



**Shaking Table Model of a Concrete Gravity  
Dam for Computer Code Validation  
Monolithic Model**



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**U.S. Department of the Interior  
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*by*  
**Terry Payne**

**U.S. Department of Interior  
Bureau of Reclamation  
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Denver, Colorado**

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Denver, Colorado

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Monolithic Model

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Bureau of Reclamation



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## **I INTRODUCTION**

Safety of dams under earthquake loading has always been a major concern in seismically active regions because of the high potential hazard that uncontrolled release of the reservoir poses to the population downstream of the dam. The current practice for the evaluation of the dynamic response of concrete dams at the U.S. Bureau of Reclamation is to initially preform a linear elastic finite element analysis of the structure under static loads plus the maximum credible earthquake predicted to occur at the site. If the response of the structure indicates that significant cracking damage would occur based on high tensile stress results, then non-linear analyses would be completed. In recent years a number of finite element programs have become available to structural engineers which provide the capability of modeling vertical contraction joint opening and concrete cracking which may occur in concrete arch dams during a seismic event. The Bureau of Reclamation has recently purchased the ABAQUS finite element program which is capable of performing non-linear cracking analyses. The ABAQUS program includes a brittle cracking material model for concrete. This is a fairly complex analytical tool and engineers in Reclamation's structural analysis group need to develop expertise in performing and understanding non-linear modeling and analysis techniques. A set of calibration models would provide a valuable data set for those performing the numerical studies to assure that known results can be obtained. Structural engineers and material engineers need to work closely to develop new standards for material testing so that the appropriate material properties are available for these analyses. Therefore a shaking table test of a 1/50 scale cantilever monolith of Koyna Dam was built at Reclamation's Material Testing Laboratory for use in calibrating linear-elastic and non-linear material properties, as well as to provide a means of evaluating the effect of various analysis parameters available in the ABAQUS program. Two models were tested, a model with a natural but preexisting crack and a monolithic model.

The ultimate goal of the shaking table test program was to develop a correlation between the material testing program and material property requirements for the non-linear numerical concrete cracking model. But before this goal can be accomplished the basic linear elastic material properties needed to be calibrated and the effects of various analysis parameters needed to be understood. These requirements were accomplished through comparisons of analytical results with laboratory measurements. This report is concerned primarily with these preliminary studies, although some non-linear analysis results are also presented.

## **II LOW STRENGTH MATERIAL DESIGN AND TESTING**

### **II.1 Similitude Requirements**

Koyna Dam is a 338 foot high concrete gravity dam in India which suffered cracking during a magnitude 6.5 earthquake in 1967. The geometry of the shake table model was scaled from Koyna Dam. Previous shake table research was completed by Doctors Akira Niwa and Ray Clough in 1980[7]. They performed shaking table tests to investigate the feasibility of studying the nonlinear response behavior of concrete dams. Their research concluded that

shaking table research is a practical means of studying the nonlinear earthquake response of concrete dams and obtaining their actual failure mechanisms.

In the present study numerical models were compared to laboratory results so exact similitude relationships were not required but to the extent possible similitude relationships were maintained. The model scale chosen was 1/50 scale. Similitude requirements for the models, estimated dam material properties, associated scale factors and the model material target values are summarized in Tables 1 and 2.

Table 1: Similitude Requirements For a 1/50 Scale Dam Model		
Component	Variable	Required Scale Ratio model / prototype
Dam	Unit Weight Length Elastic Modulus Ultimate Strength Poisson's Ratio Strain Force	$\rho = 1$ $L = 1/50$ $E = 1/50$ $\sigma = 1/50$ $\nu = 1$ $\epsilon = 1$ $F = (1/50)^3$
Earthquake Motion	Displacement Acceleration Duration and Period	$L = 1/50$ $a = 1$ $T = (1/50)^{1/2}$

Table 2 : Dam Material Properties			
Property	Prototype Estimate	Scale Factor	Target Value
E	4,000,000 psi	1/50	80,000 psi
$f_c'$	4,000 psi	1/50	80 psi
$f_t$	400 psi	1/50	8 psi
Density	150 pcf	1	150 pcf
$\epsilon_u^c$	0.0025	1	0.0025
$\epsilon_u^t$	0.00012	1	0.00012

## II.2 Concrete Mix Design

In this study a low strength concrete mix was designed to produce a concrete like material which would to the extent possible maintain similitude relationships, and yet be simple enough for direct comparisons with computer predicted results. Consideration was also given to reproducing the correct failure mechanism at model scale. A trial mix was initially made in the U.S. Bureau of Reclamation Materials Testing Laboratory . Bentonite pellets were used to reduce the material strength. In the laboratory trial mix the bentonite pellets were saturated overnight before they were added to the mix. Material property testing was completed on the trial mix which resulted in reasonable strength properties for use in the test model. Then a commercial concrete company(Colorado Ready Mix) was hired to produce the approximately 6 cubic yards of material needed for the model. The commercial company attempted to accomplish the saturation in the mixer drum during transit. The water was also adjusted from the original design at the plant due to the desire to decrease sloshing in transit. As a result the material properties of the commercially supplied material actually used in the model were not the same as those produced in the laboratory trial mix. Table 3 shows the mix components for both the laboratory trial mix and the commercially supplied mix which was actually used in the model. The material properties produced in the laboratory trial mix and the commercially produced mix are shown in Table 4.

Component	Lab Mix Wt. per cu. Yd.	Volume in mix	Model Mix Wt. per cu. Yd.	Volume in Mix
Air		0.14 (assumed by 1/2% entrapped air)		0.52
Water	560	8.99	480	7.68
Cement	160	0.82	168	0.86
Bentonite	40	0.25	42	0.26
Sand	1336	8.4	1454	8.87
No. 4 - 3.8" Gravel	553	3.36		

### II.3 Laboratory Material Property Test Results

Both standard and specialized laboratory testing was done in the material testing laboratory[9]. Static compressive strength was determined following the American Society for Testing and Materials (ASTM) C 39 "Standard Test Method for Compressive Strength of Cylindrical Specimens." The modulus of elasticity was determined as per ASTM C 469 "Standard Test Method for Modulus of Elasticity and Poisson's Ratio in Compression." [1] All of the compressive cylinder tests failed in a classic shear plane typical of concrete (approximately 65 degrees). Figures A.1 through A.3 show the resulting stress-strain curves for three tests.

