PERFORMANCE TESTS ON THE PROTOTYPE AND MODEL OF THE
HEART BUTTE SPILLWAY AND OUTLET WORKS
MISSOURI RIVER BASIN PROJECT

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DESCRIPTION OF PROJECT

The Heart Butte Dam is located on the Heart River 60 miles west of Bismarck, North Dakota, and is a part of the Heart River Unit of the Missouri River Basin Project, Figure 1. The dam is of compacted earth fill with a rock riprap cover, rises 135 feet above the Heart River stream bed, and is 1,850 feet long, Figure 2. The project is a combined irrigation and flood control structure, with no power being developed. The reservoir at maximum water-surface elevation containing 395,500 acre-feet of water, which is collected from a drainage area of 1,810 square miles.

The flood control spillway, located near the right abutment, consists of a morning-glory spillway with an outside diameter of 32 feet 6 inches, discharging into a vertical shaft 11 feet in diameter. The shaft is connected to a 90° vertical bend and a nearly horizontal tunnel 14 feet in diameter and about 300 feet long, Figure 3, which leads to the hydraulic jump stilling basin, Figure 2. The maximum vertical fall from headwater to stilling basin floor is about 130 feet.

The morning-glory spillway is unusual in that it is designed to operate throughout the range of free discharge, throughout the transition range between free and submerged discharge, and up to submergences as great as 53.7 feet of water above the crest. The spillway crest is equipped with six equally spaced piers placed radially in plan, but there are no control gates of any kind. The outlet works, used primarily for release of irrigation water, Figures 2 and 3, is an integral part of the spillway structure. The entrance to the outlet works encircles the vertical shaft of the spillway and discharges into a 5-foot 3-inch-diameter tunnel located directly above the spillway tunnel. The smaller tunnel is controlled at its lower end by a 4- by 5-foot, high-pressure slide gate and discharges into the spillway tunnel, entering the larger tunnel from above through a specially designed junction section. The spillway tunnel then carries the outlet works discharge into the single stilling basin used for both spillway and outlet works discharges, Figure 2.

The capacity of the outlet works is 200,000 second feet with reservoir elevation at spillway crest level, elevation 2054.50. For normal operation, the outlet works will be closed when the spillway is in operation.

The capacity of the spillway is 3,600 second feet at maximum reservoir elevation 2118.2. The feasibility of a combined spillway and outlet structure was determined, and the detailed shape and arrangement of the various parts of the structure were developed from hydraulic model tests on a 1:21.5 scale model in cooperation with Spillway and Outlet Works No. 1 and No. 2 design sections.
SUMMARY OF HYDRAULIC MODEL TESTS

The Model

Tests were made on a 1:21.5 scale model of the discharge structures, including the morning-glory, the outlet works intake structure, and the surrounding topography which were constructed within the head box; the two tunnels including the outlet works control gate, the 90° vertical bend, and tunnel junction section, which were built outside of the head box; the stilling basin common to both the spillway and outlet works, and a portion of the down river topography, which were constructed within the tail box. Much of the structure was modeled in transparent plastic to permit the observation of flow conditions throughout the structure, Figure 3.

Spillway and Pier Tests

Tests on a preliminary design of the morning-glory spillway indicated that the discharge capacity of the structure was larger than necessary. Consequently, the vertical shaft diameter was reduced from 14 to 11 feet, the spillway profile was reshaped to fit the vertical shaft, and a 90° vertical transition bend was installed. The discharge capacity was then found to be approximately correct, according to the irrigation and flood control requirements.

Vortices which formed in the model when the spillway was submerged, Figure 4A, were thoroughly investigated, experimentally and mathematically, and when it was found that these same vortices could form to scale in the prototype, attempts were made to eliminate them. Various arrangements of piers, dividing walls, and floating and fixed rafts were tested, and as a result, six spillway crest piers were recommended for use on the prototype, Figure 4B. It was found unnecessary to extend the piers as high as the maximum headwater elevation, a distance of 54 feet. Since vortex action diminished rapidly when the head on the crests approached 14 feet, it was necessary to extend the piers only to this height.

Deflector and Vertical Bend Tests

The tests to determine the most satisfactory type of vertical bend showed that a diverging elbow joining the 11-foot-diameter shaft with the 14-foot-diameter horizontal tunnel had a distinct advantage in that it provided greater space between the water surface and the tunnel crown for ventilation, from the atmosphere at the tunnel outlet to the water surface in the vertical bend.

