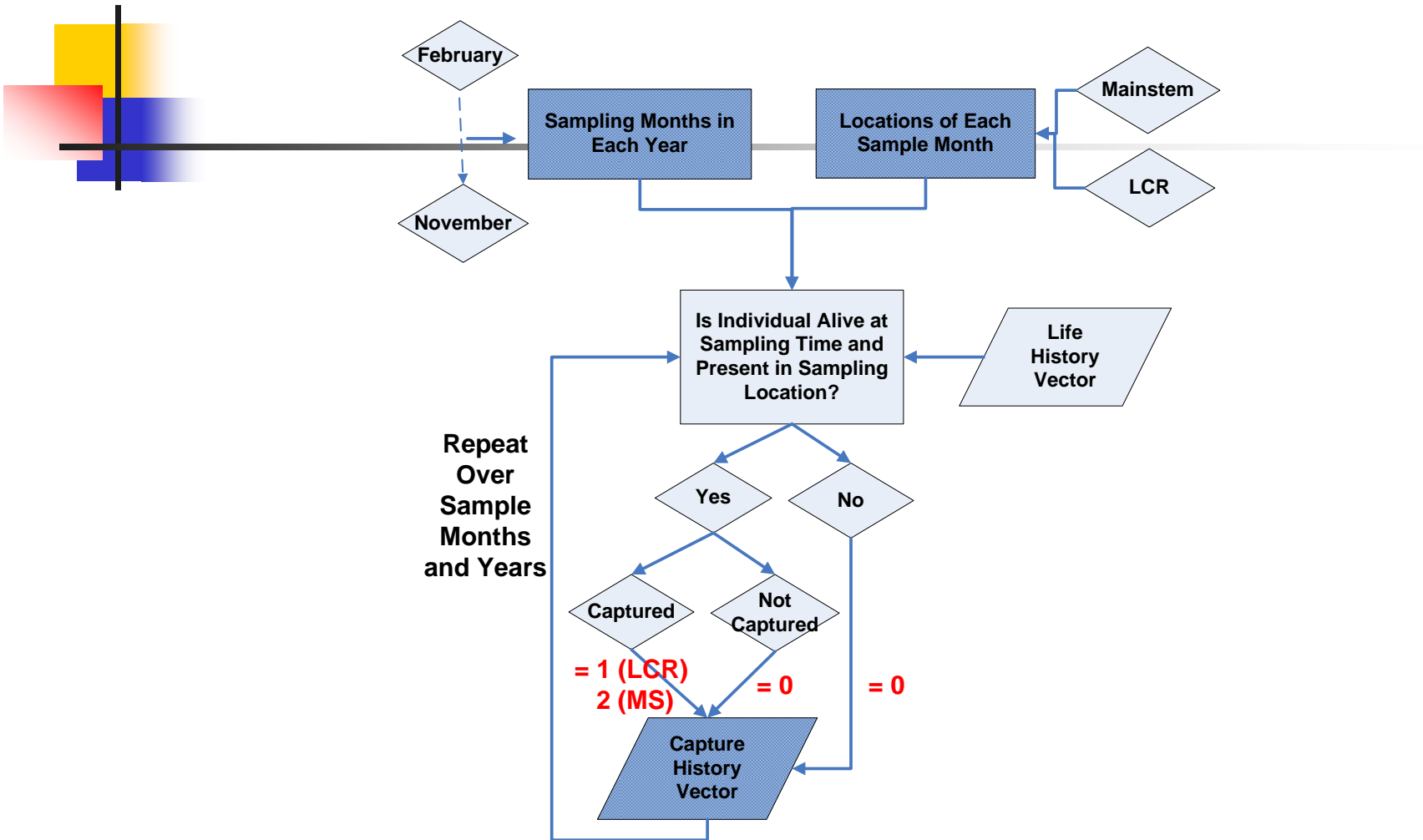
Simulate Life History Vectors for All Individual Fish



|| e.g. ,

[1 1 2 2 1 1 1 1 0 0 0 ...] (12 months x 5 years = 60 digits;
0 = dead)

Simulate Capture History Vectors for All Individual Fish



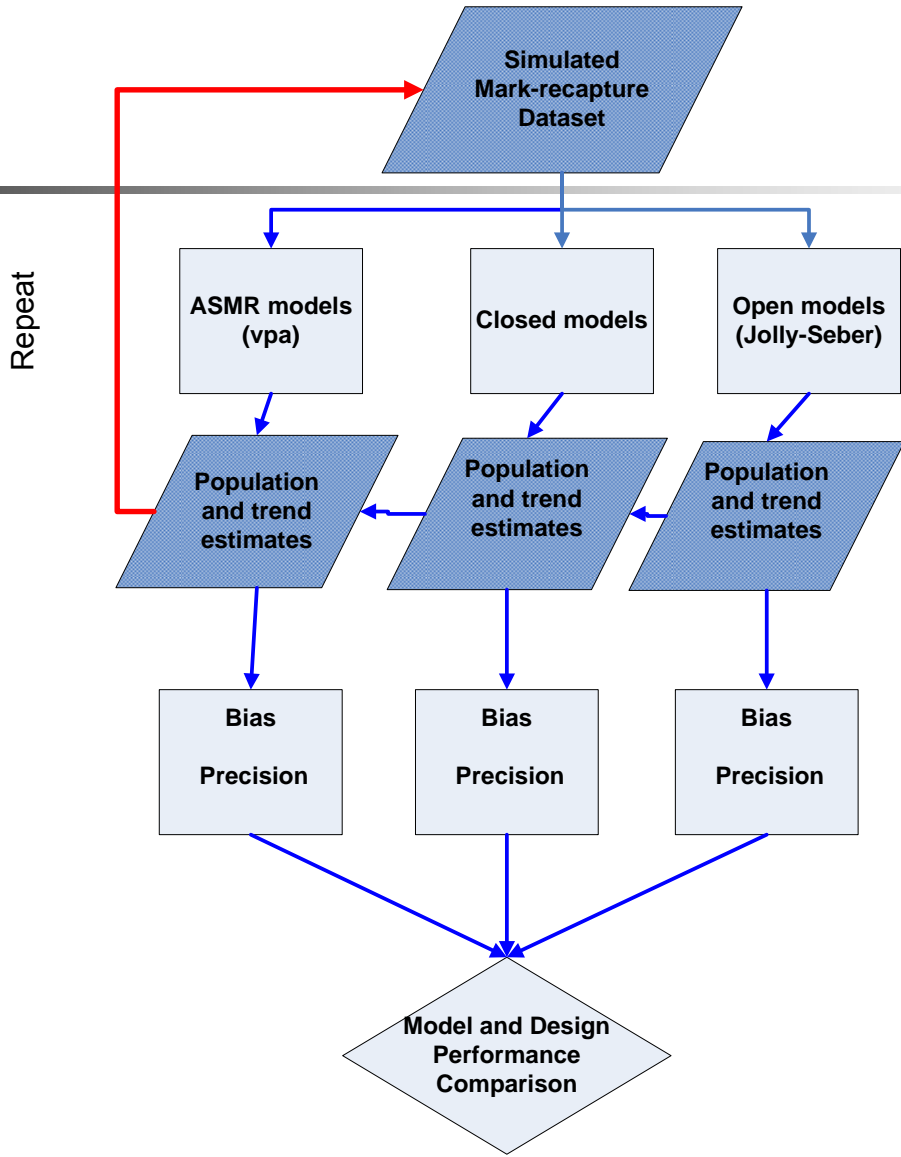
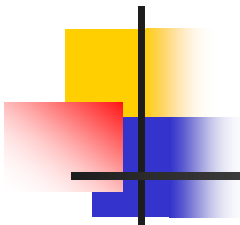
Repeat Over Sample Months and Years