Dynamic tests were performed following the ASTM procedures for the static tests with the exception of loading rate. A uniaxial testing machine capable of providing failures within a strain rate of  $10^{-3}$  and a time frame of approximately 0.1 seconds was used for the three dynamic compression tests. Figures A.4 through A.6 show the stress-strain curves resulting from the rapid compression tests. Typical unload-reload data resulting from cyclic compression tests is shown in Figures A.7 and A.8. Fracture (crack width versus load - beam test ) data is shown in Figure A.9. The material density was measured as 138.2 pcf.

Table 4 : Laboratory Material Test Results Material Properties for Koyna Dam (Monolithic Model) Low Strength Concrete Age: 15 days		
PROPERTY	ACTUAL KOYNA MIX	TARGET VALUE
Slump	8 inches	8 inches
Density	138.2 lb/ft <sup>3</sup>	150 lb/ft <sup>3</sup>
Static Modulus of Elasticity	157,000 lb/in <sup>2</sup>	80,000 lb/in <sup>2</sup>
Dynamic Modulus of Elasticity	113,000 lb/in <sup>2</sup>	-
Ultimate Static Compressive Strength	203 lb/in <sup>2</sup>	80 lb/in <sup>2</sup>
Static Tension		
Splitting Tension	27 lb/in <sup>2</sup>	8 lb/in <sup>2</sup>
Beam Tension	60 lb/in <sup>2</sup>	8 lb/in <sup>2</sup>
Dynamic Tension	52 lb/in <sup>2</sup>	-
Ultimate Strain ( $\epsilon_u$ )	0.004	0.0025

### III LABORATORY SHAKE TEST SET-UP AND PROCEDURE

#### III.1 Model Geometry

The laboratory shake table tests were completed at the U.S. Bureau of Reclamation, Materials Engineering and Research Laboratory[9]. A shake table for large scale tests has been in existence at Reclamation since 1969. The shake table was set up for this experiment using steel I beams to attach the Koyna scaled model to the table. Figure B.1 shows the Koyna monolithic model mounted on the shake table. Accelerations were applied to the model in the upstream downstream direction only(one dimensional shake test). The table was tested using ultrasonic methods for response modes and tested in motion with accelerometers to determine capabilities for higher frequencies. Input frequencies below 26 Hz gave good responses but higher frequencies were eliminated from testing. Response of the table was clearly best at frequencies of 26 Hz and below. A similitude simulation of an earthquake motion was not used. Rather, for practical reasons associated with the table, and for simplicity in numerical model calibration a sinusoidal motion was selected.

Figure B.2 and B.3 show the Koyna scaled model geometry and the steel I beam setup. The 1/50 scale model resulted in a 8.5 foot tall model weighing 7850 pounds. The first model tested was cast laying down on its side. The casting and forming operation was easier to completed in this case, but after a period of approximately 20 days a small shrinkage crack appeared in the exposed face. When at approximately 28 days, the model was positioned on the shake table and the forms were removed. The shrinkage crack was evident on all four faces of the model so it was assumed to extend through the model thickness. The plane of the crack had an inclination of approximately 20 degrees from horizontal towards the side of the model. This model is referred to in this report as the "cracked" model in reference to the preexisting shrinkage crack. The second model tested had the concrete forms constructed on the shake table so that the concrete for the model could be poured on the shake table with the model in the upright position. This was done to avoid the potential for shrinkage cracking. By pouring the second model upright on the shake table, and by testing earlier(15 days) the onset of shrinkage cracking was avoided and the second "monolithic" or "uncracked" model produced a material failure under dynamic loading. Earlier testing also held the curing strengths lower. The test cylinders of this material were poured on the same day as the model and tested immediately following the breaking of the model.

#### III.2 Loads

The only static load included in the analyses in this study was the gravity load. The primary focus of this study was the dynamic material properties and the response of the model to dynamic loading. Two input motions were used in the monolithic model study. The first input record (SHAKEA) was used to determine the natural frequencies of the model. The second input record (SHAKEB) was used to fail the model.

SHAKEA was a sinusoidal forcing motion applied to the model in the upstream/downstream direction only, with a constant acceleration of 0.1 g, and with frequencies starting at 2 Hz, and then increasing in 2 Hz increments to 30 Hz. The acceleration time history

plot (Figure B.4) shows the upstream-downstream acceleration time history measured at the base of the model(Accel#1). This acceleration time history was used as an input motion for the ABAQUS analyses.

SHAKEB was a sinusoidal forcing motion with a constant frequency of 14 Hz (figure B.5). In this input record the acceleration amplitude was increased in 0.2 g increments until failure of the model occurred. This input motion was selected at the time of placement of the cracked model(Koyna I). Numerical analyses for the cracked model predicted a fundamental mode of 14 Hz. The results of the cracked model study are not included in this report, they are mentioned here only in reference to the selection of a 14 Hz sinusoidal input motion for the laboratory tests in which the models were shaken to failure.

The acceleration response spectra at 5 percent damping for both input motions are shown in Figure B.6. The response spectrum for input record SHAKEA indicates that structures with a natural frequency in the range of 3 to 5 Hz would have the most significant response to this input record. The response spectrum for input record SHAKEB indicates that structures with a natural frequency in the range of 14 to 15 Hz would have the most significant response, as expected. These response spectra were used as input for response spectrum analyses in ABAQUS.

### **III.3 Boundary Conditions**

The rectangular base of the model was poured continuously with the Koyna portion of the model and acts as a foundation block. All-thread rods were embedded in the foundation to provide a means of anchoring the model to the shake table as shown in Figure B.1. Some unforeseen problems with these boundary conditions developed during the test in which the model was shaken to failure. Prior to failure of the dam, the all-thread rods embedded in the base of the model began to break loose allowing the model to rock. As more material around the all-threads failed, the rocking of the model increased which resulted in increasing vertical accelerations. Eventually the material failure around the all-thread was severe enough that the entire model could slide back and forth a small amount in the direction of the excitation. This was evident in the measured displacement time history records shown in Figure B.7 at LVDT#1 which was located on the model base. The figure shows that the displacements oscillated about an initial offset of approximately -0.04 inches until approximately 300 seconds into the test. From this time on the position about which the measured displacements tended to oscillate drifted and an indeterminate non-linear boundary condition had developed. No attempt was made to duplicate these non-linear boundary conditions in the numerical analysis, but it is believed that general comparisons can still be made based on the final accelerations and the material properties presented.

