# HYDRAULIC MODEL STUDIES 

# OF CRYSTAL DAM SPILLWAY 

 AND OUTLET WORKSCOLORADO RIVER STORAGE PROJECT

Engineering and Research Center Bureau of Reclamation

| 1. REPORT NO. |
| :--- | :--- | :--- | :--- |
| REC-ERC-73-22 |

17. KEY WORDS AND DOCUMENT ANALYSIS
a. DESCRIPTORS--/ hydraulic models/ vortices/ hydraulics/ cavitation/ piers/ *outlet works/plunge basins/ riprap/ flip buckets/ *spillways/ bellmouths/ discharge coefficients/ head losses/ *model studies/ submerged flow/ submerged orifices
b. IOENTIFIERS-- / *jet-flow gatesi Crystal Dam, CO
c. COSATI Field/Group 13 M
18. DISTRIGUTION STATEMENT

Available from the National Technical Information Service, Operations Division, Springfield, Virginia 22151.

| 19. SECURITY CLASS. (THIS REPORT) UNCLASSIFIED | 21. NO. DF PAGES $24$ |
| :---: | :---: |
| 20. SECURITY CLASS (This PAGE) UNCLASSIFIED | 22. PRICE |

REC-ERC-73-22

## HYDRAULIC MODEL STUDIES

OF CRYSTAL DAM SPILLWAY
AND OUTLET YORKS
COLORADO RIVER STORAGE PROJECT
by
P.H. Burgi
S. Fujimoto

December 1973

Hydraulics Branch
Division of General Research
Engineering and Research Center
Denver, Colorado

## ACKNOWLEDGMENT

The s.jdies were supervised by D. L. King, Head, Applied Hydraulics Section, and reviewed by W. E. Wag̣ner, Chief, Hydraulics Branch. The authors acknowledge the cooperation of the Hydraulic Structures Branch, Division of Design, in developing recommendations presented herein. The contribution of the Division of General Research shops in their accurate and rapid construction of the models is also acknowledged. Photography was by W. M. Batts, General Services Branch.

## CONTENTS

Page
Purpose ..... 1
Results ..... 1
Application ..... 1
Introduction ..... 1
Model Investigations ..... 1
The Spillway and Plunge Pool Model ..... 1
Spillway Studies ..... 3
The spillway profile ..... 3
Reservoir approach conditions ..... 3
Pier nose design ..... 4
Flip bucket ..... 4
Plunge Pool Studies ..... 8
Initial and recommended designs ..... 8
Impact pressures ..... 12
Outlet Works ..... 12
The $1: 13.60$ model (prel'minary design) ..... 14
The $1: 19.85$ model (recommended design) ..... 14
Vortex formation ..... 14
Conduit bellmouth entrances ..... 17
Bellmouth Head Loss Coefficients for Preliminary and Recomimended Intake Towers ..... 17
Preliminary intake tower design ..... 17
Recommended intake tower design ..... 19
Cavitation of the jet-flow gate ..... 20
Effect of submergence upon energy dissipation ..... 21
Jet-flow gate discharge coefficient ..... 23
LIST OF FIGURES
Figure
1 Crystal Dam features ..... 2
2 1 to 36-scale spillway model ..... 3
3 Model construction ..... 3
4 Spillway discharge versus head on spillway crest ..... 4
5 Water manometer pressures on spillway surface ..... 5
Depth of spillway jet ..... 6
7 Initial reservoir approach ..... 7
8 Improved reservoir approach ..... 7
$9 \quad$ Progressive pier designs ..... 7
10 Spillway pier design ..... 8
11 The spillway jet ..... 9
12 Plunge pool designs ..... 10
Figure Page
13 : Improved water surface with modified plunge pool (Figure 12B) ..... 10
14 3 to 1 riprap slope (1-yard riprap) ..... 11
15 3 to 1 riprap slope with 15 -foot deflector wall(1/4-yard riprap) ..... 11
16 Model plunge pool piezometer locations ..... 12
17 Plunge pool floor impact pressures ..... 13
18 Flunge pool floor impact pressure cell trace ..... 14
19 Intake tower designs ..... 15
20 Outlet works model layout (preliminary design) ..... 16
21 Vortex in horizontal outlet conduit ..... 17
22 Bellmouth profiles and pressure distributions ..... 17
23 Extrapolated model data (intake towers) ..... 18
24
Typical cavitation cloud downstream from a submerged jet-flowgate (gate 75 percent open)21
25 Model jet-flow gate ..... 21
$26^{\text {* }}$ Plunge pool pier configurations for outlet works ..... 22
27 Jet-flow gate submergence (gates discharging .875 cis eacin) ..... 22
28 Discharge coefficient of jet-flow gate ..... 23
29 Gate loss coefficient versus gate opening ..... 23
30 Head loss versus discharge for the jet-flow gate ..... 24

## PURPOSE

This investigation verifies the hydraulic design of the Crystal Dam spillway plunge pool, and outlet works. The coefficient of discharge of the outlet works was determined for the spillway and for the subrnerged jet-flow gates.

## RESULTS

1. The recommended spillway, with a 15 -foot (4.57-meter) radius bucket extended beyond the bucket invert to a $4: 1$ tangent at the bucket lip. operates satisfactorily for all discharges. The 4 to 1 slope on the soillway bucket lip is required to adequately flip the spillway jet into the plunge pool.
2. Because of the proximity of the spillway to the upstream right abutment, flow over the right side of the spillway is somewhat rough for discharges greater than $30,000 \mathrm{cfs}\left(850\right.$ meter $^{3} / \mathrm{sec}$ ). The recommended design shows a considerable improvement over the initial design, Figures 7 and 8.
3. The eliptical pier developed during the model study provides excellent flow conditions around the pier and along the spillway training walls, Figure 10.
4. To protect the 3 to 1 riprap slope at the downstream end of the plunge pool, a 15 -foot (4.57-meter) high deflector wall with a $1: 4$ batter is needed on the floor of the plunge pool, Figure 16. The riprap slope should start 2 feet ( 0.51 -meter) below the top of the wall.
5. A spillway discharge of 42,350 cfs $(1,171$ meters ${ }^{3} / \mathrm{sec}$ ) is attained at the design head of 16 feet ( 4.88 meters), Figure 4.
6. At design discharge the spillway jet impinges on the plunge pool floor approximately 278 feet ( 84.73 meters) from the axis of the dam.
7. The prefiminary location of the bellmouth transition from the vertical intake tower to the outlet conduit resulted in a violent vortex in the bellmouth entrance, Figure 21. This vortex was eliminated by raising the floor of the intake tower closer to the bellmouth invert, Figure 19.
8. The recommended single-intake tower system operates satisfactorily.
9. A minimum submergence of 13 feet $\{3.96$ meters) at 60 percent gate opening is required to
protect the jet-flow gates from cavitation damage. This depth will also provide adequate energy dissipation for the submerged jet to prevent extreme water surface disturbance in the plunge pool.