= 1 (LCR)
= 2 (MS)
= 0
= 0

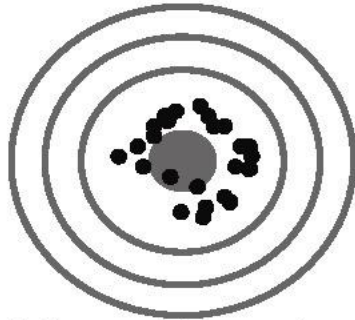
|| e.g. ,

[1 2 0 0 0 2] (Designs 1,3,5)
[1 1 0 1 2 2 0 1] (Designs 2,4)

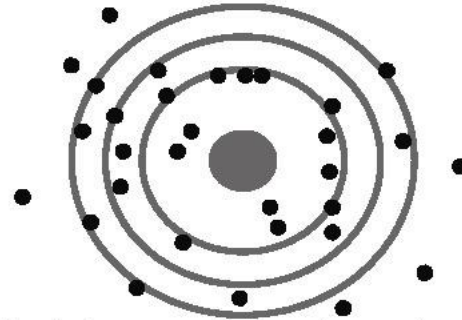
Model and Design Performance



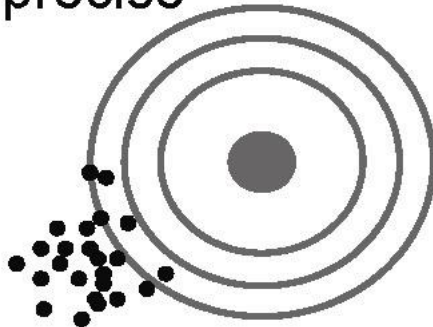
STATISTICAL PROPERTIES OF ESTIMATORS



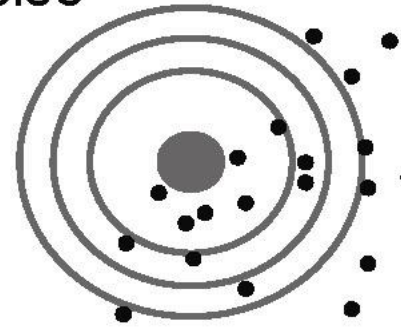
Unbiased and
precise



Unbiased but not
precise



Biased but
precise



Biased and not
precise



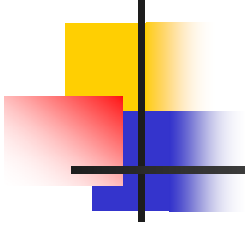
Sampling Designs and Estimation Models

- Designs

1. Spring concurrent, 3 trips
2. Spring concurrent, 4 trips
3. Fall concurrent, 3 trips
4. Fall concurrent, 4 trips
5. GCMRC: Spring and fall, LCR, 2 trips each; Summer mainstem, 2 trips