However, with this arrangement in place, difficulty was encountered in preventing the horizontal tunnel from filling unexpectedly when the spillway and outlet works were both operating. Flow passing
through the bend did not break cleanly from the crown of the bend. The flow had a tendency to follow the crown throughout the bend, causing a change in the location of the flow control. When the control moved downstream the head on the system increased, causing an increase in discharge which filled the tunnel. This, in turn, caused a still greater head with a correspondingly greater discharge and resulted in negative pressures of dangerous magnitudes occurring on the spillway face. Once the tunnel filled, it was impossible to again obtain open channel flow unless the head on the spillway was reduced considerably below the point where it had filled. Consequently, a small deflector was placed at the base of the vertical shaft on the downstream, or crown, side of the shaft, Figure 5. The deflector accomplished three things: (1) it provided a positive control at the base of the vertical shaft and prevented the tunnel from filling, (2) it had a stabilizing effect on smaller flows and provided a flat water surface on all flows passing into the vertical bend, and (3) it provided a clear passage for air to circulate as far upstream as the base of the deflector. The thickness of the deflector at the base was varied in the model to determine the size necessary to exactly meet the discharge requirements at certain heads since precise tests had shown that the 11-foot-diameter vertical shaft was slightly too large. Spillway flow in the tunnel was found to be satisfactory after the structure had been modified as described. Figure 6 shows the flow entering, passing through, and leaving the vertical bend with the deflector in place. Note the smooth and flat water surface on the flow entering the tunnel.

Outlet Works and Tunnel Junction Tests

The outlet works discharge entered the spillway tunnel from above in a junction section as shown in Figure 7A. The jet in striking the tunnel bottom caused a “piling up” of water as shown in the photograph. This caused no difficulty unless the spillway was operating at maximum or near maximum flow. In the high spillway discharge range, the resistance caused by the pile-up in the junction section caused the spillway tunnel to fill, an undesirable condition.

A longer transition was tested in an attempt to eliminate the rough water at the entrance to the main tunnel, and some improvement was obtained, Figure 7B. With the longer transition the tunnel did not fill under any flow condition. Other benefits were minor in nature, however, and it was decided to use the shorter transition with the limitation that the outlet works gate be closed when the spillway was discharging. The larger transition did not provide sufficient improvement to warrant its extra cost.
Stilling Basin Tests

An effective energy-dissipating device was required in the
stilling basin because of the friable nature of the material in the
river channel and riverbanks. Even moderate erosion tendencies and
wave heights could not be tolerated. Consequently, it was felt that
a hydraulic jump basin would be necessary to provide good energy dis-
sipation and a smooth water surface in the downstream channel. The
first stilling basin tests indicated that the main problem was con-
cerned with spreading the high-velocity water, about 60 feet per
second, into a uniformly distributed sheet suitable for the formation
of a jump. The first attempt to induce lateral spreading was by means
of a sudden rise in the stilling basin floor downstream from the tun-
nel portal. It was found that a hump sufficiently long to produce even
a moderate amount of spreading resulted in an extremely long stilling
structure. With a basin of reasonable length, sufficient spreading
could not be produced to permit the formation of an effective jump.
The problem was solved by discharging the flow onto a horizontal floor
about 23 feet long after it had passed through a transition section at
the end of the tunnel which started the spreading of the flow, Figure
8. The flat floor then induced more spreading upstream before the flow
dropped downward on the trajectory curve. Tests showed that this
arrangement produced good lateral distribution of flow as far downstream
as the trajectory curve and fairly good distribution beyond this point.
The addition of two low walls placed so as to divide the basin into
thirds, roughly, gave excellent downstream distribution of flow and an
efficient hydraulic jump in the basin. The walls, which varied from
3 to 4 feet high throughout their length, did not extend upward through
the flow for high discharges, but produced the desired effect of dis-
tributing the flow, from 1/4 feet wide at the tunnel portal to an
ultimate 42.5 feet, in a horizontal distance of 75 feet.

Chute blocks and baffle piers were used to increase the fine
grain turbulence in the basin and thereby reduce the required length of
the stilling basin. The shape of the baffle piers, dividing wall noses,
and trajectory curves were modified to provide atmospheric pressures or
above on critical areas, since tests on preliminary designs had indicated
that pressures as low as 18 feet of water below atmospheric pressure
occurred downstream from sharp corners. The recommended stilling basin
is shown in Figure 8.

The performance of the developed stilling basin was evaluated
from erosion tests made on a movable bed located downstream from the
model basin and from wave height observations made in the excavated tail-

case channel. Erosion tests were made using a well-graded sand (100
percent passed a No. 4 sieve and 3 percent passed a No. 50 sieve). These
tests showed that erosion tendencies were less severe on the channel
bottom than on the sloping sides. Wave action originating in the hydraulic
jump combined with a slight surging action caused rapid decay of the banks. Every effort was made to keep the waves and surges to a minimum, but it was deemed necessary to riprap the banks of the prototype. Figure 9 shows the performance of the recommended basin.