### **III.4 Instrumentation**

Instrumentation was designed to measure displacements, and accelerations on the model. The general instrumentation locations are shown in Figure B.8 Accelerometers #1, #4, #5, and #6 were positioned at various elevations on the upstream face of the Koyna model and set to measure horizontal accelerations in the upstream/downstream direction. Accelerometers #1, #2, and #3 are all located at the same position and measure accelerations in the

upstream/downstream, cross-canyon, and vertical directions respectively. These three instruments were positioned at the top of the foundation block on the upstream face of the model. Accelerometer #8 was positioned at the center of the top surface of the model and was set to measure vertical accelerations. Four LVDT's were used to measure upstream/downstream displacement time histories during the laboratory tests. LVDT#1 was positioned on the downstream face of the foundation block. LVDT#2 was positioned on the upstream face at a height of approximately 5 foot above the bottom of the foundation block. LVDT#3 was positioned on the sloping surface of the downstream face, while LVDT#4 was positioned above the change in slope on the downstream face. All of the instruments were placed at the model center line with respect to the cross canyon direction.

#### **IV LABORATORY SHAKE TEST RESULTS**

##### **IV.1 Modal Characteristics Determined From Laboratory Measurements**

The acceleration time histories recorded during the laboratory test using input record SHAKEA provide an indication of the modal characteristics of the model. Since the frequency of the input motion in SHAKEA was stepped through even frequencies from 2 to 30 Hz at a constant amplitude, any clear jumps seen in the accelerations measured on the model can be used to identify resonant frequencies in the model. Figures C.1 and C.2 show the acceleration time histories measured at each of eight accelerometers during the laboratory test using input motion SHAKEA. Figure C.1 shows the upstream-downstream, cross-canyon, and vertical acceleration time histories measured at the base of the model using accelerometers #1, #2, and #3. Figure C.2 shows the vertical acceleration time history measured at the top of the model using accelerometer #8. Figure C.1 and figure C.2 show the upstream-downstream acceleration time histories measured at accelerometers #4, #5, #6 and #7.

These acceleration records also provide evidence concerning the orientation of the mode shapes associated with these resonant frequencies. The plots show that a significant jump in the model's cross-canyon and vertical response occurred at an input frequency of 18 Hz. A corresponding jump is not seen in the upstream-downstream records. Measurements from accelerometers #5, #6, and #7 actually show a decrease in upstream-downstream response when the input motion's frequency was 18 Hz. This suggests that the model's first mode acts primarily in the cross-canyon and vertical directions and that the first natural frequency is approximately 18 Hz. The upstream-downstream accelerations also show a gradual increase in amplitude peaking at 24 Hz suggesting that a second cantilever mode acting in the upstream-downstream direction may occur at 24 Hz.

There was also a definite jump in the model's cross-canyon response to the input motion at a frequency of 30 Hz. The model's upstream-downstream and vertical responses were also high at 30 Hz. This is the first resonant frequency of the table and may not be significant in terms of the response of the model.

Since the material properties of the model effect the mode shapes and natural frequencies, it may be possible to use this information from the excitation of the laboratory



Both methods result in a very low damping factor(1 to 2 %). Low level forced vibration field tests on dams typically result in viscous damping ratio's in the range of 1 to 3 percent, while the use of 5 to 10% viscous damping is considered reasonable for dams under large earthquake loading. The use of 5 to 10% viscous damping in the analysis of dams is reasonable because of the existence of vertical contraction joints in the structure which provide a physical damping mechanism. The laboratory model is a solid structure rigidly fixed to the shaking table so a viscous damping ratio of 1 to 2% is reasonable for the analyses in this study.

### **IV.3 Measured Acceleration and Displacement Time Histories**

Figures C.1 and C.2 show the time history plots of accelerations measured during the modal sweep(input record SHAKEA) testing procedure. The displacement time histories measured at the four LVDT's during this laboratory test are shown on Figure C.4. Acceleration time history plots from the second laboratory test, in which the model was shaken to failure(input record SHAKEB), are shown in Figures C.5 and C.6. Displacement time histories from the second shake test are shown in Figure C.7.

### **IV.4 Final Failure Mode**

Figure C.8 shows the final failure surface as it occurred during the SHAKEB laboratory test. Development of a crack through the model and failure occurred very quickly. The test was videotaped using a standard video frame rate of 1/30 of a second. When this film record was reviewed frame by frame after the test it was observed that a failure surface was not visible in one frame and had developed and propagated through the structure by the next video frame. So a through crack developed in less than 0.03 seconds. It was also noted that after initiation of the crack the top of the model began to slide before toppling occurred. The top portion toppled from the model approximately 1 second(14 cycles) after crack propagation began.

## **V ABAQUS LINEAR-ELASTIC FINITE ELEMENT ANALYSES**

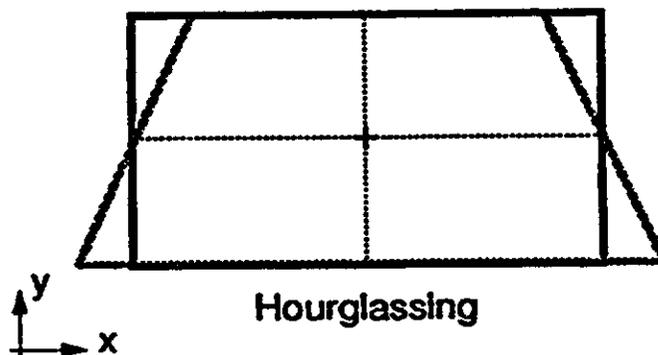
The ABAQUS finite element analysis program has both linear and non-linear analysis capabilities. This portion of the study focuses only on linear elastic dynamic analyses. Performing a linear elastic analysis is the first level of investigation in evaluating the response of a dam-reservoir-foundation system to an earthquake loading. Linear elastic analyses are less expensive than non-linear analyses. While linear elastic analyses cannot predict plastic deformation, crack propagation, or the stress distribution after cracking has occurred, a preliminary linear elastic analysis can be used to calculate natural frequencies and to determine whether or not a non-linear analysis is required through comparison of concrete stress levels with strength properties and to calibrate linear elastic material properties used in a study. Linear elastic dynamic analyses can be performed by using the implicit direct-integration or modal superposition procedures in ABAQUS/Standard[6], or by using an explicit direct-integration procedure in ABAQUS/Explicit[5]. ABAQUS/Standard and ABAQUS/Explicit are separate program modules within ABAQUS. First, modal superposition procedures using ABAQUS/Standard were used for frequency extraction, modal dynamic time history analysis, and response spectrum analyses. The results of these analyses were then compared to the results

from an implicit direct-integration dynamic analyses performed using ABAQUS/Standard and an explicit direct-integration analyses performed using ABAQUS/Explicit. Wherever possible the results from each analysis were compared to laboratory measurements. Sensitivity studies were also completed for various analysis parameters, material property parameters and mesh definitions.