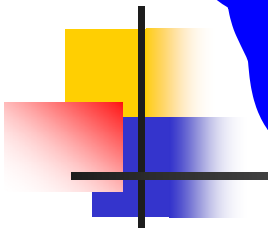
- Estimation models

- 3 ASMR
- 3 Closed
- 1 Jolly-Seber type open



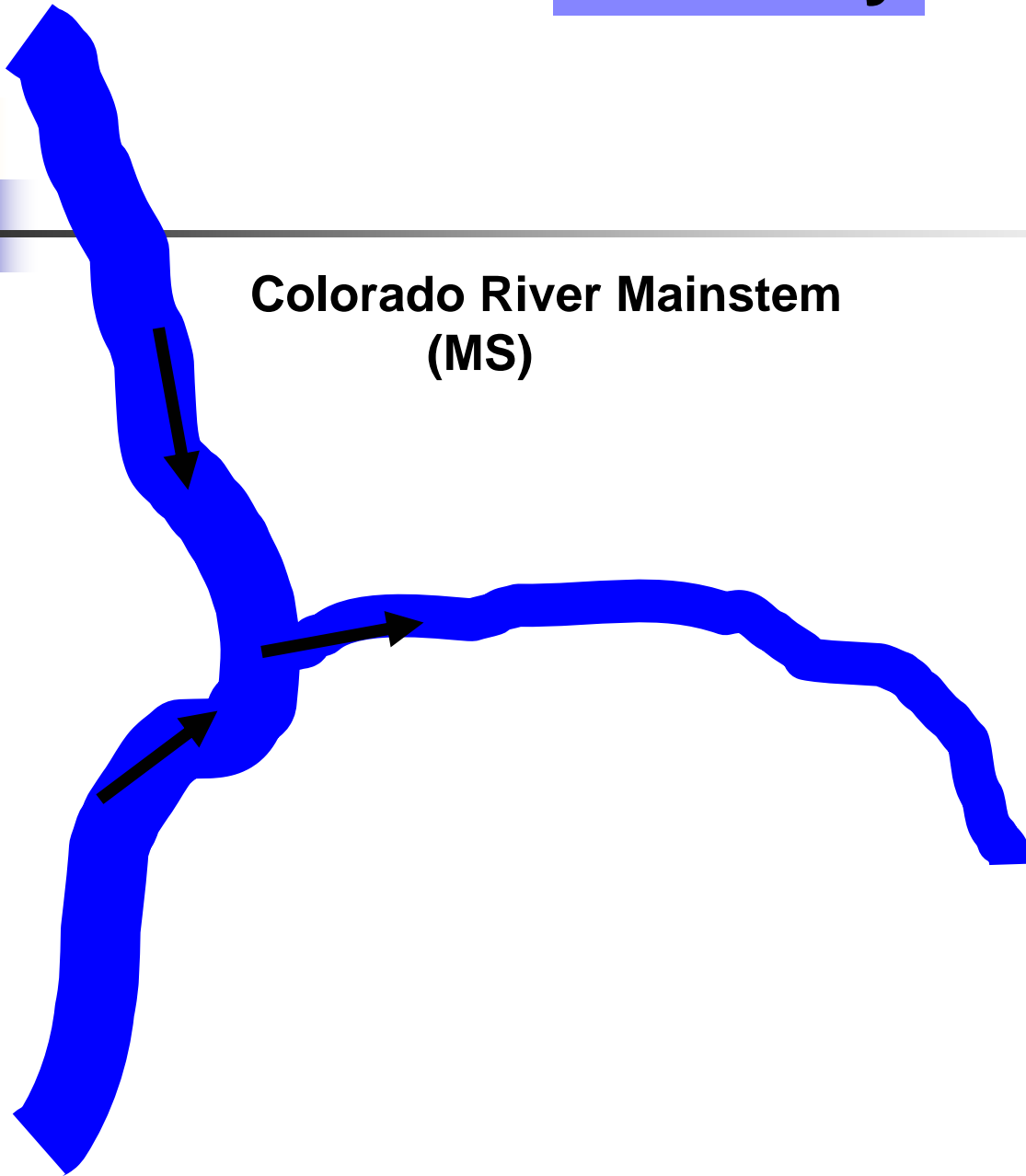
Movement Dynamics

February

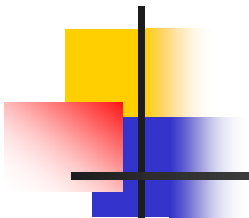


**Colorado River Mainstem
(MS)**

**Little Colorado River
(LCR)**



March

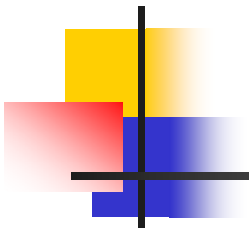


**Colorado River Mainstem
(MS)**



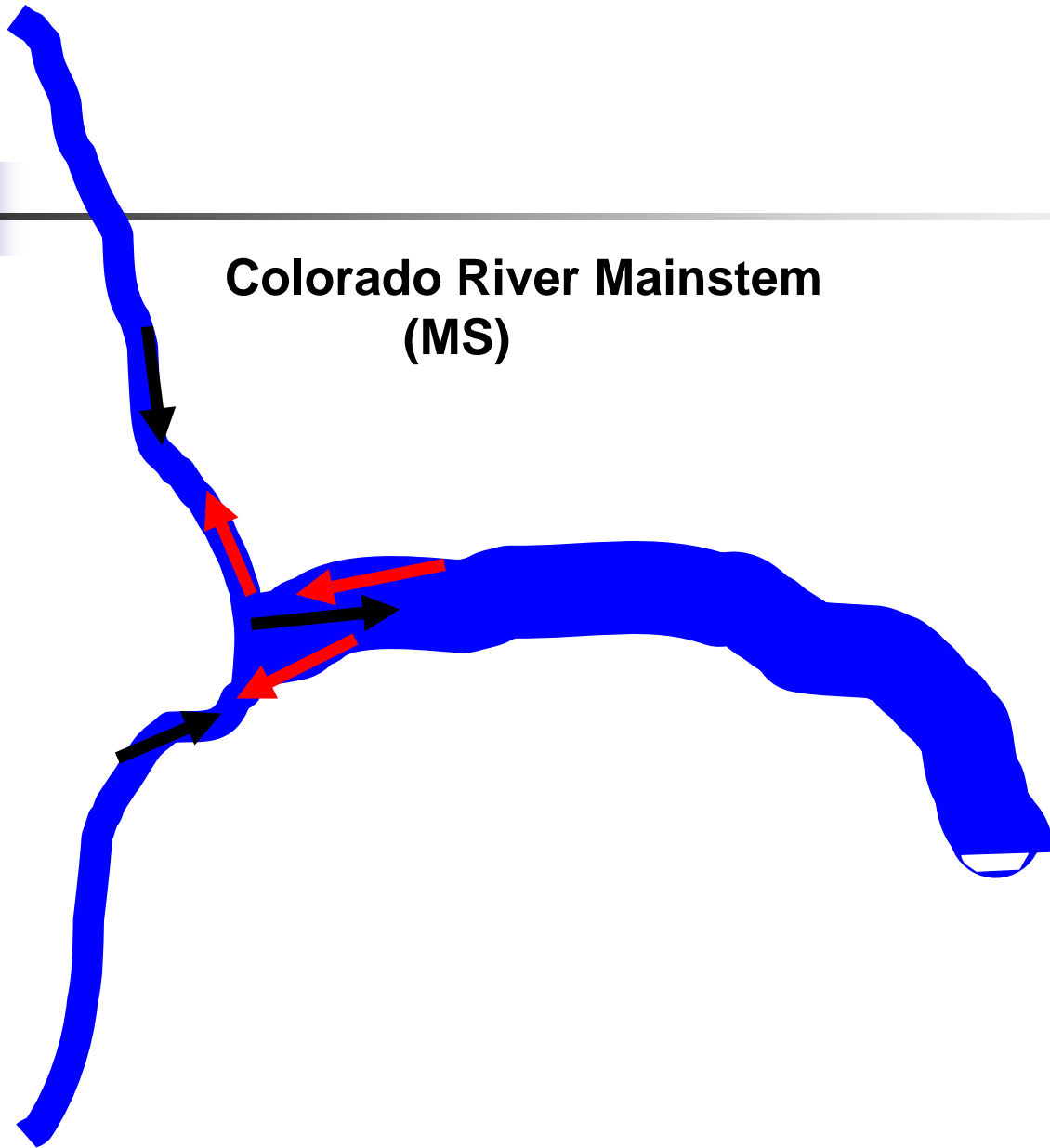
**Little Colorado River
(LCR)**

April

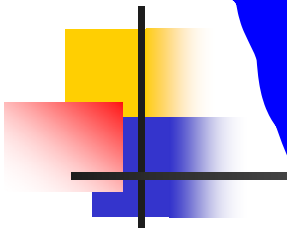