Spillway Air Tests

When the morning-glory spillway was designed, it was felt by some that air introduced into the spillway discharge at a point just below the spillway crest might help to cushion the impact of the flow passing around the vertical bend. It was important that unnecessary impact and vibrations, caused by the flowing water, be eliminated because the entire structure was to be constructed on sand. Furthermore, if for any reason cavitation should occur in or near the vertical bend, the presence of the entrained air might reduce the tendency to damage the concrete tunnel lining. Laboratory tests have shown that even very small quantities of air introduced into the flow will delay the appearance of cavitation damage.

Model tests on the many devices proposed to increase the entrained air in the flow showed that only a relatively small amount of air entered the flow regardless of how the air-entraining devices were arranged. However, it was known that air flow in small hydraulic models is uncertain and that a greater quantity of air can be expected to enter a similar prototype structure. The amount of increase to be expected in the prototype is not known, however, and could not be computed since the factors governing the entrainment of air are not known. After tests on many different model arrangements, it was finally decided to construct the prototype air vents shown in Figure 5 and to provide measuring facilities in the prototype structure so that air quantity determinations could be made. Figure 6 shows the vertical bend discharging 3,750 cfs with air, induced by the air deflectors, entrained in the flow. To the unaided eye the air flow appeared continuous, but in the 1/15,000-second exposure photograph the air appears to enter in gusts. This is more clearly illustrated in the extremely slow motion pictures made of this condition. For a more detailed description of the model tests reference is made to Hydraulic Laboratory Report No. HYD-326, "Hydraulic Laboratory Studies of the Spillway and Outlet Works--Heart Butte Dam--Missouri River Basin Project."

DESCRIPTION OF 1950 SPRING FLOOD

Preceding the heavy run-off in April 1950, the weather had been cold and the ground was frozen and covered with snow. A stiff wind had blown the snow off the ridges, concentrating the snowfall on the slopes and in the valleys of the drainage area. The weather then turned unseasonably warm, causing a fast melt and heavy run-off from the frozen
terrain. On April 15, 1950, the temperature was about 60°, and the snow melt caused an increase in the inflow to the reservoir from 5,000 to 31,500 cfs on April 16, Figure 10. The high run-off and inflow continued throughout April 17 and most of April 18. The spillway went into operation on April 17, reaching a peak flow of 3,760 second feet on April 19 and continued without appreciable reduction in discharge through April 29, a period of over 12 days. The maximum outflow discharge represented 68 percent of the anticipated maximum outflow, and the maximum reservoir elevation indicated that 30 percent of the flood storage had been utilized. Figure 11 shows the hydraulic data in terms of the spillway elevations. At the time of maximum outflow, the spillway crest was submerged 17.24 feet making the reservoir elevation 3.24 feet over the tops of the spillway piers, Figure 11. The maximum height of fall, head water to tailwater, was 72 feet, and the energy entering the stilling basin amounted to 31,000 horsepower.

The Heart River, on which Heart Butte Dam is constructed, flows into the Missouri at Mandan, North Dakota, about 6 miles from Bismarck, Figure 1. Some flood damage occurred at Mandan, caused primarily by high water in the Missouri River. Rail and highway travel were made impossible during the high water. The Heart Butte Dam does not reduce the flood crest at Mandan, but no figures are available as to extent. The structure operated as intended and therefore provided as much protection as was anticipated.

MODEL-PROTOTYPE COMPARISON TESTS

It was recognized that comparison data pertaining to the spillway discharge and the air demand would be particularly valuable and that model-prototype comparisons of the erosion in the excavated channel, wave heights below the stilling basin, and profiles below the stilling basin would also be of interest. In the course of recording these data, other comparisons were made which included observations on vortex formation above the spillway and a comparison of the computed and actual tailwater curves in the excavated channel and in the river. Water-surface profiles in the stilling basin and data on the riprap protection were also obtained.

Spillway Capacity

During the 1950 run-off, when the headwater was above the spillway crest, readings were taken each morning and afternoon on the headwater gage located in the gate operating house. These are shown plotted in Figure 11. Using the discharge-capacity curve obtained from the model tests on the morning-glory spillway, Figure 12, an outflow hydrograph was prepared, Figure 13. On April 17, 19, 25, and May 1, the United States Geological Survey made stream gage measurements in the
river downstream from the stilling basin to determine the discharge of the spillway. During these measurements, the irrigation outlet works was closed. The discharges determined by the United States Geological Survey, indicated by circles, on Figure 13 indicate the degree of agreement between the model and the prototype measurements. Differences were 4.6, 1.1, and 1.8 percent for the April 17, 19, and 25 determinations respectively. For all practical purposes, these points indicate good agreement between model and prototype discharge characteristics. On April 17 the difference was 23.4 percent, indicating considerable disagreement. The measurements on April 17 and May 1 were made, however, under anything but ideal conditions. The United States Geological Survey notes for April 17 indicate that ice in the channel may have affected the measurements, and that on May 1, when the greatest disagreement was found, a wind was blowing which might have altered the relation between the head on the crest and the headwater gage reading. Another possible cause for the discrepancy might be the rapidly falling stage in the reservoir during the measurements on May 1 as indicated in the hydrograph-Figure 13. In general, however, the agreement between model and prototype discharges is considered excellent, particularly at the higher discharges, and it is believed that the rating curves obtained from the model will adequately serve to determine discharge values through the prototype morning-glory spillway.