## APPLICATION

In general, results of this investigation apply to the structure studied. However, designs were developed which may be applicable to similar structures.

## INTRODUCTION

Crystal Dam, Figure 1, is on the Gunnison River 6 miles ( 9.65 km ) downstream from Morrow Point Dam and 14 miles ( 22.53 km ) east of Montrose, Colo. Construction of Crystal Dam will complete the Curecanti Unit of the Colorado River Storage Project.

The dam and raseryewin werve in a regulating capacity for Morrow Point and Blue Mesa Dams, releasing a relatively constant discharge downstream. The 164.1-foot ( 50.02 -meter) long flip-bucket spillway will have a design capacity of 41,350 cfs $\left(1,171_{1}\right.$ meters ${ }^{3} / \mathrm{sec}$ ). Two 48 -inch ( $1,219-\mathrm{mm}$ ) jet-flow gates will control river releases through the outlet works. The powerplant will have one 28,000 -kilowatt generating unit.

## MODEL INVESTIGATIONS

## The Spillway and Plunge Pool Model

The spillway model, constructed to a scale of $1: 36$, included 400 feet ( 122 meters) of the upstream reservoir, the concrete arch dam, and 800 feet (244 meters) of the downstream river channel, Figure 2. The flip-bucket spillway was constructed of high-density ( 6 $\mathrm{lb} / \mathrm{cu}$ foot) polyurethane and milled and sanded to the desired profile, Figure 3A. Twenty piezometers were installed in the model spillway along two radial lines to measure pressures on the spillway flow surface. The canyon topography was constructed in the model from $\mathbf{2 5 - f o o t}$ ( 7.62 -meter) interval field contours. The scaled contours were cut from wood, placed in the model, and covered with metal lath. The lath was covered with approximately $3 / 4$ inch ( 19 mm ) of cement mortar, Figure 38. Three pipes representing the penstork and two intake towers for the outlet works were connected between the reservoir head box and the powerplant in the tailbox. A tailgate assembly and sand trap were used to control the downstream tailwater elevation and collect eroded pea gravel. Water was supplied to the



Figure 2. $\uparrow$ to 36 -scale spillway model. Photo P622.D.74343

A. View of polyurethane spillway in construction. Photo P622-D-74322

B. Construction of the model dam and reservoir topography in the head box. Photo P622-D-74323
model through the permanent laboratory system and was measured by one of a bank of Venturi meters installed in the laboratory.

## Spillway Studies

The spillway profile.-The spillway profile was designed to minimize adverse stresses in the thin-arch dam during construction and operation and to maximize the discharge coefficient. The spillway profile was described by the equation:

$$
x^{2}=24 y
$$

> where
> $x=$ horizontal distance from the crest, and
> $y=$ vertical distance below the crest.
which terminated in a 15 foot ( 4.57 -meter) radius, horizontal exit bucket. Figure 4 shows the headdischarge curve for the recommended spillway profile. The design head of 16 feet ( 4.88 meters) vields a spillway discharge of $41,350 \mathrm{cfs}\left(1,171 \mathrm{~meters}^{2} / \mathrm{sec}\right)$. The design discharge coefficient is 3.92 .

The spillway profile was designed for a partial vacuum crest at the design head of 16 feet ( 4.88 meters). Piezometric pressures were measured on the spillway profile along two radial lines. One line was near the center of the spillway and the other line was 27 feet ( 8.23 meters) from the left training wall. Pressure measurements along the two lines were essentially equal. Figure 5 clescribes the water manometer pressures for several discharges and th. maximum water surface profiles in the wenter and along the training walls. The minimum pressure of minus 2.6 feet 10.79 meter) was recorded at piezometer 2 for the design discharge of $41,350 \mathrm{cfs}\left\{1,171\right.$ meters $\left.^{3} / \mathrm{sec}\right\}$. Flow depths along the spillway centerline profile were measured for several discharges less than design and are presented in Figure 6.

Reservoir approach conditions.-The initial spillway location produced a very poor spillway flaw condition for discharges above $30,000 \mathrm{cfs}\left(850\right.$ meters $^{3} / \mathrm{sec}$ ), Figure 7A. Figure 7B shows the disturbance to the retervoir water surface on the right one-third of the spillway approach. The protrusion of the canyon wall in the foreground of the photograph prevented the flow from uniformly approaching the spillway, as indicated by the flow lines of confetti.

To improve the reservoir approach the protrusion was cut back along a 150 -foot ( 45.7 -meter) radius, tangent to a line passing along the right training wall. The cu: extended to a horizontal bench 10 feet ( 3.05 meters)

Fiqure 3. Model construction.


Figure 4. Spillway discharge versus head on spiliway crest. $1: 36$-scale model.
below the spillway crest elevation. Figures 8 A and 8 B illustrate the improved flow conditions on the spillway and along the reservoir approach.

Later in the studies the axis of the dam was realined and the spillway was moved 30 feet ( 9.14 meters) toward the center of the dam and away from the right abutment. This new alinement should provide good flow distribution without removing the protrustion described above.