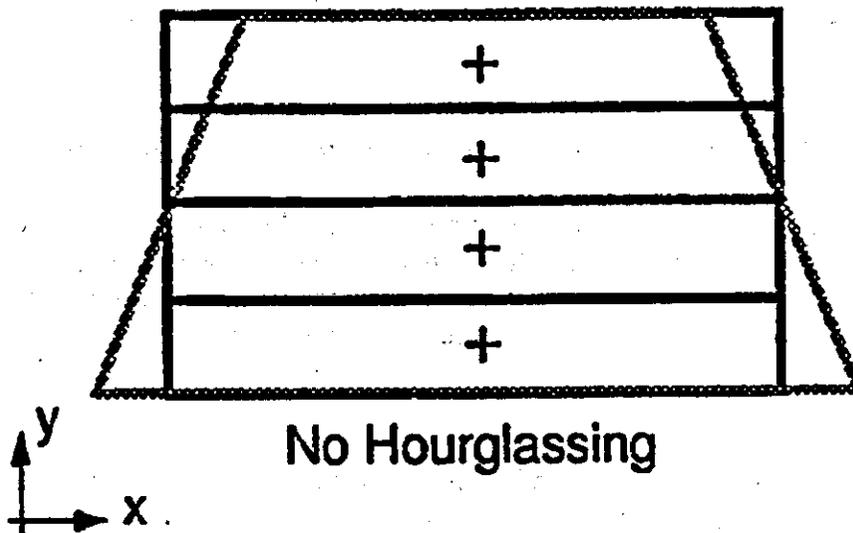
## V.1 Finite Element Models

Six different finite element meshes were used in the analyses of the Koyna scale model. All of the analyses use the same three-dimensional solid model which was created to match the physical dimensions of the laboratory model(See Figure B.3). The ABAQUS element type designated "C3D8R" was used in all the models in this study. This is an eight noded, reduced-integration, three dimensional solid brick element with hourglass control. ABAQUS/Standard has a very extensive element library, while the ABAQUS/Explicit element library is more limited. In ABAQUS/Standard fully integrated 3D brick elements are available with both 8 and 20 nodes, in ABAQUS/Explicit only 8 noded 3D brick elements with reduced integration are available. The 8 noded, reduced integration, 3D brick element was selected for this study primarily to facilitate comparisons of results from ABAQUS/Standard and ABAQUS/Explicit in the non-linear analyses to be completed later. The use of tied contact surfaces in ABAQUS was also investigated. A tied contact surface is used to mathematically link two separate finite element models along a common boundary.

The issue of mesh density is particularly important when linear reduced-integration elements are used. These elements can have a numerical characteristic called "hourglassing". The following figure shows the deformed shape of a linear element with reduced-integration subjected to pure bending. Since this is a linear element with only 8 corner nodes the element edges are not curved, and since this is a reduced integration element it has only one integration point located at the element centroid. When the vertical and horizontal element dimensions are measured through the integration point their length does not change and the angle between them remains 90 degrees in the element's deformed shape. Therefore all of the components of stress at the element integration point are zero and there is no strain energy generated by this element in bending. So if a single linear, reduced-integration element were used through the thickness of a beam model, all the integration points would lie on the neutral axis and the model would be unable to resist bending loads.



However if enough elements are used through the model thickness then linear reduced-integration elements produce acceptable results in bending. The next figure illustrates the deformed shape resulting when four elements are used through the thickness of a model subjected to bending loads. In this case the horizontal element length measured through the integration point in the top element decreases in the deformed shape indicating that the direct stress in the x-direction ( $\sigma_{xx}$ ) is compressive; while the horizontal element length measured through the integration point in the bottom element increases indicating that  $\sigma_{xx}$  is a tensile stress. The angle between a vertical line drawn through all the integration points and horizontal lines drawn through each integration point remain at 90 degrees so the shear stress remains zero. In this case, conditions are consistent with the expected state of stress for pure bending and acceptable results are achieved.



The finite element models varied in element mesh density and orientation. Mesh densities were increased in localized regions of the model around tied contact surfaces. These meshes were identified as Mesh#1, Mesh#2, Mesh#3, Mesh#4, Mesh#5 and Mesh#6. Mesh#1 and Mesh#2 both used tied surfaces to change the mesh density near the change in geometry on the downstream face of the model. Mesh#1 has a finer mesh density than Mesh#2, and the upper tied contact surface is closer to the change in geometry than the tied surface in Mesh#2. The other four mesh definitions do not include any contact surfaces. Meshes #3,#4 and #5 all used a vertical-horizontal mesh orientation with varied densities. Mesh#6 included a sloped mesh orientation. Figures D.1 and D.2 show the six finite element mesh definitions used, while the following table provides a summary of the mesh characteristics.

Mesh Designation	Number of Elements	Number of Nodes	Number of Tied Contact Surfaces
Mesh#1	1470	2102	Two
Mesh#2	484	784	Two
Mesh#3	612	889	None
Mesh#4	2160	2826	None
Mesh#5	84	180	None
Mesh#6	252	410	None

## V.2 Boundary Conditions Used For The Finite Element Analyses

The same displacement boundary conditions were used for all of the mesh definitions in this study . All the nodes on the bottom of the model base and on the upstream and downstream faces at and below 23.625 inches were identified as fixed nodes against all three components of translation. The displacement boundary conditions are shown in Figure D.3.

## V.3 Loads

The loading sequence used for all of the linear-elastic sensitivity studies was to apply the gravity load in the first analysis step, followed by a frequency extraction step only when modal superposition dynamic procedures were used, and then to apply the laboratory input accelerations to the numerical model in the upstream/downstream direction in the final analysis step. Accelerations were applied at the fixed nodes. Input motion SHAKEA was used for the majority of the linear-elastic analyses because this was a low amplitude acceleration record and therefore the response of the model to this loading was expected to stay well within the linear-elastic range. One second of the SHAKEA acceleration record was extracted from the laboratory data for use in the sensitivity studies. The entire record is approximately 480 seconds long so it was not feasible to analyze the entire record. One second of the SHAKEA record at a point where the frequency was 14 Hz was selected because the entire SHAKEB input acceleration record which will be used for the non-linear analyses has a frequency of 14 Hz.

## V.4 Linear Elastic Material Property Model

The ABAQUS linear elastic material model was used for all of the analyses in the first part of this project. The total stress is defined from the total elastic strain as :

$$\sigma = D^{el} \epsilon^{el}$$

where  $\sigma$  is the total stress,  $D^{el}$  is the fourth-order elasticity tensor, and  $\epsilon^{el}$  is the total elastic strain. This material model is only valid when the elastic strains are small. The ABAQUS elastic material model can be either isotropic or anisotropic. The low strength concrete mix used in this study was considered to be homogeneous and isotropic. The elastic properties were completely defined by the Young's Modulus(E), and the Poisson's ration( $\nu$ ).