It may be significant that the prototype discharge measurements consistently indicated a larger flow than was shown in the model. Perhaps the scale, 1:21.5, did not provide a model sufficiently large to overcome the greater viscous and surface tension forces that are normally expected in a small model. Additional prototype discharge measurements, particularly for the lower reservoir elevations, during some future runoffs, would undoubtedly help to establish the exact discharge values for the morning-glory spillway.

Spillway Performance—Free and Submerged Discharges

During the modal tests it was noticed that for certain arrangements of the structure the transition from free to submerged flow, and vice versa, was accompanied by violent surging in the vertical shaft. In some cases the unstable flow condition existed over several feet of change in reservoir elevation. A mushroom-shaped column of water rose and fell in the shaft, causing severe splashing and turbulence. In addition to giving poor hydraulic conditions it was feared that the prototype structure would be subjected to unnecessary forces and vibration. Consequently, the structure recommended for field construction was developed by tests to provide a minimum transition range, i.e., less than 0.2 foot. The rating curve determined by model tests, Figure 12, indicates the definite change from one type of flow to the other. It was for this reason that the prototype spillway was closely observed when the headwater reached the transition range. The following paragraphs discuss the operation of the prototype structure.
On April 16, 1950, the reservoir had risen to the spillway crest elevation 2064.5. Ice covered most of the reservoir area, but there was some open water close to the spillway, Figure 14A. Before flow started over the spillway the tunnel was inspected and ice which had formed around the outlet works gate was removed, Figure 14B. By April 17, 1950, the reservoir had risen sufficiently to submerge the spillway and provide a head of 9.3 feet on the crest, corresponding to a discharge of 3,250 cfs, Figure 15. Sometime during the night the reservoir elevation had passed through the critical region where the flow changes from free to submerged. Some ice had been discharged through the spillway, but it had caused no apparent difficulty. On April 18, the piers were completely covered and the reservoir was covered with ice, Figure 16A, which appeared to be about 12 inches thick. A small amount of trash had collected over the spillway and slight movement of the trash was the only evidence that the spillway existed. The reservoir continued to rise throughout April 19, but on April 20 it started to recede. On April 21 the reservoir was still a foot or so above the piers, Figure 16B. The ice was breaking up fast and the wind was shifting it around the spillway area. Regardless of whether ice or water was over the spillway entrance, the operation was satisfactory, with no evidence of serious vortex action.

On April 26, with the reservoir at elevation 2074 and the piers again visible, operation was also satisfactory, Figure 17.

On April 28, the reservoir was down to elevation 2071, or about 0.7 foot above the point where the flow changes from submerged to free discharge, see Figures 18 and 12. The photograph indicates the mild condition inside the spillway. There was no pulsating or rising and falling of the "mushroom."

On April 29, the reservoir had fallen to 0.8 foot below the critical submergence point and although the "mushroom" was lower in the shaft, it was still stable with no rising and falling evident. Again the flow had passed through the critical range during the night when photographs and observations were not possible to obtain. Indications are, however, that the prototype submerged at about the headwater elevation shown by the break on the curve of Figure 12 and that the change occurred abruptly as also indicated on the model curve.

On April 30, the spillway was discharging freely with reservoir elevation 2068.6, discharge 1,600 cfs, Figure 19. No spray emerged from the glory hole at this or lower heads as has occurred on other glory hole spillways.

Throughout the flow range there was no vibration noticeable in the structure. Several excursions down into the outlet works gate access well were made while the spillway was operating. Efforts were made to
detect vibration in the structure by feeling the various parts of the structure, but none could be detected. Also, there was no "noise" from the spillway at any head that could be detected from the top of the dam or from the reservoir banks. The outlet works gate was opened and closed on April 21, 1950. No noise or vibration was evident during this operation.

One year later, the spillway again went into operation, reaching a maximum reservoir elevation of 2075 or about 7 feet less than occurred in 1950. On March 27, 1951, the reservoir was at elevation 2070.0, Figure 20, about 0.2 foot below the submergence point. Again the operation was satisfactory with no visible difficulty despite the fact that on February 15, 1951, the ice in the reservoir was 36 inches thick. There was no difficulty due to ice.

Spillway Air Demand

Measurements were made in the model to determine the quantity of air being entrained by the spillway discharge as it passed over the air-entraining deflectors located on the spillway face just below the spillway crest, Figure 5. Air-flow measurements in the model were made using a 3/8-inch-diameter sharp-edged orifice connected to a differential water manometer. All air entering the model passed through the orifice before entering the venting system. Since the differential was extremely small for the air quantity flowing in the model, a specially constructed gage was used which multiplied the actual differential so that more consistent readings could be obtained throughout a series of tests. The gage was calibrated to provide reasonably accurate air measurements, but consistency was considered more important than absolute accuracy.