**Colorado River Mainstem
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**Little Colorado River
(LCR)**

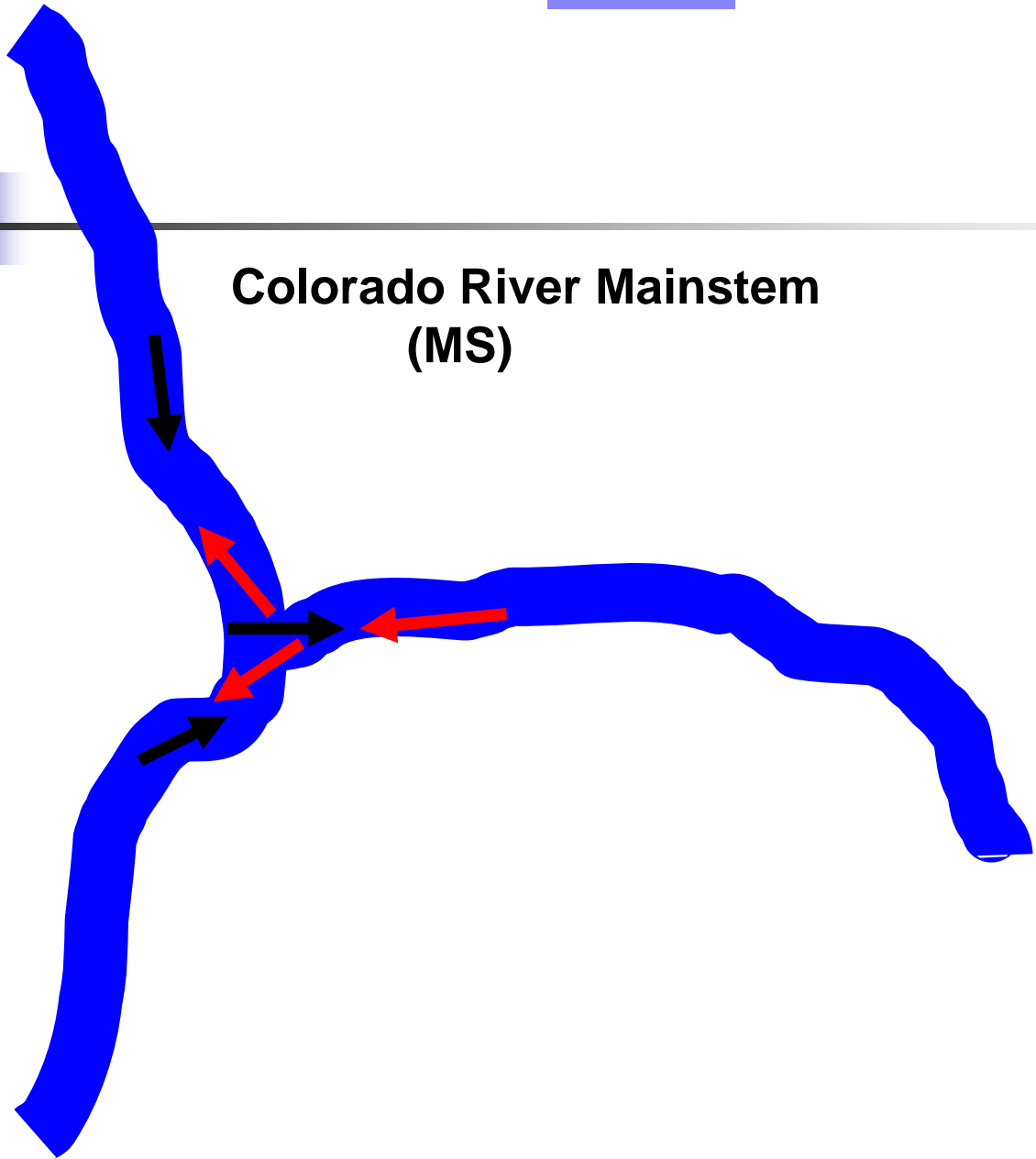


May

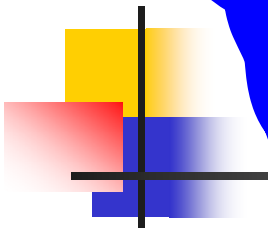


**Colorado River Mainstem
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**Little Colorado River
(LCR)**

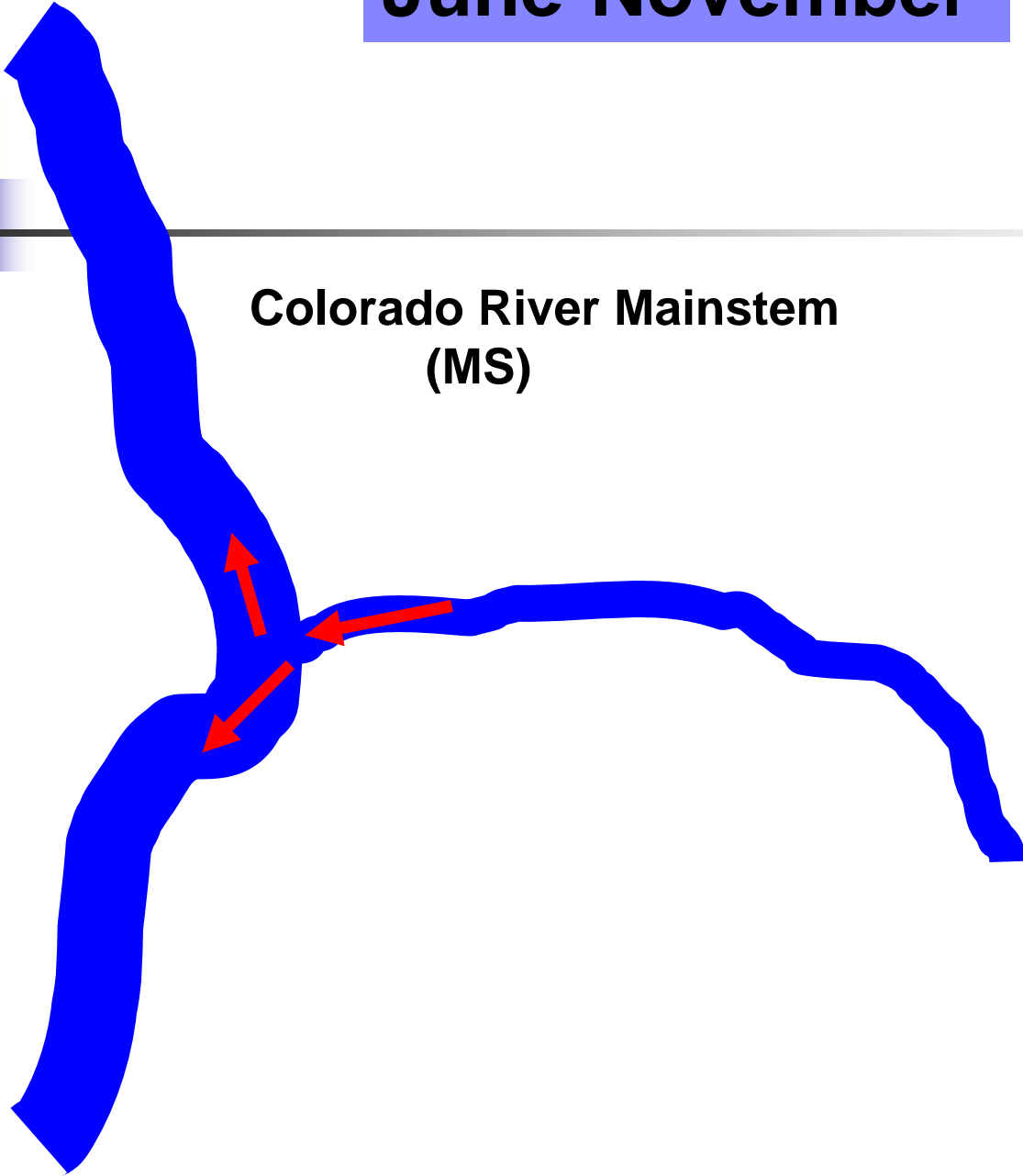


June-November

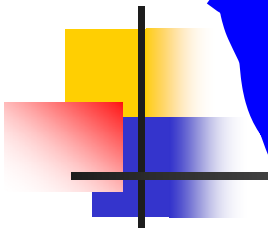


**Colorado River Mainstem
(MS)**

**Little Colorado River
(LCR)**

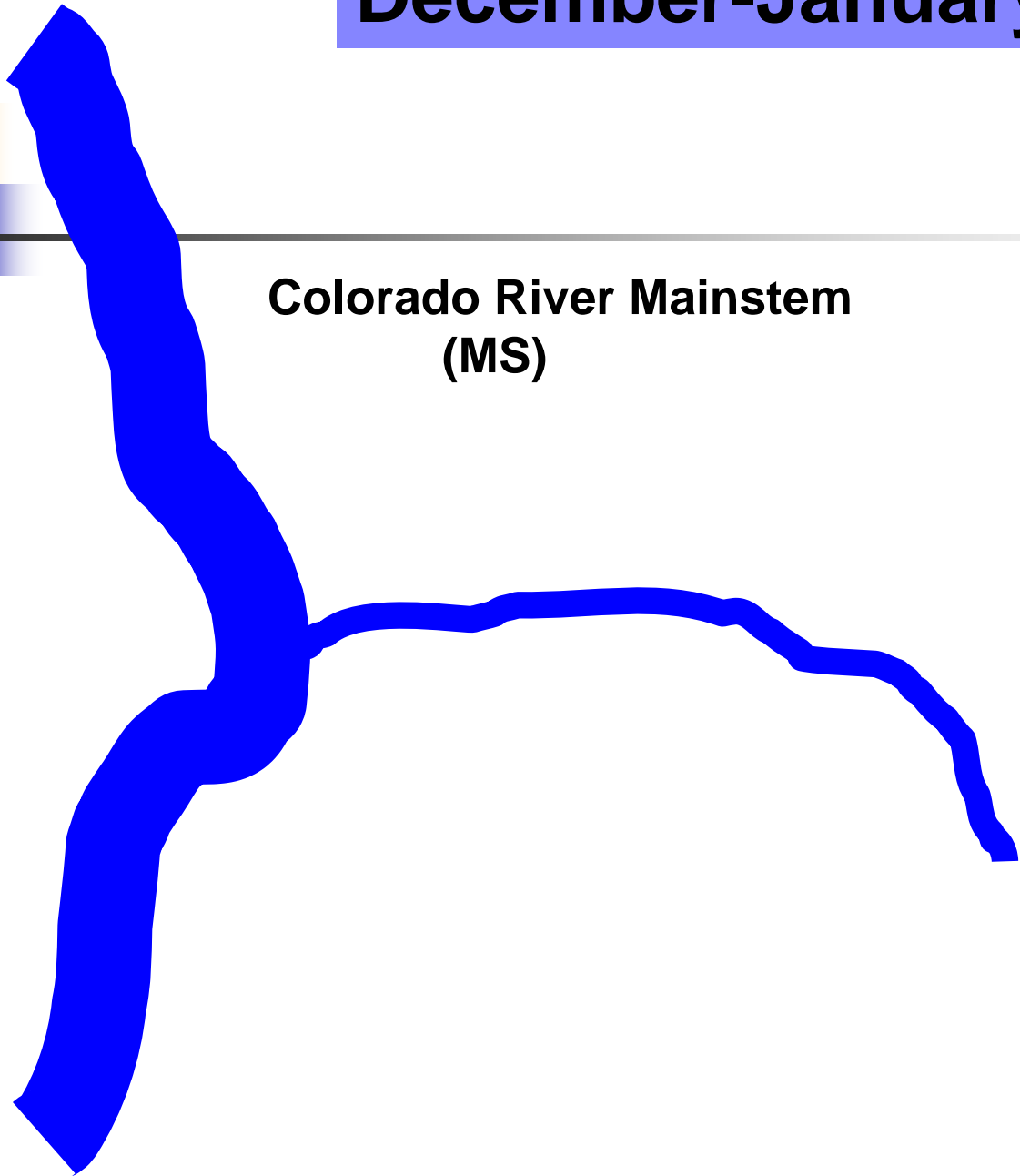