Pier nose design.-Several pier designs were tested in an attempt to reduce the abrupt water surface drawdown around the pier. These designs are shown in Figure 9. The preliminary pier design turned the flow too abruptly and caused a very prezounced drawdown around the pier, resulting in a very rough flow condition along the training wall as the flow accelerated over the spillway, Figure iOA. The recommended elliptical pier was developed based on work by Rouve". For a river intake, Rouve found the following limits yielded optimum flow conditions near the pier.

$$
\begin{aligned}
& 0.85 \mathrm{~B} \leq \mathrm{L} \leq 0.95 \mathrm{~B} \\
& 0.65 \mathrm{~B} \leq \mathrm{B}_{2} \leq 0.72 \mathrm{~B}
\end{aligned}
$$

$B, B_{2}$, and $L$ are shown in Figure 9.
Equations for the four radii, $\mathrm{R}_{1}, \mathrm{R}_{2}, \mathrm{R}_{3}$, and $\mathrm{R}_{4}$, Figure 9 , which best approximate Rouve's ellipse are:

$$
\begin{aligned}
& R_{1}=\left[\left(L-B_{2}\right)+\frac{\sqrt{L^{2}+B_{2}{ }^{2}}-\left(L-B_{2}\right)}{2}\right]\left[\frac{\sqrt{L^{2}+B_{2}{ }^{2}}}{B_{2}}\right] \\
& R_{2}=\left[\frac{\sqrt{L^{2}+B_{2}{ }^{2}}-\left(L-B_{2}\right)}{2}\right]\left[\frac{\sqrt{L^{2}+B_{2}{ }^{2}}}{L}\right] \\
& R_{3}=\left[\left(B_{1}-L_{1}\right)+\frac{\sqrt{L_{1}{ }^{2}+B_{1}{ }^{2}}-\left(B_{1}-L_{1}\right)}{2}\right]\left[\frac{\sqrt{L_{1}{ }^{2}+B_{1}^{2}}}{L_{1}}\right] \\
& R_{4}+\left[\frac{\sqrt{L_{1}{ }^{2}+B_{1}{ }^{2}}-\left(B_{1}-L_{1}\right)}{2}\right]\left[\frac{\sqrt{L_{1}{ }^{2}+B_{1}{ }^{2}}}{B_{1}}\right]
\end{aligned}
$$

where

$$
L_{1}=\frac{B_{1}^{2}}{R_{2}}
$$

To minimize adverse stresses in the thin arch, the pier width, B, was selected as 10 feet ( 3.05 meters). Based on the previous limits, the dimensions $L$ and $B_{2}$ were selected as 9 feet ( 2.74 meters) and 6.8 feet ${ }^{2}(2.07$ meters), respectively. Figure 10B shows the improved flow along the training wall with the elliptical pier.

Flip bucket.-The preliminary spillway profile, with the horizontal exit from the bucket lip, did not flip the spillway discharge an adequate distance from the dam

[^0]

Figure 5. Water manometer pressures on spillway surface. 1:36-scale model.

OF JET ABOVE SPILLWAY PROFILE (FT.)
$40,600 \mathrm{cFS}$


Figure 6. Depth of spillway jet. 1:36-scaie model.
$L$


 Mol！panoudu！alon suo！！！puos yjeordde nonasay＇g

1EEもL－a－zZ9d 0104d u6isap jood axun！d ןe！！！u！＇s！o OGE＇Lt Gu！блецวs！p Nem！！ds＇$\forall$


sZEtL－a－ZZ9d 0104d ubisap

LZEもL－Q－ZZ9d 0104d punorbarof ratuaว aчt u！uo！isniloid ॥EM vo人ues a




A. Preliminary pier design. Note abrupt draw down at pier and resulting rough flow surlace along training wall. Photo P622-D.74332


[^1]Figure 10. Spillway pier design.
to insure protection against rock erosion and undercutting of the right abutment and base of the dam. To
flip the spillway jet further into the paol, the radius of the bucket was extended from the bucket invert, elevation 6711.0 to elevation 6711.45 , where the bucket lip terminated at a 4 to 1 tangent. The spillway jet impinged well within the excavated plunge pool as a result of the modified bucket design and improved reservoir approach, Figures 11A and 1iB.

The spillway jet sprang iree from the bucket when the head was approximately 6.9 inches ( 175.3 mm ) or at a discharge of 250 cfs ( $7.08 \mathrm{~meters}^{3} / \mathrm{sec}$ ). The spillway jet impinged on the downstream right canyon wall at discharges below approximately 500 cfs $(14.2$ meters $^{3} / \mathrm{sec}^{\text {l }}$. Figure 11C. This impingement will occur only at low flows over the spillway.

## Piunge Pool Studies

Initial and recommended designs.-The initial plunge pool design resulted in a surface boil near the powerplant access road. The model study indicated that a considerable amount of expected excavation on the right side of the downstream canyon could be eliminated but that more excavation was needed on the left side to avoid the high boil on the water surface. Figure 12 illustrates the initial and modified plunge pool designs looking down from the dam. Figure 13 shows the improved flow conditions in the downstream plunge pool and along the powerplant access road. The initial performance is shown in Figure 8A.

To test the action of the submerged jet on large riprap. the 3 to 1 slope at the downstream end of the plunge pool was made up of rock representing 1 -yard (0.76-meter ${ }^{3}$ ) riprap, Figure 14A. Riprap along the left bank near the retaining wall was not simulated in the model because it would have required a major, expensive, model modification.

The model was tested for 1 hour at a spillway discharge of $41,000 \mathrm{cfs}\left(1,161\right.$ meters $\left.^{3} / \mathrm{sec}\right)$. A considerable amount of the large riprap was carried up the slope and deposited along the left bank. Figures 14 B and 14 C show the plunge pool water surface and eroded riprap.