At the time of prototype construction, pipe was extremely difficult to obtain on short notice. Since the model tests continued throughout most of the construction period, only a small amount of pipe and special fittings could be provided for measuring stations in the prototype. Thus, the data obtained from the prototype are not sufficient to determine pressures in various parts of the venting system, but do indicate the quantity of air flow in the prototype for various spillway discharges.

The air quantity flowing in the prototype vents was determined by measuring the air velocity with a Taylor anemometer held in the 18-inch-diameter air vent pipe. Air-velocity determinations were made on one of the vertical pipes contained in the wall of the gate operating house and in one of the horizontal pipes just upstream from the point where it emerges into the tunnel junction section, Figure 21. Concurrently with the air-velocity measurements, pressure measurements were made on the other horizontal air vent using a U-tube containing water for an indicator. The pressure-measuring station is also shown in Figure 21.
Air flow in the prototype was not smooth, as evidenced by the sound of the air flow and from the difficulty experienced in holding the anemometer steady. There was chance for considerable error in any one anemometer measurement and so several determinations were made for each flow in both the vertical and horizontal vent pipes. Readings were taken until it was felt by the observer that a true average had been obtained; a consistent set of readings over a period of say 10 or more minutes was obtained. The anemometer recorded lineal feet of flow which, when divided by the elapsed time, gave the air velocity in feet per second. Each observation was for about 2 minutes so that the average velocity of air flow was that occurring for from 6 to 12 minutes of testing time. Pressures measured in the U-tube also indicated that the air flow was not steady. Differentials varied from plus to minus, but an average reading was easier to obtain than was the air velocity.

The results of the air quantity and pressure determinations are plotted on Figure 22. The percentage of air entrained in the spillway discharge, for both model and prototype, showed a decrease as the discharge increased. In this respect the model predicted the performance of the prototype. The prototype, however, entrained a roughly four times as much air as was predicted by the model. In this respect also, the prototype performed as anticipated except that accurate predictions could not be made from the model tests to determine how much more air the prototype would entrain. Where the model showed air entrainment of 5.5 percent of the water discharge for 1,000 second feet of spillway discharge, the prototype showed 20.5 percent. For 3,600 second feet the model values was 1.9 percent and the prototype 7.7 percent.

The points from which the curves of Figure 22 were drawn are also shown in the figure. The prototype air demand curve was not drawn through the points for 2,500 second feet because the pressure values, which were considered more reliable, indicated that the curve should be drawn below the velocity points. Moreover, the shape of the curve was then similar to the model curve which was based on very consistent data. To further prove the validity of the shape and values of the prototype curve, computations of air flow were made, assuming that both vent pipes carried equal quantities of air and using the usual losses for bends, friction, inlet, etc. The computed values were found to be in fair agreement with the measured values.

Performance of the Stilling Basin

The performance of the stilling basin was satisfactory in every respect and, furthermore, it performed according to the predictions made from the model tests. A general view of the basin and surrounding area is shown in Figure 23.
Water leaving the tunnel appeared to be fully aerated and at the approximate depth indicated in the model studies, Figure 24A. The entire basin contained extremely turbulent water, Figure 25B, and was long enough to obtain the full jump height before the flow entered the excavated channel, Figures 25A and 25B. A considerable amount of spray was thrown into the air, at times, where the outflow from the tunnel plunged beneath the tail water, but most of the spray fell back into the basin. The small amount of spray which fell adjacent to the basin caused no difficulty. Much of the time the flow entered the basin smoothly as shown in Figure 25A. Flow leaving the basin had a relatively quiet water surface with few measurable waves, Figure 25B. There were long-period swells, however, with a maximum height of 12 to 18 inches which were caused by pulsations set up in the stilling basin. The disturbances below the stilling basin were similar to those noted during the model tests.

Water-surface profiles were measured in the prototype for discharges of 3,700, 3,300, 2,350, and 1,050 cfs. These are shown in Figures 26 and 27, along with the profile obtained during the model tests for 5,600 cfs. Although no exact comparisons can be made, the prototype profiles seem to be in good agreement with the model profile. If differences do exist, they are probably due to the greater air entrainment in the prototype, making the prototype profiles slightly higher than those in the model for the same discharge.

Erosion Downstream from Stilling Basin

Erosion tests in the model had indicated that the channel banks just downstream from the stilling basin would be subjected to greater erosion forces than the channel bottom and that rock riprap would be necessary in the prototype to prevent bank damage. The channel bottom was shown by the model tests to be relatively free from erosion tendencies and no damaging erosion was expected there. As a precaution, however, because of the fine-textured friable material composing the channel, rock riprap was used in the prototype channel bottom. No riprap was used in the model tests.