December-January

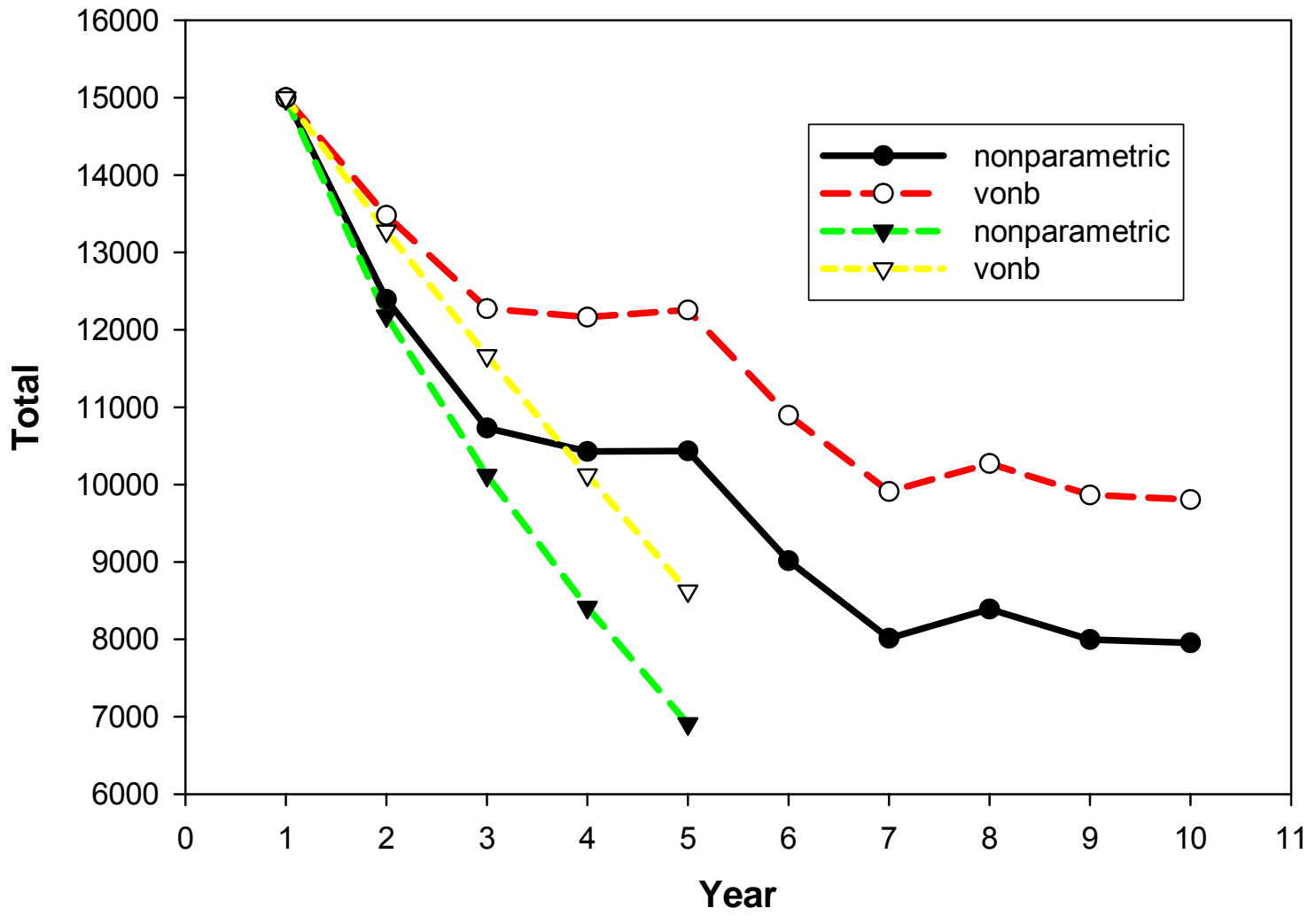
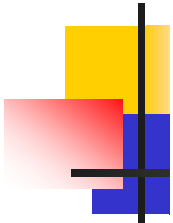


**Colorado River Mainstem
(MS)**

**Little Colorado River
(LCR)**



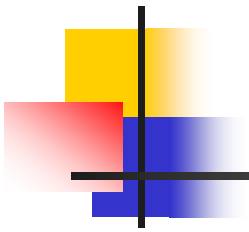
True Population Sizes





Results

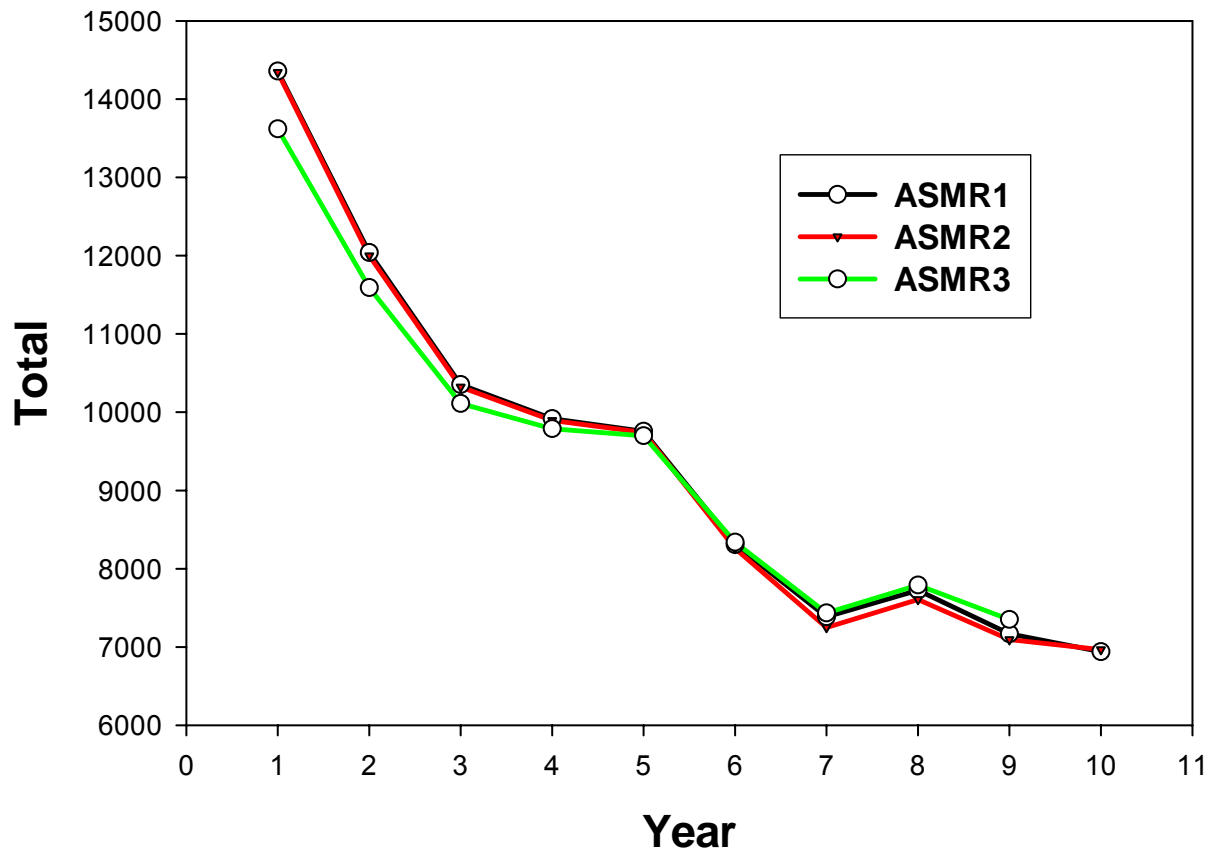
- Reduction of the set of candidate estimators
- Comparison of estimators
- Comparison of sampling designs
- Miscellaneous
 - Trend estimation
 - Effect of reduced capture probability in LCR
 - Effect of age misclassification