To deflect the submerged jet up, away from the riprap, a 15 -foot ( 4.57 -meter) high deflector wall with a $1: 4$ batter was placed on the floor of the plunge pool, as shown in Figure 15A. Rock representing $1 / 8$-yard $\left(0.19-\right.$ meter $^{3}$ ) riprap [average diameter $=1.89$ feet ( 0.57 meter)], which would be more common in the vicinity of the dam, was placed behind the wall and on the 3 to $i$ slope. The model was tested for 1 hour at a spillway discinarge of $41,000 \mathrm{cfs}\left(1,161\right.$ meters $\left.^{3} / \mathrm{sec}^{\mathrm{c}}\right)$. Figures 15 B and 15 C show the plunge pool water surface and the relatively undisturbed riprap after the

A. View of spillway jet missing the plunge pool-horizontal bucket lip. Photo P622-D-74324

B. View of spillway jet hitting the plunge pool-4 to 7 tangent at bucket lip. Photo P622-D-74330

Spillway discharging 20.000 cfs

C. View of full spillway jet springing free. Photo P622-D-74351

Figure 11. The spillway jet

A. View from the dam looking toward the dawnstream end of the plunge pool. Initial design. Note excavation of right canyon wall. Photo P622-D-74333

B. View from the dam looking toward the downstream end of the plunge pool. Modified design. Note the decreased excavation on the right side and modified left bank alinement. Photo P622-D. 74335

Figure 12. Plunge pool designs.


Spillway discharging 41,350 cfs. Photo P622-D. 74334
Figure 13. Improved water surface with modified plunge pool (Figure 12B).

A. View of 3 to 1 slope before the test. The rock represents 1 -yard riprap. Photo P622-D-24336

B. Spillway discharging 41,000 efs. Photo P622-D-74337

C. View of the 3 to 1 slope after the test. Note how some riprap has been moved to the top of the slope. Photo P622-D-74338

Figure 14. 3 to 1 riprap slope (1-yard riprap).

A. View of 3 to 1 slope and 15 -foot deflector wall before the test. The rock rapresents $1 / 4$-yard riprap. Photo P622-D-74339

B. Spillway discharging $41,000 \mathrm{cfs}$. Fhoto P622-D-74340

C. View of 3 to 1 slope after the test showing very little movement of the riprap material. Photo P622-D. 74342

Figure 15. 3 to 1 riprap slope with 15-foot deflector wall (1/4-yard riprap).

1-hour test. The high boil near the powerplant access road in Figure B is due to the steep concrete slope in the model represented by the dark concrete in Figure 15A.

The recommended design for the side slope behind the deflector wall ranges from 3 to 1 to 2 to 1 , as shown in Figure 1. The access road will be located some 60 feet ( 18.3 meters) further from the plunge pool and 5 feet (1.5 meters) higher than the design tested, Figure 15. Although this configuration was not tested because of: insufficient space in the model, the increased size of the piunge pool should be more than adequate to contain the energy of the spiliway jet.

For small spillway discharges there is a tendency for rock to be pulled over the deflector wall into the plunge pool. Therefore, it is recommended that the riprap slope start 2 feet ( 0.6 meter) below the top of the deflector wall.

Impact pressures. - To measure the impact pressures on the floor of the plunge pool, a grid of 16 piezometers was placed in an area 48 feet ( 14.6 meters) wide by 144 feet ( 43.9 meters) long, as shown in Figure 16. Maximum pressures (water manometer) were recorded for several discharges and corresponding tailwaters. The equipressure (equielevation) lines in Figure 16 indicate plunge pool floor pressures for $Q=41,500 \mathrm{cfs}(1,174$ meter ${ }^{3} / \mathrm{sec}$ ) with the recommended spiliway bucket lip. Figure 17 illustrates the observed pressures on the plunge pool floor along the spillway centerline. Six more piezometers were later placed on the floor in a 3 -foot ( 0.9 -meter) by 6 -foot ( 1.8 -meter) area on the spillway centerline 278 feet ( 84.7 meters) from the axis of the dam, where the highest impact pressures were observed. These piezometers were equipped with pressure cells immediately below the floor of the plunge pool. Dynamic pressures were recorded for several discharges. The highest average value observed on the six pressure cells for a discharge of $41,000 \mathrm{cfs}$ ( 1,161 meters $^{3} / \mathrm{sec}$ ). represented a total pressure head of 147 feet ( 44.8 meters), or elevation 6612, Figure 18. The maximum instantaneous pressure represented an elevation of 6766, the reservoir elevation for a discharge near 41,000 cfs ( 1,161 meters $^{3} / \mathrm{sec}$ ). This would indicate that at times the instantaneous energy level on the floor of the plunge pool reaches the potential energy level of the reservoir.

## Outlet Works

The river outlet works consists of two 54 -inch ( $1,371.6 \cdot \mathrm{~mm}$ ) diameter, approximately 120 -foot (36.6-meter) long conduits which run through the dam and powerplant. These outlet condsits are controlled by


GRYSTAL DAM SPILLWAY ANO OUTLET WORKS
Figure 16. Nodel plunge pool piezometer focations. 1:36-scale model

48-inch ( $1,219.2-\mathrm{mm}$ ) diameter jet-flow gates located at the downstream end of each conduit, Figure 1.

In the preliminary design, each conduit had its own vertical intake tower located on the upstream face of the dam. The two intake towers were 160 feet ( 48.8 meters) in height with a 7.5 -foot ( 2.29 -meter) radius semicircular cross section. This design was later changed to a single 11.0 -foot ( 3.35 -meter) radius semicircular intake tower with two 54 -inch $(1,371.6-\mathrm{mm})$ diameter outlet conduits at the base, Figure 19.

The normal operating discharge of the river outlet works will be $1,600 \mathrm{cfs}\left(45.3\right.$ meters $\left.^{3} / \mathrm{sec}\right)$ with the reservoir surface elevaticn ranging from the top of inactive conservation storage, elevation 6700 to elevation 6755. Since the centerline elevation of the conduits and jet-flow gates is 6518 , the gates will operate under a minimum submergence of 11 feet ( 3.35 meters).


Figure 17. Plunge pool floor impact pressures. 1:36-scale model.

$\mathrm{O}=41,000 \mathrm{cfs}$
Tailwater elevation 6565
278 feet from axis of dam
Figure 18. Plunge pool floor impact pressure celf trace. 1:36-scale model.