## V.5 Output Locations

Figures D.4 to D.9 show the output locations from ABAQUS used for accelerations and displacements for each of the six meshes used in this study. Each figure shows plan and elevation views of a mesh with the nodes at which accelerations and displacements will be requested as output shown in red. The elevations of these nodes are listed on the figures as well as the elevations at which the instrumentation were actually located on the laboratory model. Therefore these figures provide documentation of how closely the location of the nodes at which output is generated in the ABAQUS analyses match the actual locations of the instructions used in the laboratory for each of the six different mesh definitions.

## VI SUMMARY AND CONCLUSIONS FOR INDIVIDUAL LINEAR ELASTIC SENSITIVITY STUDIES

### VI.1 Sensitivity of Results to the Number of Modes Extracted in Frequency Analysis

Since both the modal dynamic and response spectrum analysis procedures base the structure's response on a subset of the eigenmodes of the system, the eigenmodes must be extracted prior to running these analyses. The number of modes extracted must be sufficient in each case to model the dynamic response of the system adequately. To determine the number of modes which must be extracted in the frequency analyses for convergence of results in the dynamic analysis, four modal dynamic analyses were completed using 2, 3, 10, and 20 modes. These analyses were completed using Mesh#3, with an elastic modulus of 150 ksi and a material density of 138 pcf.

The resulting accelerations, displacements and CPU times were compared. The results from this sensitivity study are shown in Figures E.1 to E.4. The first three natural frequencies were 15.7, 29.9, and 54.2 Hz. Calculated peak accelerations and displacements are shown on Figures E.1 and E.2. CPU time are also listed on Figure E.1. Acceleration time history plots are shown on Figure E.4.

The results from modal dynamic analyses using from 2 to 10 modes showed only slight differences in peak accelerations and displacements, and the results from analyses using 10 and

20 modes were nearly identical. CPU times ranged from 53 sec, when only 2 modes were extracted, to 210 sec when 20 modes were extracted. CPU times included a static loading step used to apply gravity, the frequency extraction step, and a one second modal dynamic analysis step. The one second input record used was from input record SHAKEA from 279 sec to 280 sec. This section of the SHAKEA input record has a magnitude of 0.1 g and a frequency of 14 Hz.

This study indicated that only the first two modes need be extracted to obtain reasonable results and that results had completely converged when 10 modes were used. Ten modes were extracted and used in the modal dynamic analyses through out the remainder of the linear elastic analysis studies.

## **VI.2 Sensitivity of Modal Dynamic Results to Variation in Mesh Definition.**

The six different finite element meshes were analyzed using the modal dynamic procedure to determine the effects of variations in density, orientation, and the use of tied contact surfaces. Identical linear elastic material properties were used for each of these analyses. The elastic modulus was 150 ksi and the material density was 138.2 pcf. Five percent modal damping was used. One second of input record SHAKEA from 279 to 280 sec was used as the ground motion for these comparisons. Modal characteristics, accelerations and displacements at the locations of instrumentation, energy levels and the CPU times for each analysis were compared.

Figures F.1 to F.12 contain the results of the modal dynamic analyses used to evaluate mesh sensitivity. The modal characteristics were very similar for all the mesh definitions. The first natural frequencies varied from 14.1 Hz for Mesh#5(a very coarse mesh) to 15.7 Hz for Mesh#4(a very fine mesh definition see figure F.1). Accelerations and displacements were also very similar for all the mesh definitions, but they were slightly higher for the coarser mesh definitions. The peak acceleration for Mesh#6(coarse) was 71.4 inch/sec<sup>2</sup>, while the peak acceleration for Mesh#4(fine) was 69.4 inch/sec<sup>2</sup>. The peak displacement for Mesh#5(coarse) was .0025 inches, while the peak displacement for Mesh#4(fine) was .0021 inches. The CPU time required to complete the analyses varied significantly for different mesh definitions. Fine mesh definitions such as Mesh#1, which also includes two contact surfaces, and Mesh#4, which has a very fine mesh definition with no contact surfaces, required 895 seconds and 446 seconds respectively, while the analysis of Mesh#5, which has a very coarse mesh definition and no contact surfaces, only required 21 CPU seconds. Figure F.1 contains tabulated natural frequencies, peak accelerations and displacements and CPU times from these analyses. Figures F.2 and F.3 show the calculated acceleration and displacement time history plots from the mesh sensitivity study; as well as, the acceleration and displacement time histories measured in the laboratory.

Figure F.4 shows tabulated values for various whole model energy quantities at the end of the static and dynamic load steps for the analyses using each mesh definition. Hourglassing can be a problem with first-order, reduced-integration elements, such as the C3D8R elements used in these analyses. The C3D8R ABAQUS elements include hourglass control, but they

should also be used with reasonably fine meshes. ABAQUS monitors the amount of energy spent on controlling hourglassing during the analysis, so the energy levels can be used as an indicator of acceptable/unacceptable mesh density. If the "Artificial" strain energy associated with hourglass control is less than 1% relative to other typical energies then the mesh density is acceptable. From the table on Figure F.4 it is evident that Mesh#1 through Mesh#4 are acceptable based on energy criteria, but Mesh#5 and Mesh#6 are not. The artificial energy levels at the end of the static analysis step for the analysis of Meshes #5 and #6 were 1.1% and 3.5% of the total strain energy, indicating that Mesh#5 and Mesh#6 are too coarsely defined.

A response spectrum analysis was also completed for each of the six mesh definitions using the response spectra generated for input motions SHAKEA and SHAKEB. The results from these analyses were also used to determine the sensitivity of results to mesh density. The maximum principal stresses at all elements were requested as output from these analyses. The material properties used for the response spectrum analyses were an elastic modulus of 210 ksi, a material density of 140 pcf with modal damping at 10 %. A summary of the results from the response spectrum analyses completed for each of the six different mesh definitions is shown in Table 5.