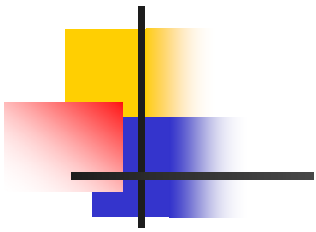
Reduction of the Set of Estimators

Comparison of ASMR Estimators

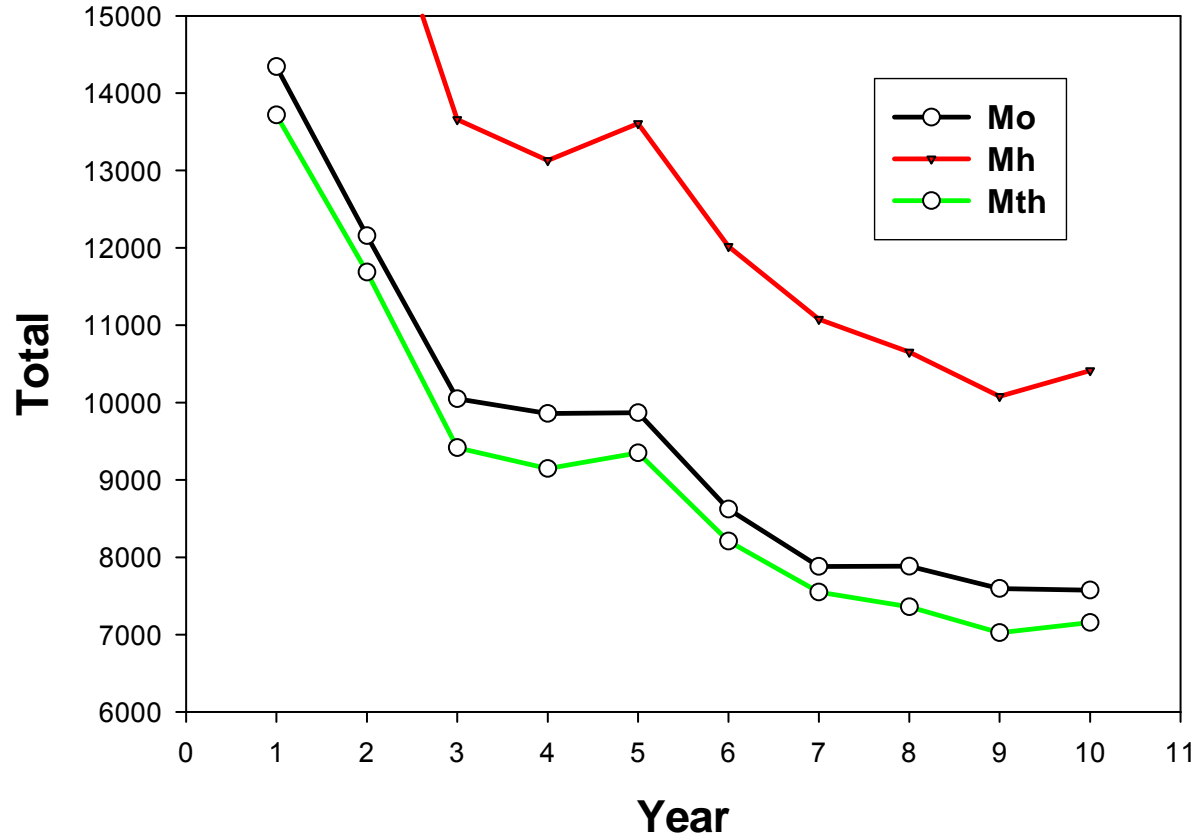
Total Estimates
Non-Parametric Survival Design 1 **Standard Capture Probabilities**
ASMR Estimators



Comparison of Closed Estimators



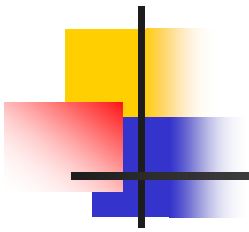
Total Estimates
Non-Parametric Survival Design 1 **Standard Capture Probabilities Closed Estimators**





Reduction of the Set of Estimators Conclusions

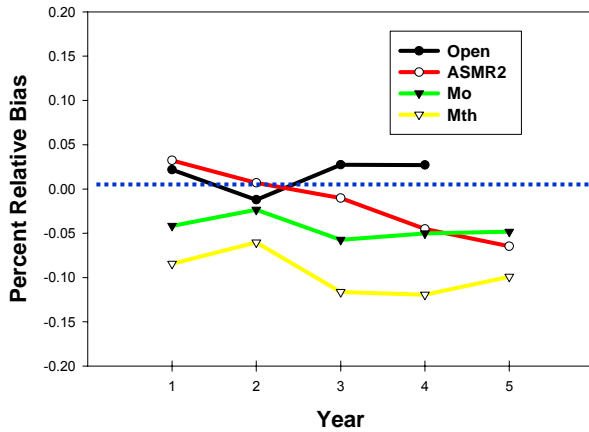
- 3 ASMR estimators not much different, but ASMR2 generally slightly better, so present only ASMR2
- M_h generally much worse than M_o and M_{th} , so eliminate
- Proceed with ASMR2, Open, M_o and M_{th}



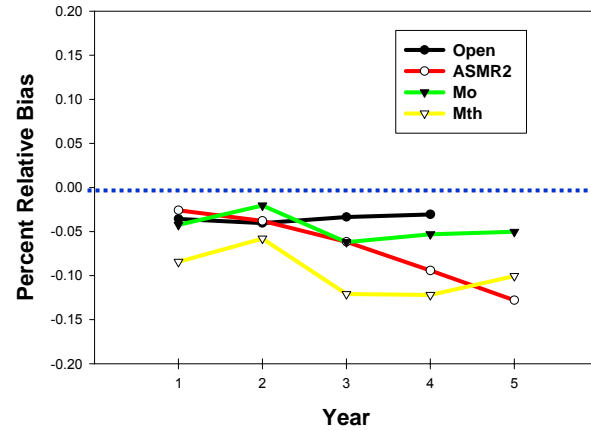
Comparison of Estimators

Percent Relative Bias

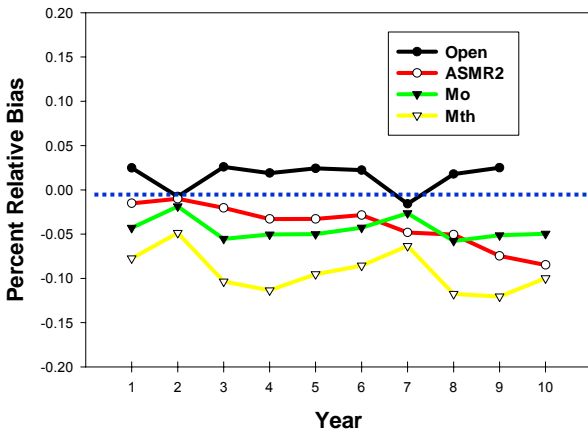
Spring Concurrent Sampling (Feb-Apr) Recruitment Estimates
Nonparametric Survival Standard Capture Probability



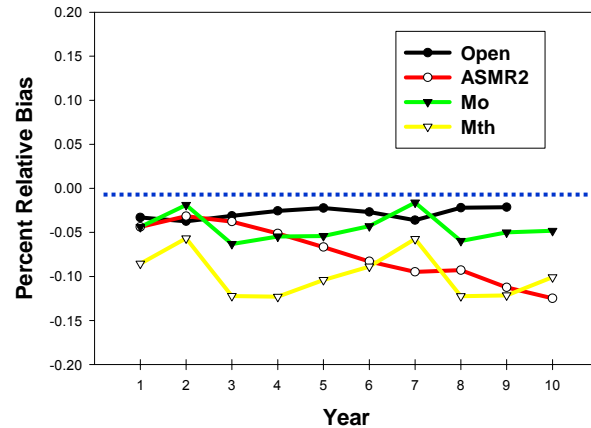
Spring Concurrent Sampling (Feb-Apr) Total Estimates
Nonparametric Survival Standard Capture Probability