The 1:13.60 model (preliminary design).-The model for_the preliminary design was built to a scale ratio of 1:13.60 so that available 3.53 -inch ( $89.7-\mathrm{mm}$ ) diameter model jet-flow gates could be used to represent the 48 -inch ( $1,219.2-\mathrm{mm}$ ) diameter prototype gates. The two 54 -inch (i,371.6-mm) diameter conduits and one of the 7.5 -foot ( 2.29 -meter) radius, semicircular, vertical intake towers were modeled with 4 -inch $(101.6-\mathrm{mm})$ pipes and a 6.62 -inch $(168.2-\mathrm{mm})$ radius model silo. One of these pipes was made of plastic and the other was made of sheet metal. The plastic model conduit included a bellmouth entrance and upstream from the model conduit the vertical, semicircular cross-sectional intake tower was built to simulate the prototype configuration. Only the lower 68 feet $\mathbf{2 0 . 7}$ meters) of the intake tower were constructed in the model and connected to the water supply pipe at an approximate elevation of 6586 . The other conduit was connected directly to the water supply pipe. Figure 20 illustrates the model test facility.

The jet-flow gates were installed in a box 12 feet ( 3.66 meters) square by 12 feet ( 3.66 meters) deep to study the submerged conditions of the gates. A false retaining wall and a false bottom were installed to simurate the spillway plunge pool into which the outlet works discharges. A valve on the tailbox outlet pipe controlled the tailwater level. Water was supplied to the model by a portable centrifugal pump through an 8 -inch ( $203.2-\mathrm{mm}$ ) diameter pipe. A calibrated $4-3 / 8$ inch ( $111.1-\mathrm{mm}$ ) diameter orifice meter was installed in the 8 -inch ( $203.2-\mathrm{mm}$ ) pipe to measure the discharge rate. Piezometers were installed at reference stations in the intake tower, upstream from the jet-flow gate, and at points within the bellmouth entrance to the conouit where low pressures were anticipated. The pressures
along the bellmouth flow surface were measured by a pot-type mercury manometer and several U-tube mercury manometers. The tailwater elevation was measured using a staff gage attached to the inside wall of the tailbox.

The 1:19.85 model (recommended design).-The 6.62 -inch ( $168.2-\mathrm{mm}$ ) model, semicircular intake tower used for the preliminary design was also utilized for the 11.0 -foot $(3.35-\mathrm{m})$ radius, single, intake tower system. Since this resulted in a change in the prototype tower radius from 7.50 feet to 11.0 feet, the model scale was changed accordingly from 13.6 to 19.85 . To model the two 54 -inch $(1,371.6-\mathrm{mm})$ conduits, 2.75 inch ( $69,85-\mathrm{mm}$ ) diameter, standard plastic pipe was used.

Piezometers were installed at reference stations $P_{i}$ and $P_{c}$ in the intake tower and at the downstream end of each conduit similar to the earlier model, Figure 20. The resulting pressures were measured by the aforementioned pot-type mercury manometer.

Calibrated $4-3 / 8$-inch ( 111.13 mm ) and $2-3 / 8$-inch $(60.66-\mathrm{mm})$ diameter orifices were used to measure the small discharges.

To regulate the flow in each conduit, the downstream end of each $2-3 / 4$-inch ( $69.85-\mathrm{mm}$ ) conduit was connected to the previously used 3.53 -inch ( $89.7 \cdot \mathrm{~mm}$ ) jet-flow gates.

Vortex formation.-The flow in the preliminary intake tower design was not stable, especially in the bellmouth transition from the intake tower to the conduit, as shown in Figure 21A. A violent vortex originated near the floor of the intake tower and developed in the bellmouth entrance to the conduit. A piezometer probe was placed in the core of the vortex by drilling a hole in the rear of the intake tower at the centerline elevation of the conduit. A pressure cell recorded model pressures of minus 23 feet ( 7.01 meters), indicating that the vortex core was at or near vapor pressure for a model discharge of 1.71 cfs ( 0.05 meter ${ }^{3} / \mathrm{sec}$ ). Pressures along the bellmouth flow surface were unsteady and pressure fluctuations as large as 200 feet ( 61 meters) prototype were recorded. The vortex formed near the entrance to the conduit and reached to the downstream end, Figure 218.

To prevent this unstable flow condition, the floor of the intake tower was raised from elevation 6510.5 to elevation 6513.5, which decreased the area available for circulation, Figure 19. This allowed enough remaining space for the bulkhead gate seals on the upstream face of the bellmouth entrance.


PRELIMINARY INTAKE CRYSTAL OAM SPILLWAY \& OUTLET WORKS

Figure 19. Intake tower designs.


Figure 20. Outlet works model fayout (prelíminary design). 1:13.6-scale model

A. Preliminary dual intake tower system. Floor of tower at elevation $6510.5,0=1160 \mathrm{efs}, 30$ feet of submergence at jet-flow gate. Note vortex extending into conduit from the intake tower. Photo P622-D-74345

E. View of vortex extending length of condult. Photo P622-D-74328

Figure 21. Vortex in horizontal outlet conduit,

With this modification there was no vortex formation, and the pressure fluctuations along the bellmouth flow surface were very small.

Conduit bellmouth entrances.-In the preliminary bellmouth design, the pressure profile showed a sudden pressure drop in the entrance, Fijure 22. Although raising the floor eliminated the vortex, the pressure distribution on the crown of the bellmouth remained approximately the same. A larger bellmouth shape was tested (recommended design) to achieve a more gradual pressure change in this region.

Figure 22 shows the two bellmouth profiles. The pressure profile in the recommended design was much improved over the preliminary design while the head losses through each were similar.

## Bellmouth Head Loss Coefficients for Preliminary and Recommended Intake Towers

Preliminary intake tower design.-The bellmouth entrance head loss, $h_{e}$, in the preliminary intake tower



CRYSTAL DAM SPILLWAY AND OUTLET WORKS
Figure 22. Bellmouth profiles and pressure distributions. 1:13.6-scale model.
design was defined as:

$$
\begin{equation*}
h_{e}=h_{L}-h_{f} \tag{1}
\end{equation*}
$$

where
$h_{L}=$ total head loss between the reference stations in the intake tower and conduit, and
$h_{f}=$ friction head loss between these stations.
For the preliminary intake tower design, Figure 20,

$$
\begin{equation*}
h_{L}=\left(P+\frac{V^{2}}{2 g}\right)_{i}-\left(P+\frac{V^{2}}{2 g}\right)_{c} \tag{2}
\end{equation*}
$$

where
$\mathrm{P}=$ piezometric head at reference stations,
$V=$ average flow velocity in intake tower or conduit, and
i, c subscripts referring to intake tower and conduit, respectively.