Before the run-off in the Spring of 1950, cross sections had been taken in the prototype channel on May 31, 1949. Following the 1950 run-off, cross sections were again taken on June 15, 1950. Cross sections for both dates at Station 14+00, located just downstream from the end sill and at Station 14+50 located 50 feet downstream from the sill are shown in Figure 28. These typical sections show the maximum erosion depth to be less than 12 inches. Close to the end sill there is no significant erosion. Using all the cross sections taken, Figures 28 and 29, calculations made to determine the volume of material moved indicated that less than 20 cubic yards of material was eroded and removed from the channel bottom during the entire run-off.
Conversely, the channel banks, despite their riprap cover, were eroded to a greater degree. The riprap, however, had been placed in a thin layer, was not well graded as to size, and in places the earth banks could be seen between the individual rocks. Swells were observed to rise over local areas and penetrate very easily into the large voids. When the water receded some of the earth was removed from behind the riprap. This was evidenced by the darker, earth-colored water which could be seen adjacent to the riprap. After several days of operation the riprap had slumped and the earth banks had caved as shown in Figure 30. In spite of the apparent damage to the banks the riprap still continued to provide a good measure of protection to further cutting, however.

The bank damage was not caused primarily by waves of the ordinary variety, since these were only a matter of inches in over-all height, but rather by swells caused by surges in the hydraulic jump. The model stilling basin had been equipped with baffle piers and chute blocks to reduce the over-all length of the stilling basin and decrease its cost. It had been noted during these and other model tests that when a hydraulic jump is reduced in length by the use of artificial devices such as baffle piers that the jump becomes more stable in most respects, but does exhibit a tendency to produce the swells discussed above. The swells are considered the lesser of the evils, however, and are not impossible to cope with. With a thicker application of riprap, containing rock well graded as to size, there probably would have been no damage.

**Tail-water Elevations**

The topography in the model extended only a short distance downstream from the stilling basin into the excavated channel and did not include any portion of the Heart River Channel, Figure 9. Tail-water elevations were set by means of an adjustable tailgates located at the end of the model using a computed curve, tail-water elevation versus discharge, for the Heart River. The excavated channel was designed so that the tail-water elevation to be expected would be essentially the same as that to be expected in the river channel. The tail-water curve used in the model tests and shown in Figure 31 was computed for a point located 200 feet downstream from the axis of the dam in the Heart River.

During the prototype operation it was readily apparent to the unaided eye that the tail-water elevation in the river was considerably lower than that in the excavated channel. Water entering the river from the channel had a steep surface slope and a much higher velocity than anticipated, Figure 32A. Observations, however, were not sufficient to establish whether the tail water in the channel was too high or that in the river too low.
Levels were run, consequently, to determine the tail-water elevation at four separate points for five different discharges. The location of these points, together with the tail-water elevation and discharge are shown in Figure 31, plotted below the tail-water curve used in the model tests. These data show the computed tail-water curve to be 2.3 feet higher at 1,000 second feet and 4.1 feet higher at 3,600 second feet than the actual measured curves in the Heart River. Tail-water elevations measured in the excavated channel more nearly coincided with the computed curve, but at 3,600 second feet the elevation at Point C, Figure 31, taken in a quiet area adjacent to the wing wall at the end of the apron, was 1 foot below the computed curve. Elevations obtained from water-surface profiles taken along the basin centerline agreed with the computed curve, but only because they included the boil height at the end of the apron which was slightly higher than the adjacent tail water.

The model stilling basin was tested to determine the permissible reduction in tail water before the jump was swept off the apron. In the model it was possible to lower the tail water only 3 to 4 feet before the jump was swept out for the maximum discharge of 5,600 second feet. Since the tail-water elevation in the Heart River is 4.1 feet lower, at a discharge of 3,600 second feet, than the computed tail water, it is imperative that a close watch be kept on the excavated channel to prevent damage which might lower the tail water to the level of the Heart River. If this should happen, the jump will, beyond a doubt, sweep out and the apron will operate as a flap bucket. Since the structure is not designed for this type of operation,uspendamagace could result.

Erosion in the Heart River

The difference in water levels between the excavated channel and the river was the cause of the high-velocity flow entering the Heart River. Water leaving the stilling basin was of relatively low velocity and would not have caused ill effects as it entered the river, Figure 25B. The 4-foot difference in elevation, however, caused an increase in velocity which proved to be sufficient to cause considerable damage to the unprotected riverbank downstream, Figure 32B. Some of the damage was caused by the direct effects of the current flowing diagonally across the river and cutting into the far or left bank. A great share of the damage, however, was caused by a large induced eddy in the river, Figure 32B. This eddy caused an upstream current along the left bank which removed large volumes of material from areas considerably upstream from the point where the main flow impinged on the bank. Although the damage was considerable in extent, it had no ill effects on the structure or its operation. Riprap placed in the eroded area will prove of value, however, since the damage will become greater with each successive run-off and the end result is difficult to predict. The bank damage is illustrated in Figure 33. A comparison of Figures 23 and 34 shows the extent of the bank damage which occurred between the start of the run-off and May 5, 1950.
Inspection of Structure Following 1950 and 1951 Floods

An inspection of the spillway conduit was made following the 1950 flood and again following the 1951 flood. Most of the findings are of no importance to this discussion but are contained in correspondence from the District Engineer to the Chief Engineer dated August 17, 1951. Certain findings are of interest here, however, and are discussed in the following paragraphs.