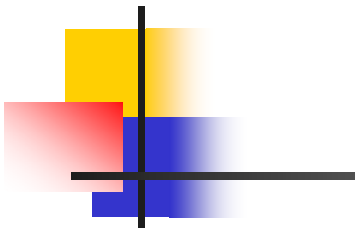
Spring Concurrent Sampling (Feb-Apr) Recruitment Estimates
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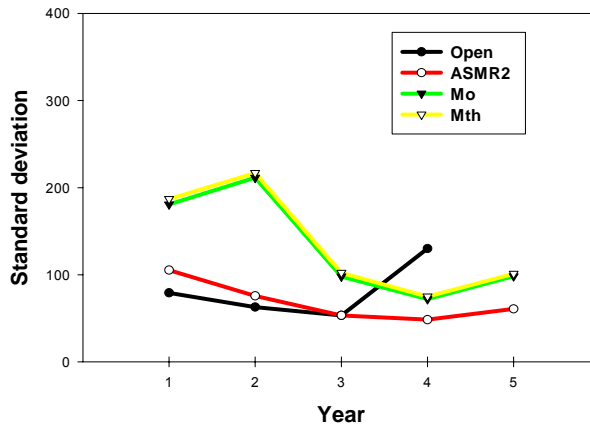
Spring Concurrent Sampling (Feb-Apr) Total Estimates
Nonparametric Survival Standard Capture Probability



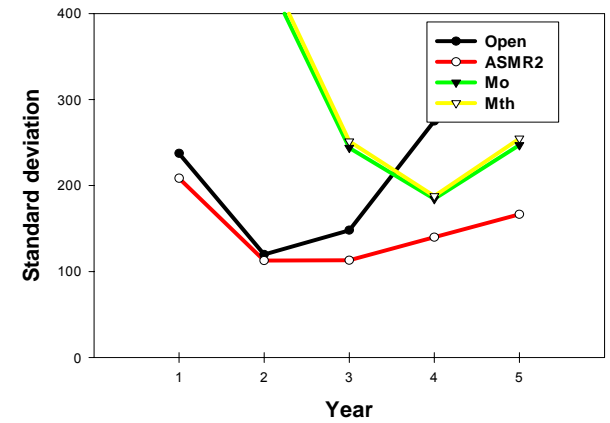
Precision



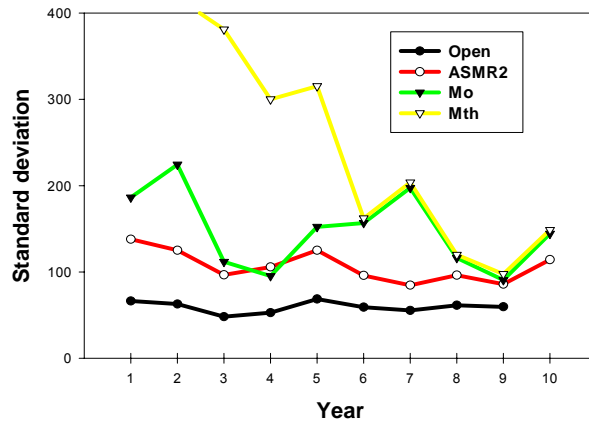
Spring Concurrent Sampling (Feb-Apr) Recruitment Estimates
Nonparametric Survival Standard Capture Probability



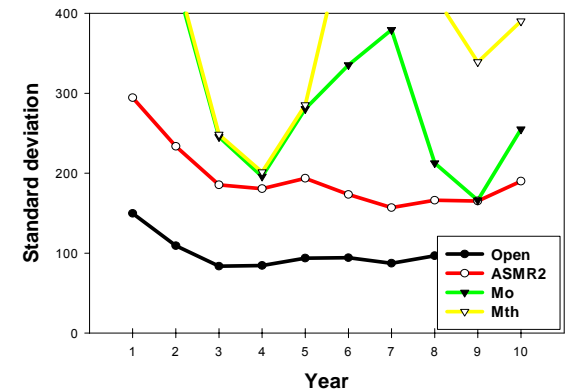
Spring Concurrent Sampling (Feb-Apr) Total Estimates
Nonparametric Survival Standard Capture Probability



Spring Concurrent Sampling (Feb-Apr) Recruitment Estimates
Nonparametric Survival Standard Capture Probability



Spring Concurrent Sampling (Feb-Apr) Total Estimates
Nonparametric Survival Standard Capture Probability

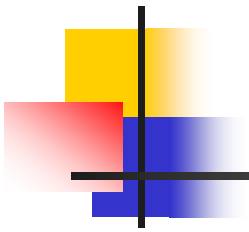




Comparison of Estimators

Conclusions

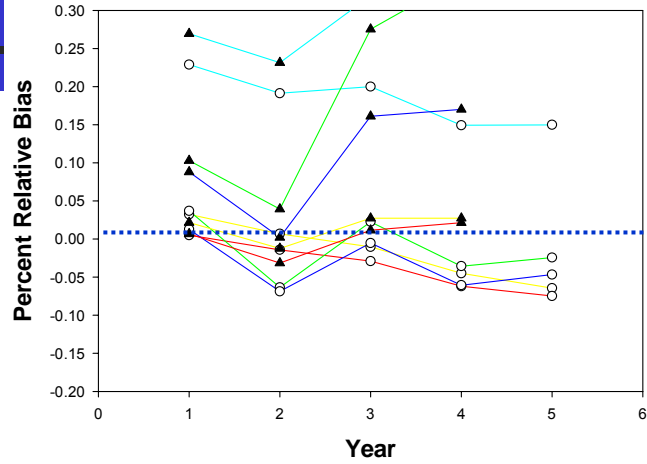
- 2 closed models are poor
- Both ASMR and Open have $PRB < 10\%$, but Open is less biased in Design 1
- ASMR more precise for $Y = 5$, and Open more precise for $Y = 10$ in Design 1
- ASMR less biased in Design 3, especially for recruits, and performs better with von B survival schedule



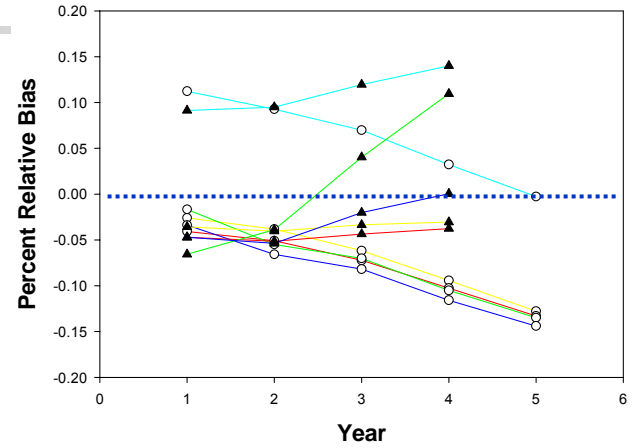
Comparison of Designs

Percent Relative Bias

Percent Relative Bias (Estimates of Recruitment)
Non-Parametric Survival
Standard Capture Probabilities

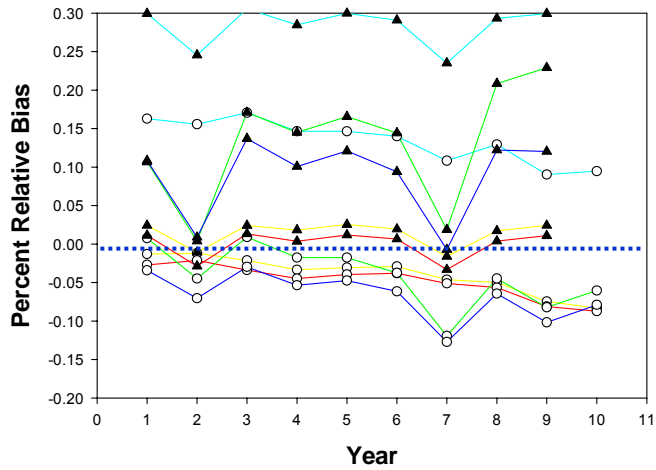


Percent Relative Bias (Estimates of Total)
Non-Parametric Survival
Standard Capture Probabilities