The extrapelated experimental results, Figure 23, indicated the following relationship between the prototype discharge, $O$, and the difference in piezometric head between the intake tower ant the condult $\quad \Delta P=P_{i}-P_{i}$

$$
\theta=112.5 \sqrt{\triangle P}
$$

or $\quad \Delta P=\left(\frac{Q}{112.5}\right)^{2}=\frac{2 g A_{C}{ }^{2}}{(112.5)^{2}} \cdot \frac{1}{2 g}\left(\frac{Q}{A}\right)_{c}^{2}$
where $A_{c}$ equals the conduit area based on the 4 -inch ( $101.6 \cdot \mathrm{~mm}$ ) diameter, model condult scaled to a 54.4 -inch $(1,382 \cdot \mathrm{~mm})$ prototype conduit diameter.

$$
\begin{aligned}
& \Delta P=\frac{64.4(16.14)^{2}}{(112.5)^{2}}\left(\frac{V^{2}}{2 g}\right)_{c} \\
& \text { therefore } \Delta P=1.33\left(\frac{V^{2}}{2 g}\right)_{c}
\end{aligned}
$$

$$
\begin{gather*}
h_{L}=1.33\left(\frac{V^{2}}{2 g}\right)_{c}+\left(\frac{V^{2}}{2 g}\right)_{i}-\left(\frac{V^{2}}{2 g}\right)_{c} \\
h_{L}=0.33\left(\frac{V^{2}}{2 g}\right)_{c}+\left(\frac{V^{2}}{2 g}\right)_{i} \tag{3}
\end{gather*}
$$

Since
but

$$
\begin{gathered}
A_{c}=0.18 A_{i} \\
Q_{i}=Q_{c}
\end{gathered}
$$

therefore $\quad V_{i}=0.18 V_{c}$
and $\quad\left(\frac{V^{2}}{2 g}\right)_{i}=0.03\left(\frac{V^{2}}{2 g}\right)_{c}$
therefore $\quad h_{L}=(0.33+0.03)\left(\frac{V^{2}}{2 g}\right)_{c}$

$$
\begin{equation*}
h_{L}=0.36\left(\frac{V^{2}}{2 g}\right)_{c} \tag{4}
\end{equation*}
$$

From equation (2) the total headloss, $h_{\mathbf{L}}$, is therefore,


GRYSTAL DAM SPILLWAY AND OUTLET WORKS
Figure 23. Extrapolatad model data (Inteke towars).

The friction head loss, $h_{f}$ in the intake tower and conduit was estimated by the Darcy-Weisbach equation as follows:

$$
h_{f}=\left(\frac{f L}{4 R} \frac{V^{2}}{2 g}\right)_{i}+\left(\frac{f L}{D} \frac{V^{2}}{2 g}\right)_{c}
$$

where
$\mathrm{f}=$ friction coefficient,
$\mathrm{R}=$ hydraulic radius,
$\mathrm{L}=$ respective length, and
$\mathrm{D}=$ diameter.

The friction head loss in the tower is negligible since the velocity head in the tower is only 3 percent of the conduit velocity head. $L$ and $D$ in the model conduit are 47 inches ( 1.19 meters) and 4 inches ( 0.10 meter). respectively. The friction coefficient, $f$, is expressed by using Manning's $n$ as follows:

$$
f=\frac{185 n^{2}}{D^{1 / 3}}
$$

Assuming a Manning's $n$ of 0.008 for the 4 inct (0.10-meter) plastic conduit,

$$
\begin{align*}
& \quad \frac{f L}{D}=\frac{185 n^{2} L}{D^{1 / 3} D}=\frac{185 n^{2} L}{D^{4 / 3}} \\
& \text { or } \quad \frac{f L}{D}=0.20 \\
& \text { therefore } \quad h_{f}=0.20\left(\frac{V^{2}}{2 g}\right)_{c} \tag{5}
\end{align*}
$$

Subst:tuting equations (4) and (5) into equation (1),

$$
\begin{align*}
& h_{e}=(0.36-0.20)\left(\frac{V^{2}}{2 g}\right)_{c} \\
& h_{e}=0.16\left(\frac{V^{2}}{2 g}\right)_{c}
\end{align*}
$$

Recommended intake tower design.-The recommended design used the same bellmouth shape as the preliminary design. Extrapolated experimental results, Figure 23, indicated the following relationship between the conduit discharge, $Q_{c}$, and the difference in piezometric head, $\Delta P=P_{i} \cdot \mathcal{P}_{\mathbf{c}}$ :

$$
\begin{equation*}
Q_{c}=106.7 \sqrt{\Delta P} \tag{7}
\end{equation*}
$$

This relationship was derived by operating either
conduit open with the other condult closed or oper. ating both conduits with equal discharges. Further test indicated that the total discharge through the intake tower equaled the sum of the two conduit discharges calculated from equation (7) when operating with unequal discharges through the conduits. Therefore, the total discharge,

$$
\begin{gather*}
Q_{i}=\left(Q_{c}\right)_{R}+\left(Q_{c}\right)^{\prime} \\
Q_{i}=106.7 \sqrt{\Delta P_{R}}+106.7 \sqrt{\Delta P_{L}} \\
Q_{i}=106.7\left(\sqrt{\Delta P_{R}}+\sqrt{\Delta P_{L}}\right) \tag{8}
\end{gather*}
$$

where
$\Delta P_{L}=$ piezometric head difference between the reference stations in the intake tower and leficonduit, and
$\Delta P_{R}=$ piezometric head difference between the reference stations in the intake tower and right conduit.