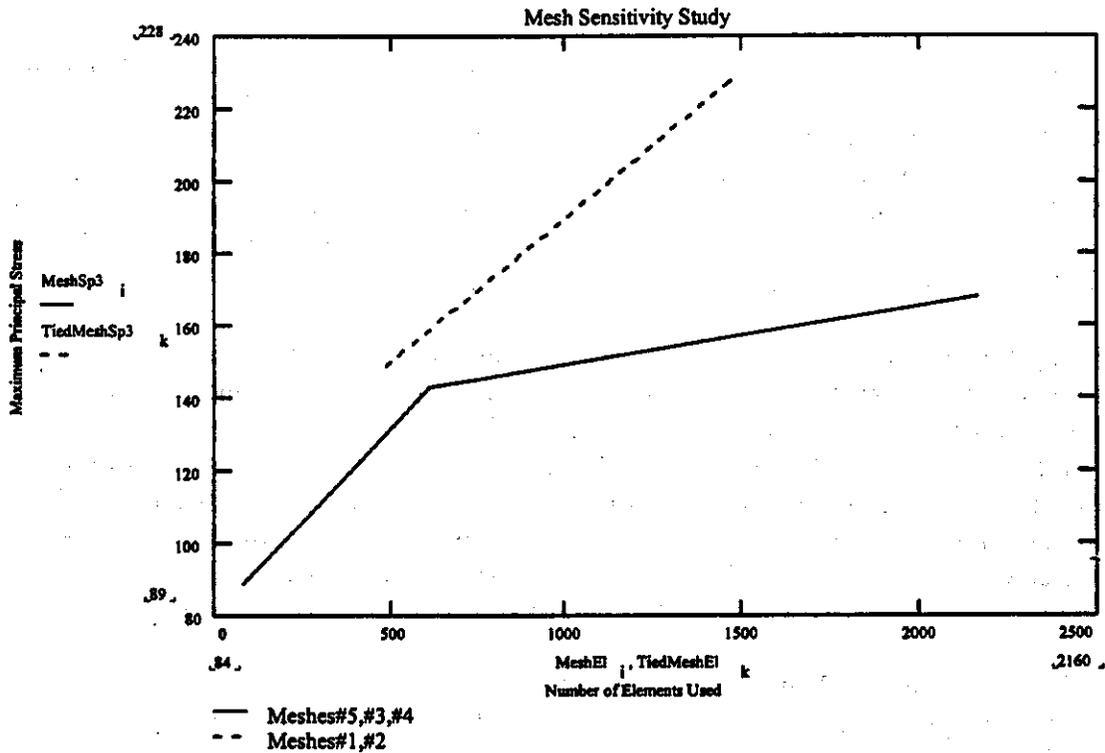
Table 5 : Maximum Principal Stresses from Response Spectrum Analyses						
Input : Response Spectrum from SHAKEA						
	Mesh#1	Mesh#2	Mesh#3	Mesh#4	Mesh#5	Mesh#6
SP3	23 psi	15 psi	14 psi	17 psi	9 psi	9 psi
@Elements	Numbers 1369, 1369	Numbers 120, 123	Numbers 282, 330	Numbers 1128, 1288	Numbers 27, 45	Numbers 74, 75
CPU Time	561 sec	109 sec	155 sec	454 sec	18 sec	53 sec
Input : Response Spectrum from SHAKEB						
SP3	228 psi	149 psi	143 psi	168 psi	89 psi	88 psi
@Elements	Numbers 1369, 1369	Numbers 120, 123	Numbers 282, 330	Numbers 1128, 1288	Numbers 27, 45	Numbers 74, 75
CPU Time	565 sec	109 sec	155 sec	456 sec	18 sec	53 sec

Figures F.5 and F.6 show the location of the elements at which the maximum principal tensile stresses occurred in response to the SHAKEA spectrum input for the six different mesh definitions. The plot of Mesh#1 indicates that the elements at which the maximum principal

stress occurred were located on the downstream face adjacent to, and directly above, the change in slope. These two elements are also adjacent to, and directly below, the upper tied contact surface. For the other five mesh definitions the elements at which the maximum principal tensile stress occurs are located adjacent to, and directly below, the change in slope on the downstream face of the model. Figures F.7 and F.8 show the maximum principal tensile stress contour plots from these response spectrum analyses. The contour plots of Mesh#1 and Mesh#2 both show a sudden jump in the stress levels at the tied contact surfaces. Mesh#1 produced the highest maximum principal tensile stress(23 psi), but these peak stresses appear to be associated with the change in mesh density occurring on the upper tied surface. In mesh#2 where the upper tied surface was moved farther away from the location of the change in slope on the downstream face the maximum principal stresses occurred at the change in slope and were reduced to 15 psi which seems much more reasonable. All of the contour plots indicate that the maximum principal tensile stress occurs on the downstream face near the change in slope, but stress results from the fine mesh definitions were significantly higher. The maximum principal stress from the analysis of Mesh#4 was 17 psi while the maximum principal stress resulting from the analysis of Mesh#5 was only 9 psi. Use of a coarser mesh definition resulted in a 47 percent under-estimate of the maximum principal stress, because the stress output location is farther away from the stress concentration at the change in slope.

Figures F.9 through F.12 show the locations of elements in which the maximum principal tensile stresses occur, and the maximum principal tensile stress contour plots from the response spectrum analyses using the spectrum from input motion SHAKED. These results are similar to the results obtained using input motion SHAKED. The maximum principal stress distributions are the same with increased magnitudes. Once again a significant increase in the maximum principal stress was seen in Mesh#1 where the tied surface was positioned near the change in slope on the downstream face. The maximum principal stress occurring in Mesh#1 was 228 psi, while the maximum principal stress occurring Mesh#2 was 149 psi.

The response spectrum results using the spectrum from SHAKED also show a 47 percent reduction in stress between Mesh#4 with a maximum principal stress of 168 psi and Mesh#5 with a maximum principal stress of 89 psi. The following plot shows the maximum principal stresses from the response spectrum analyses for spectrum SHAKED plotted against the number of elements in the mesh.



Results from Mesh#1 and Mesh#2 are plotted separately using the dashed curve since these mesh definitions include tied surfaces. Meshes #3,#4, and #5 are shown with a solid curve. The plot shows maximum principal stress values converging as the mesh density increases with the exception of the results from Mesh#1. The maximum principal stresses resulting from the analysis of Mesh#1 appear to be associated with the location of the tied surface and are therefore considered to be invalid. There was a considerably more gradual increase in maximum principal stress value between Mesh#3(612 elements) and Mesh#4(2160 elements) than between Mesh#5(84 elements) and Mesh#3, but there was also an 273 percent increase in CPU time between analyses using Mesh#3 and Mesh#4.

The results of the mesh sensitivity study indicate that the quantities calculated at nodes, such as accelerations and displacements, are not extremely sensitive to mesh definition, however the stress values calculated at the element integration points were sensitive to changes in mesh density, with substantial underestimation of stress resulting from the use of mesh definitions that are too coarse. Energy terms are also a useful tool in determination of acceptable mesh density. Mesh#3 was selected for use in the rest of the linear elastic sensitivity studies in this report since it provided a reasonable combination of degree of convergence of results, relatively short CPU time, and acceptable energy levels.