The conduit inspection, in both instances, revealed that the concrete was in excellent condition with the exception of four small eroded areas located in the 90° bend. Following the 1950 flood, plaster casts were made of the two most prominent areas. These are shown about full size in Figures 35 and 36. The largest area is about the size of a human hand and by actual measurement has a maximum depth of erosion of 3/4 inch. The smaller area shows a maximum depth of 1/2 inch. The surfaces shown in Figures 35 and 36 were molded in sponge rubber against the plaster casts made in the field and are therefore an exact replica of the tunnel surface following the 1950 flood.

These areas are located near the invert and near the bottom of the 90° bend. Construction timbers or ice falling into the shaft could have, by impact, caused the surface damage shown. Persons who have viewed the rubber casts have been unanimous in stating that "this damage was not started by cavitation."

Following the 1951 flood, these areas were again noted. Quoting from the official record, "There does not appear to have been any marked change in these areas as a result of the 1951 spring floods." "No repairs are believed necessary at this time."

Plaster casts of these areas should be made from time to time to chart the progress of erosion, whatever the cause. Valuable information, either positive or negative, can be obtained on the durability of concrete in a vertical bend, and it may be possible to determine whether cavitation is a contributing factor to the damage noted.

Inspection of the riprap downstream from the stilling basin, following the 1950 flood, indicated that repairs would be advisable. Quoting again from the official report—"The slumped riprap in the channel immediately downstream from the stilling basin structure was repaired in May and June 1950. Gravel backfill was placed on the slopes to bring them to grade and rock replaced over the gravel. The erosion of the riverbank just downstream from the end of the ripraped channel was sloped and covered with gravel and rock."
The essential parts of the spillway and outlet works were modeled in transparent plastic. The intake for the outlet works encircles the spillway shaft. Outlet works discharge is controlled by the slide gate shown.

HEART BUTTE DAM
Spillway and Outlet Works Model, Scale 1:21.5
A--A violent vortex was formed in the spillway for heads above the submergence point. The tail of the vortex extended down into the horizontal tunnel.

B--Six piers placed radially on the crest reduced the vortex to negligible size.

HEART BUTTE DAM
Morning-glory Spillway Model Tests--Discharge 3,750 cfs
SECTION A-A
HEART BUTTE DAM
Spillway and Outlet Works Entrance Details
Flow in the vertical bend for a discharge of 3,750 cfs. Note the smooth flow in the bend and the flat water surface produced by the deflector at the base of the vertical shaft. 1/15,000-second exposure shows air entering flow in bursts. To the eye air flow appeared continuous.

HEART BUTTE DAM
Hydraulic Model (Vertical Bend) Tests
A--The short junction section recommended for use in the prototype caused some disturbance in the flow at the entrance to the spillway tunnel.

B--A considerably longer junction section was tested. Smoother flow resulted but the improvement did not justify the extra cost.
A--The recommended basin, shown in operation, was reduced to minimum dimensions consistent with acceptable performance.

B--Although some erosion occurred the operation was considered acceptable since riprap protection was to be used in the prototype. Model operated 1/2 hour.

HEART BUTTE DAM
Stilling Basin Model Tests
Discharge 5,600 cfs--Tail-water Elevation 2012
Figure 10

Heart Butte Dam
1950
Flood Hydrographs

Max. Inflow 30,500 cfs
Max. Outflow 3,760 cfs

Flow - CFS

30,000
25,000
20,000
15,000
10,000
5,000

April 14 15 16 17 18 19 20 21 22 23 24 25 26 27 28 29 30
HEART BUTTE DAM
Reservoir Elevations and Hydraulic Data - 1950 Flood

Max. Water Surface Elev. 2115.2

Reservoir Capacity - Acre Feet

392,500
303,200
227,500
165,500
116,000
46,700
25,000
11,400
3300
300

5 10 15 20 25 5 10 15 20 25 5 10 15
MARCH April May
1950
Note: Curve obtained from tests on a 1:21.5 scale hydraulic model.

Crest Elev. 2064.5
Morning Glory

Discharge - Thousands of cfs

HEART BUTTE DAM
SPILLWAY DISCHARGE CAPACITY
HEART BUTTE DAM
MODEL - PROTOTYPE

DISCHARGE COMPARISON

Note: Curve based on prototype headwater gage readings and hydraulic model discharge capacity. Circles are discharge measurements made in River downstream from the dam.
A--On April 16, 1950, the reservoir had risen to the spillway crest, elevation 2064.5. The riprapped upstream face of the dam is at right.