From equation (7)

$$
\Delta P=\left(\frac{Q_{c}}{106.7}\right)^{2}=\frac{2 g A_{c}^{2}}{(106.7)^{2}} \frac{1}{2 g}\left(\frac{Q}{A}\right)_{c}^{2}
$$

where $A_{c}$ equals the conduit area based on the 2.72 -inch ( $70 \cdot \mathrm{~mm}$ ) diameter model conduit scaled to a 54.0 -inch ( $1,371.6-\mathrm{mm}$ ) prototype conduit diameter

$$
\begin{equation*}
\Delta P=\frac{64.4(15.9)^{2}}{(106.7)^{2}}\left(\frac{V^{2}}{2 g}\right)_{c}=1.43\left(\frac{V^{2}}{2 g}\right)_{c} \tag{9}
\end{equation*}
$$

The total head loss, $h_{1}$, between reference stations in the intake tower and either conduit is,

$$
\begin{aligned}
h_{L} & =\left(P+\frac{V^{2}}{2 g}\right)_{i}-\left(P+\frac{V^{2}}{2 g}\right)_{c} \\
h_{L} & =\Delta P+\left(\frac{V^{2}}{2 g}\right)_{i}-\left(\frac{V^{2}}{2 g}\right)_{c} \\
\text { or } & h_{L}=0.43\left(\frac{V^{2}}{2 g}\right)+\left(\frac{V^{2}}{2 g}\right)
\end{aligned}
$$

Equation (10) is similar to equation (4). The relationship between the terms $\left(\frac{V^{2}}{2 g}\right)_{i}$ and $\left(\frac{v^{2}}{2 g}\right)_{c}$ is a function of the ratio $\frac{Q_{i}}{\alpha_{c}}$. However, in this instance the ratolo $\frac{Q_{j}}{\alpha_{c}}$
is variable (for example, $Q_{L}=0.1 Q_{i}$ and $Q_{R}=0.9 Q_{i}$ ).
The friction head loss, $h_{f}$, in the intake tower and either conduit is,

$$
h_{f}=\left(\frac{f L}{4 R} \frac{V^{2}}{2 g}\right)_{i}+\left(\frac{f L}{D} \frac{V^{2}}{2 g}\right)_{c}
$$

Under the same assumption of negligible tower loss and in this case substituting $L_{c}=37$ inches ( 940 mm ) and $D_{c}=2.72$ inches ( 70 mm ) and using Manning's $n=$ 0.008,

$$
\begin{gathered}
\frac{\mathrm{fL}}{\mathrm{D}}=\frac{185 n^{2} L}{\mathrm{D}^{1 / 3} \mathrm{D}}=\frac{185 n^{2} L}{D^{4 / 3}} \\
\frac{\mathrm{fL}}{\mathrm{D}}=0.26
\end{gathered}
$$

Therefore, the entrance head loss is determined to be,

$$
\begin{align*}
& h_{e}=h_{L}-h_{f}=0.43\left(\frac{V^{2}}{2 g}\right)_{c}+\left(\frac{V^{2}}{2 g}\right)_{i}-0.26\left(\frac{V^{2}}{2 g}\right)_{c} \\
& \text { or } \quad h_{e}=0.17\left(\frac{v^{2}}{2 g}\right)_{c}+\left(\frac{v^{2}}{2 g}\right)_{i}  \tag{11}\\
& \text { but } \quad\left(\frac{V^{2}}{2 g}\right)_{i}=\left(\frac{Q_{i}}{Q_{c}}\right)^{2}\left(\frac{A_{c}}{A_{i}}\right)^{2}\left(\frac{v^{2}}{2 g}\right)_{c}
\end{align*}
$$

Therefore, equation (11) can be restated as,

$$
\begin{gathered}
h_{e}=0.17\left(\frac{V^{2}}{2 g}\right)_{c}+\left(\frac{Q_{i}}{Q_{c}}\right)^{2}\left(\frac{A_{c}}{A_{i}}\right)^{2}\left(\frac{V^{2}}{2 g}\right)_{c} \\
\left(\frac{A_{c}}{A_{i}}\right)^{2}=\left(\frac{15.9}{190}\right)^{2}=0.007
\end{gathered}
$$

Therefore, for either conduit bellmouth,

$$
\begin{equation*}
h_{e}=\left[0.17+0.007\left(\frac{Q_{i}}{Q_{c}}\right)^{2}\right]\left(\frac{v^{2}}{2 g}\right)_{c} \tag{12}
\end{equation*}
$$

Equation (12) indicates a bellmouth entrance loss slightly greater than that of the preliminary design, equation (6). If one conduit is open and the other closed, then $Q_{c}=Q_{i}$ and

$$
h_{e}=0.177\left(\frac{V^{2}}{2 g}\right)_{c}
$$

If both conduits have equal discharges, then

$$
\begin{gathered}
Q_{c}=1 / 2 Q_{i} \\
\text { and } h_{e}=(0.17+0.028)\left(\frac{v^{2}}{2 g}\right)_{c}=0.198\left(\frac{v^{2}}{2 g}\right)_{c}
\end{gathered}
$$

Cavitation of the jet-flow gate.-Cavitation of the Crystal Dami jet-flow gates was anticipated as a result of the Teton Dam hydraulic model study, which indicated inadequate circulation downstream from the submerged jet-flow gate for an enfargement less than 3 diameters. The Teton Dam jet-flow gate will operate with back pressures greater than 80 feet ( 24.4 meters). Figure 24B shows the cavitation cloud which formed with the Teton Dam submerged jet-flow gate in the range of 60 to 80 percent open under a relatively low back pressure, 15 feet ( 4.6 meters), discharging into a cownstream chamber with a diameter three times the gate orifice diameter. The cavitation cloud originates at the intersection of the horizontal gate leaf and the circular crifice.

Pressures on the submerged downstrearn face of the orifice plate and gate frame of the Crystal Dam jet-flow gate were measured using four pressure cells to determine the possibility of subatmospheric pressures. Figure 25 shows the location of the four piezometers on the model jet-flow gate.

Tests of the preiiminary outlet design, Figure 26A, with two jet-flow gates discharging into the tailbox, produced a minimum instaritaneous pressure (Piezometer 3) of 13 feet ( 3.96 meters) subatmosphere at a gate opening of 70 percent ( 800 cfs ). This minimum pressure occurred with a 19 -foot (5.8-meter) submergence and an estimated reservoir elevation of 6750 .