### **VI.3 Sensitivity of Results to Variations in Linear-Elastic Material Properties**

To determine the sensitivity of results to variations in material and damping parameters a series of modal dynamic analyses were performed. The resulting acceleration and displacement time histories were compared with laboratory measurements. In the first set of analyses only the elastic modulus was varied. Analyses using elastic moduli of 90, 113, 120, 130, 157, 200, 300, and 350, ksi were included. For this first set of analyses the modal damping option was used with the damping set at 3.5% of critical damping. The material density was 138.2 lb/ft<sup>3</sup>. The value 138.2 lb/ft<sup>3</sup> is the density of this material as determined in the laboratory.

Figure G.1 shows the natural frequencies obtained from this set of analyses. These analyses resulted in a fairly linear increase in the natural frequency with increased elastic modulus. The first natural frequencies varied from 12.1 Hz for a elastic modulus of 90 ksi to 23.9 Hz for an elastic modulus of 350 ksi. The second natural frequencies varied linearly from 23.2 Hz for a elastic modulus of 90 ksi to 45.74 Hz for an elastic modulus of 350 ksi. The first natural frequencies obtained using a material density of 138.2 pcf best match the laboratory test predictions when the elastic modulus used was approximately 200 ksi. This material property set resulted in a first natural frequency of 18 Hz and a second natural frequency of 35 Hz.

Figures G.2 and G.3 show tabulated and plotted peak acceleration and displacements for this series of analyses. Acceleration and displacement time history plots are shown in figures G.4 and G.5. The calculated accelerations and displacements approached the peak values measured in the laboratory experiment as the elastic modulus increases, with the best match occurring for an elastic modulus between 300 and 350 ksi. The elastic modulus which produced best overall match for natural frequencies, accelerations and displacements was between 200 and 300 ksi.

In the second set of analyses the input acceleration frequency was varied. Analyses using elastic moduli of 113, 157, 200, ksi were re-analyzed using input records with frequencies of 6, 10, 14, 18, 20, 22, 24, and 26 Hz. These input records were extracted from the SHAKEA input record. For this set of analyses the modal damping and material density were the same as in the first set of analyses. The Rayleigh damping was set so that the majority of the frequencies were damped at 3.5% of critical damping, and the material density was 138.2 lb/ft<sup>3</sup>. The natural frequencies obtained from this set of analyses were the same as those obtained from the first set of analyses, which are shown in figure G.1. The first natural frequencies best match the laboratory test predictions when the elastic modulus used was approximately 200 ksi.

Figures G.6 and G.7 show tabulated and plotted peak horizontal accelerations resulting from this series of analyses. Figure G.8 shows the tabulated and plotted peak vertical acceleration for this series of analyses. Figures G.9 and G.10 show the peak displacements. Acceleration and displacement time history plots are shown in figures G.11 through G.28.

The peak upstream-downstream accelerations generated by ABAQUS, for analyses using input frequencies of 14 Hz or greater, approached the peak values measured in the laboratory experiment as the elastic modulus was increased(  $E > 200$  ksi). The laboratory values tended to

be lower than the results produced by the analyses and the results produced by the analyses tended to decrease as the modulus was increased.

The peak vertical accelerations measured in the laboratory for input frequencies of 20 Hz or less tended to be significantly higher than the values produced by the analyses. The ABAQUS values for the vertical acceleration at the top of the model tend to increase as the modulus is decreased, therefore the analyses using lower moduli ( $E < 113$  ksi) best match the measured values. For input frequencies of 22 Hz or greater this trend is reversed with the higher moduli producing the best match with the laboratory measurements.

The peak upstream-downstream displacements measured in the laboratory tended to be lower than those calculated in the analyses. The ABAQUS values decreased as the modulus increased producing the best match for higher moduli ( $E > 200$  ksi).

The upstream-downstream acceleration time history plots showed that at low input frequencies (6 and 10 Hz) the results are less sensitive to the value of elastic modulus used. The acceleration results from ABAQUS matched the laboratory curves equally well over all three moduli. However, the results were sensitive to the modulus used in the analyses with input frequency of 14 Hz or greater. In the analyses using input acceleration of 14 Hz or greater the ABAQUS results consistently most closely matched the laboratory values when an elastic modulus of 200 ksi was used.

The vertical acceleration time history plots showed that the laboratory values were significantly higher than the ABAQUS values for input frequencies of 14, 18, and 20 Hz. These input frequencies bracket the natural frequency of the structure (18 Hz). It may be that the boundary conditions in the laboratory did allow for some vertical movement at the base of the model which was not accounted for in the analysis. When input frequencies of 22 and 24 Hz were used the ABAQUS analyses using an elastic modulus of 157 were the best match to the laboratory measurements, while the analyses using a 26 Hz input motion best matched the laboratory values when a modulus of 200 ksi were used.

The upstream-downstream displacement time history plots for input frequencies of 6, 10 and 14 Hz show the best match when the modulus is increased ( $E > 200$  ksi). When an 18 Hz input motion was used a 180 degree phase shift developed between the ABAQUS curves and the displacement time history curve from the laboratory measurements, although the amplitudes still matched best when a modulus of 200 ksi was used. Again this is an indication that the boundary conditions in the laboratory were not completely captured in the analyses. The plots of displacement time history records for input frequencies of 20 Hz and greater are back in phase with the best match in terms of amplitude resulting from the analyses using an elastic modulus of 200 ksi.

In the third set of analyses only the material density was varied. Analyses using a material density of 100, 138.2 and 200 lb/ft<sup>3</sup> were included. The amount of modal damping used was 3.5% of critical damping. The three densities were analyzed for each of the following elastic moduli : 113, 157, 200, 300 and 350 ksi.

The natural frequencies from these analyses are shown in figures G.29 to G.33. The first natural frequencies calculated using an elastic modulus equal to or less than 157 ksi approached 18 Hz when the material density was decreased, while the analyses using an elastic modulus greater than 157 ksi approached 18 Hz when the material density was increased. Interpolation of these results indicates that each of the following material property combinations would result in first natural frequencies of exactly 18.0 Hz :

Elastic Modulus	Material Density	First Natural Frequency	Second Natural Frequency
113 ksi	68 pcf	18.0 Hz	34.4 Hz
157 ksi	111 pcf	18.0 Hz	34.5 Hz
200 ksi	140 pcf	18.0 Hz	34.6 Hz
300 ksi	207 pcf	18.0 Hz	34.4 Hz
350 ksi	228 pcf	18.0 Hz	34.5 Hz

Plots of the mode shapes obtained from three of these analyzes are shown in Figures G.34 through G.36. These plots show that the first mode is a cantilever mode acting in the cross-canyon direction, while the second mode is a cantilever mode acting in the upstream-downstream direction.