B--Ice in the tunnel, formed from small leaks around the outlet works control gate, was removed before the spillway operated.

HEART BUTTE DAM
Spillway and Outlet Works Tests
On April 17 the reservoir had risen sufficiently to submerge the spillway crest. Some of the ice was discharged through the spillway but the wind had moved some of the ice upstream. Reservoir elevation 2073.8, head on crest 9.3 feet.

HEART BUTTE DAM
Spillway Operation—Discharge 3,250 cfs
A—On April 18 the spillway piers were submerged. Arrow indicates spillway location. Very slight motion on water surface beneath the arrow was noted. Reservoir elevation 2080.2, head on crest 15.7 feet, piers submerged 1.7 feet, discharge 3,650 cfs.
Continuous outflow reduced the reservoir to elevation 2074.0 on April 26, 1950. Ice hides the slight disturbance over the glory hole. Construction timbers lodged on tops of piers.

HEART BUTTE DAM
Spillway Operation--Discharge 3,260 cfs
On April 28, 1950, the reservoir was at elevation 2071, or about 0.7 foot above the point where the flow changes from free to submerged. Action inside the morning-glory is very mild. Note flow lines visible on water surface.

HEART BUTTE DAM
Spillway Operation--Discharge 3,090 cfs
The spillway was discharging freely on April 30, 1950, with reservoir elevation 2068.6.

HEART BUTTE DAM
Spillway Operation--Discharge 1,600 cfs
In the Spring of 1951 the reservoir rose to elevation 2075.0. This photo, taken on March 27, shows the reservoir at elevation 2070.0, or about 0.2 foot below the submergence point. In February the ice was 36 inches thick but no difficulties due to ice were encountered.
HEART BUTTE DAM
Spillway Air Vent System

PLAN

VENTS OPEN TO ATMOSPHERE AT TOP OF COLD TUNNEL

SECTION A-A

12 - 6' pipes, radial in plan

10' Pipe

SECTION

Vents open to tunnel junction section
See Figure 2
Stilling basin, excavated channel, and Heart River as seen from the top of the dam. Basin was very effective in dissipating energy. Outflow is about 56 percent of capacity. April 17, 1950.
A—Flow entering the basin was well aerated and well distributed across the basin width.

B—The profile of the hydraulic jump is indicated along the stilling basin wall. Flow leaving the basin is smooth and uniform.

HEART BUTTE DAM
Stilling Basin Performance—Discharge 3,600 cfs
Flow from the tunnel was spread to the entire basin width by the dividing walls, which, for this discharge, are submerged.
Do not smudge grid lines!!

E.1.2017

Model - 5000 cfs
April 21 - 5700 cfs
May 1 - 1050 cfs

Heart Butte
Model-Prototype Comparison
Shiffling Basin Profile
Sheet 106
HEART BUTTE DAM
CROSS-SECTIONS BELOW STILLING BASIN

Sections taken May 31, 1949
Sections taken June 15, 1950
A—Loss of bank material was caused by swells removing fine material from behind the coarse riprap. Note man standing on the riprap.

B—Loss of bank material also occurred along the right bank, particularly near the junction of excavated channel and river.

HEART BUTTE DAM
Erosion of Excavated Channel Banks
HEART BUTTE DAM

COMPARISON OF MEASURED AND COMPUTED TAILWATER ELEVATION

Symbols
- POINT A
- POINT B
- POINT C
- U.S. Survey

Location of Measuring Stations

Computed Tailwater Curve for Heart River

Measured Tailwater Curve in Excavated Channel

Notes:
- Computed curve is used in model tests.
- Water surface profile points are higher than tailwater at C because of boil at end of apron.
A--Flow entering the river from the excavated river channel was accelerated by the difference in elevation apparent in the photograph. At 3,700 cfs the difference was about 4 feet.

B--The high-velocity concentrated flow into the river set up a back-eddy which damaged the riverbank upstream from the flow impact.

HEART BUTTE DAM
Flow Conditions--Junction of Channel and River
After flood had receded the loss of bank material opposite the excavated channel was readily apparent.
Over-all view after flood had passed shows extent of downstream bank erosion on May 5, 1950. Note bars formed from eroded material. Compare with Figure 23.
One of the four eroded areas found in 90° bend after the 1950 flood had passed. This area, shown full size, has the deepest erosion, 3/4 inch.

HEART BUTTE DAM
Eroded Area in 90° Bend--"Upper Right"
Another eroded area in 90° bend, shown full size. This area, the largest of the four round, has a maximum erosion depth of 1/2 inch. 1971 flood did not cause measurable increase in area or depth.

Depth in feet.