To improve the circulation on the downstream face of the submerged jet-flow gate, the 8.75-foot (2.67-meter) piers were cut back at a $30^{\circ}$ angle below the minimum tailwater elevation 6529, and the sill was removed, as shown in Figure 26B. In this instance, the minimum instantaneous pressure (Piezometer 4) was 7.2 feet (2.19 meters) subatmosphere at, a gate opening of 60 percent ( 650 cfs ). It occurred urijer 13 -foot (3.96-meter) submergence and an estimated reservoir elevation 6750.

It was concluded that with this configuration the jet-flow gate would be free from cavitation damage without further modification since the recorded minimum pressure was above that which would be considered a cavitation pressure. Tests run with less submergence had greater subatmospheric pressures, as would be expected. Therefore, a minimum submergence of 13 feet ( 3.96 meters) at 60 percent valve

A. No cavitation (high back pressure). Photo P622-D-74328

B. Cavitation cloud originating at the intersection of the circular orifice and the horizontal gate leaf. \$15-foot back pressure). Photo P622-D-74326

Figure 24. Typical cavitation cloud downstream from a submerged jet-flow gate (gate 75 percent open).


TOP VIEW


SIDE VIEW

## GRYSTAL DAM SPILLWAY AND OUTLET WORKS

Figure 25. Model jet-flow gate.
upening was arbitrarily set as the minimum tailwater criterion, where depth of submergence was defined as the distance from the valve centerline to the water surface.

Effect of submergence upon energy dissipation.Several tailwater depths were tested to determine the effect of submergence of the jet-flow gate upon the water surface disturbance in the spillway plunge pool for normal operation with both valves 75 percent open, each discharging 875 cfs ( 24.8 meters $^{3} / \mathrm{sec}$ ).

Tests were run with submergences of 6,10 , and 14 feet (1.83, 3.05, and 4.27 meters), Figure 27. The 6 -foot (1.83-meter) and 10 -foot ( 3.05 -meter) depths resulted
－（4כea sjo g 18


09EカL－a－てZ9d



6ヵ\＆もL－व－てZ9d



8tEもL－a－Zて9d



LDEもL－O－Zて9d




9ヵEもL－0－てZ9゚d 0104d
＇II！s pue saa！d 200 J－GL＇8 4

in a rough water surface and were inadequate. The 14 -foot (4.27-meter) depth was sufficient, and the 13-foot (3.96-meter) submergence criterion for prevention of cavitation damage is adequate to minimize water surface disturbances in the plunge pool.

Jet-flow gate discharge coefficient.-The discharge characteristics of the submerged jet-flow gate were determined for various submerged depths and gate
openings. The discharge coefficient, $C$ (both with and without the conduit velocity head) and the head loss coefficient, K, of the jet-flow gate are shown in Figures 28 and 29, respectively. The discharge coefficient and the head loss coefficient are 0.628 and 2.536 at 100 percent gate opening. The head loss through the jet-flow gate for various gate openings is shown in Figure 30.


Figure 29. Gate loss coefficient versus gate opening.


CRYSTAL DAM SPILLWAY AND OUTLET WORKS
Figure 30. Head loss versus discharge for the jet-flow gate.
7.1750 (3.71)

Burect of Reclamation

## CONVERSION FACTORS-BRITISH TO METRIC UNITS OF MEASUREMENT

The following conversion factors adopted by the Bureau of Reclamation are thoge published by the American Society for Testing and Materials (ASTM Metric Practice Guide, E 380-68) except that additional factors (*) commonly used in the Bureau have been added. Further discussion of definitions of quantities and units is given in the ASTM Metric Practice Guide.

The metric units and conversion factors adopted by the ASTM are based on the "Intemational System of Units" (designated SI for Systeme International d'Unites), fixed by the International Committee for Weights and Measures; this system is also known as the Giorgi or MKSA (meter-kilogram (mass)-second-ampere) system. This system has been adopted by the Intemational Organization for Standardization in ISO Fecommendation R-31.

The metric technical unit of forca is the kilogram-force; this is the force which, when applied to a body having a mass of 1 kg , gives it an acceleration of $9.80665 \mathrm{~m} / \mathrm{sec} / \mathrm{sec}$, the standard acceleration of free fall toward the earth's center for sea level at 45 deg latitude. The metric unit of force in SI units is the newton (N), which is defined as that force which, when applied to a body having a mass of 7 kg , gives it an acceleration of $1 \mathrm{~m} / \mathrm{sec} / \mathrm{sec}$. These units must be distinguished from the (inconstant) local weight of a body having a mass of 1 kg , that is, the weight of a body is that force with which a body is attracted to the earth and is equal to the mass of a body multiplied by the acceleration due to gravity. However, because it is general practice to use "pound" rather than the technically correct term "pound-force," the term "kilogram" (or derived mass unit) has been used in this guide instead of "kilogram-force" in expressing the conversion factors for forces, The newton unit of force will find increasing usn, and is essential in SI units.

Where approximate or nominal English units are used to express a value or range of values, the convirted metric units in parentheses are also approximate or nominal. Where precise English units are used, the converted metric units are expressed as equally significant values.

Table I
QUANTITIES AND UNITS OF SPACE


C.

| scinauluasumx xunat <br> surad surw <br>  | $\begin{aligned} & 6911 \\ & 6990 \\ & \hline 299 \end{aligned}$ |  ( 80 иeamid) sullod (nossturatirn <br>  |
| :---: | :---: | :---: |
|  |  |  |
|  |  |  |
|  |  |  |
|  |  |  |
| ием\1! |  |  |
|  |  |  |
|  |  |  |
|  |  |  |
|  |  |  |
| 2 9 \%60p | 2\%'t |  <br>  |



-sazé м м













## 10VH1Sg*


 เəן











10VHISGV
 ач7 цıоq лод иәл! 6 әде sıиә!

 sy,





 'paısà sem кем


 дəן












[^0]:    *Rouve, Dr. Von Ing. Gerhard, Der Krafthaustrennpfeiler, Stromung sverhaltnisse an gekrummten Wanden, Januair 1958.

[^1]:    B. Recommended elliptical pier design. Photo P622-D-74341