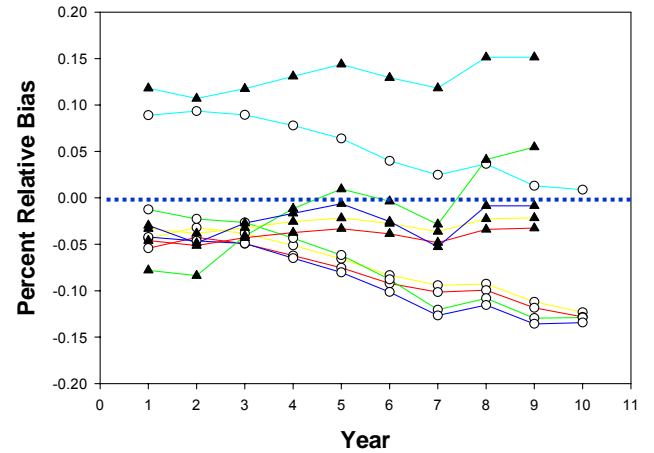


- ASMR2-1
- ASMR2-2
- ASMR2-3
- ASMR2-4
- ASMR2-5
- ▲ OPEN-1
- ▲ OPEN-2
- ▲ OPEN-3
- ▲ OPEN-4
- ▲ OPEN-5

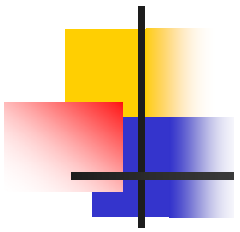
Percent Relative Bias (Estimates of Recruitment)
Non-Parametric Survival
Standard Capture Probabilities



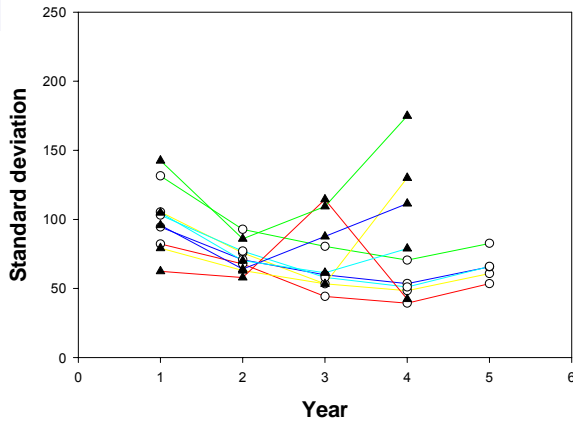
Percent Relative Bias (Estimates of Total)
Non-Parametric Survival
Standard Capture Probabilities



Precision

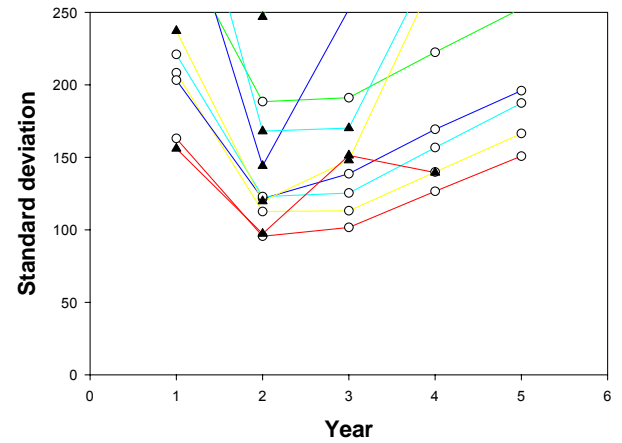


Standard deviation (Estimates of Recruitment)
Non-Parametric Survival
Standard Capture Probabilities

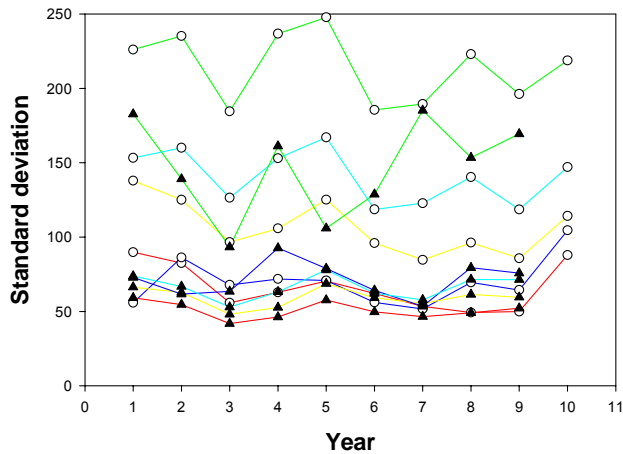


- ASMR2-1
- ASMR2-2
- ASMR2-3
- ASMR2-4
- ASMR2-5
- ▲— OPEN-1
- ▲— OPEN-2
- ▲— OPEN-3
- ▲— OPEN-4
- ▲— OPEN-5

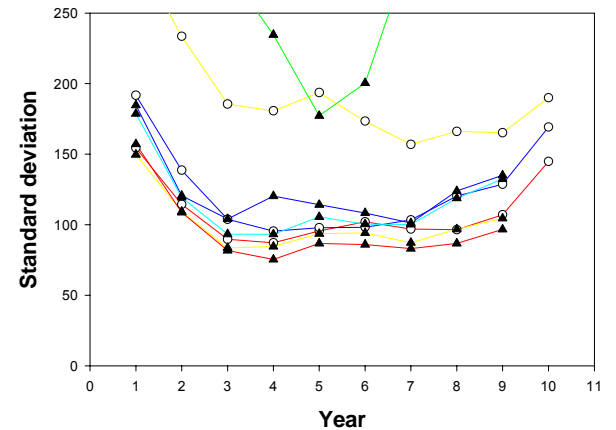
Standard deviation (Estimates of Total)
Non-Parametric Survival
Standard Capture Probabilities



Standard deviation (Estimates of Recruitment)
Non-Parametric Survival
Standard Capture Probabilities



Standard deviation (Estimates of Total)
Non-Parametric Survival
Standard Capture Probabilities

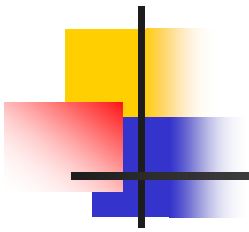




Comparison of Designs

Conclusions

- Four trips produce marginal increase in precision relative to 3 trips, but no change in bias
- Bias generally less than 10% for all Designs except Design 5, which produces larger bias
- Precision is very good for all Designs except Design 3
- No difference in relative performance of Designs with respect to survival assumptions



Miscellaneous



Estimation of Trend

- Estimates of log-linear trend in both recruitment and total population size have minimal bias and high precision ($\pm 1-2\%$) for both ASMR and Open models

Effect of Decrease in Capture Probability in the LCR

(Based on a Single Simulation)

- Minimal effect on PRB
- Causes relatively large decrease in precision, especially for Open model, but precision still generally good



Effect of Age Misclassification (Based on Nonparametric Survival and $Y = 5$)

- Misclassified age at first capture

Scenario 1

$$P[\text{correct}] = .6$$

$$P[\pm 1 \text{ ageclass}] = .3$$

$$P\{\pm 2 \text{ ageclass}\} = .1$$

Scenario 2

$$P[\text{correct}] = .5$$

$$P[+ 1 \text{ ageclass}] = .25$$

$$P\{+ 2 \text{ ageclass}\} = .25$$

- No important effect on bias or precision



Summary Statistical Conclusions

- Spring concurrent sampling with 3 trips is the best design
- Both ASMR and an Open Jolly-Seber type estimator produce good results, except for significant bias with GCMRC sampling design
- Good performance of estimators due to large capture probabilities
- No large, consistent superiority in performance of ASMR versus Open model
- Open model has other advantages
 - Fewer restrictive assumptions about capture probabilities and survival structure and hence probably more robust to violation of assumptions
 - Can utilize formal model selection theory
 - Straightforward variance estimation