Figures G.37 through G.46 show tabulated and plotted peak accelerations and displacements for the series of three analyses completed for each of five elastic moduli where the density was varied (100, 138.2, and 200 pcf). In each set of analyses the peak values from the analyses more closely approach the peak values measured in the laboratory when the material density was decreased. Figures G.47 to G.51 show acceleration time history plots. Each plot shows four acceleration time histories, one curve for each of the three densities analyzed for a given elastic modulus plus the acceleration time history measured in the laboratory. Each figure contains four such plots, one for each of the four horizontal accelerometers on the model. These plots show that the accelerations decrease with decreased material density independent of the elastic modulus, and that the accelerations decrease as the elastic modulus increases independent of material density.

The average value for the elastic modulus determined from the static compression tests was 157 ksi, while the average value for the elastic modulus resulting from rapid compression tests was 113 ksi. A decrease in dynamic modulus compared to the static modulus was unexpected. Typically the dynamic modulus is equal to or greater than the static modulus. The current practice at Reclamation for the static finite element analysis is to reduce the average elastic modulus determined from the static compression test by a factor of one third to account for long term creep ( $E_{static} = 105$  ksi), and to increase the average elastic modulus from the static

compression test by a factor of four-thirds for use in the dynamic finite element analyses ( $E_{\text{Dynamic}} = 209 \text{ ksi}$ ). Reclamation is currently performing rapid compression tests on all concrete core to develop a database of static and dynamic properties.

Dr. Jerome Raphael's paper "Tensile Strength of Concrete" published in the ACI Journal in 1984,[8] reported on tensile and compressive strength testing on concrete specimens which resulted in the conclusion that the rate of loading characteristic of an earthquake increases compressive strength an average of 31 percent and increases tensile strength an average of 56 percent.

The results of this sensitivity study show that any number of combinations of the two linear elastic material properties (elastic modulus and material density) could be used to obtain modal characteristics matching those produced in the free vibration test. It is recommended that the modulus be varied because the calculation of density using volume and weight measurements of a material specimen is very straight forward and are expected to be quite accurate. The measured density of 138.2 pcf is probably accurate within  $\pm 5 \text{ pcf}$ .

Selection of the dynamic elastic modulus is much less certain. Comparisons of natural frequencies resulting from the modal dynamic ABAQUS analyses and the resonant frequencies identified from the measured acceleration and displacement time histories suggest that the most appropriate elastic modulus would be approximately 200 ksi. Comparison of accelerations and displacements resulting from the modal dynamic analyses and the accelerations and displacements measured in the laboratory suggest that the most appropriate elastic modulus would be between 200 and 300 ksi. The value which would be selected based on current practice at the Bureau is 210 ksi. Therefore the results from the current study tend to support current practice of increasing the static modulus for use in dynamic analyses.

#### **VI.4 Variation in the Amount of Damping Included in Modal Dynamic Analyses**

In this set of analyses the modal direct damping option was used which allows the same damping for each mode. Only the percent of critical damping used was varied. Analyses were completed for the following material properties:

Linear Elastic Material Property set #1)  $E = 190 \text{ ksi}$  and  $\gamma = 133 \text{ pcf}$ ,

Linear Elastic Material Property set #2)  $E = 200 \text{ ksi}$  and  $\gamma = 140 \text{ pcf}$ ,

Linear Elastic Material Property set #3)  $E = 210 \text{ ksi}$  and  $\gamma = 140 \text{ pcf}$ ,

Linear Elastic Material Property set #4)  $E = 250 \text{ ksi}$  and  $\gamma = 140 \text{ pcf}$ .

The analyses for each material property were repeated for different percentages of critical damping to determine how much damping would influence the resulting acceleration and displacements and to determine how much damping would be required for the resulting acceleration and displacements to match those measured in the laboratory experiment. The

modal damping percentages used were 3.5%, 5%, 10%, 38%, and 88%. Peak values of acceleration and displacement, acceleration and displacement time histories, natural frequencies, and CPU times were compared.

The first three natural frequencies for each material property are shown on Figure H.1. The first natural frequencies for these material property sets are approximately 18 Hz, with the exception of material property set #4 which had a first natural frequency of 20 Hz. The material density for material property set #4 would have to be increased an unrealistic amount to maintain a first natural frequency of 18 Hz. Peak values of acceleration and displacement, as well as the CPU time required to complete each analysis, are shown in Figures H.2 through H.9. These results indicate that the percent damping used has relatively little affect on the accelerations and displacements. At least 88 percent of critical damping would be required for the peak values from these analyses to converge exactly with the values measured during the shake test. This was true for all four material property sets. Acceleration and displacement time history plots are shown on Figures H.10 through H.17. These results show that while it may require an unrealistic amount of damping to match the measured accelerations exactly, the curves generated from all of these analyses actually match the measured values fairly well for all levels of damping. It is also notable that a phase shift develops in the displacement time history curves at damping levels equal to or greater than 38 percent. The analyses using damping levels less than 38 percent are not as good a match with respect to the peak magnitudes, but they are a much better match in phase. The amount of damping did not have a significant effort of the CPU time required to run the analyses. CPU time only varied from 267 to 278 seconds.

#### **VI.5 Variation in Selection of Damping Method in Modal Dynamic Analyses**

In this set of analyses only the damping method was varied. Modal dynamic analyses were completed using three damping methods : direct, Rayleigh, and composite. Only the method of applying the damping was varied. For this set of analyses the elastic modulus was 210 ksi, and the material density was 138.2 lb/ft<sup>3</sup>. Accelerations, displacements and CPU times were compared.

The first damping method was "direct" modal damping. When the direct method is used the damping in each eigenmode is given as a fraction of the critical damping for that mode. The equation of motion for a one of the eigenmodes of the system is given as:

$$m\ddot{q} + c\dot{q} + kq = 0$$

Where m is the mass, c is a damping factor, k is the stiffness and q is the modal amplitude. The solution is of the form

$$q = A \exp \lambda t$$

Where A is a constant, and

$$\lambda = -\frac{c}{2m} \pm \sqrt{\frac{c^2}{4m^2} - \frac{k}{m}}$$

If the expression under the root sign is negative the solution will be oscillatory (under damped). Critical damping is defined as the damping value which makes the expression under the root sign equal to zero or

$$c_{cr} = 2\sqrt{mk}$$

When an acceleration load is removed from a critically damped system there will be no oscillation, the amplitude will decay very rapidly. For these analyses 10% of the critical damping level was applied to each of the first three modes, and only the first three modes were considered in the analysis. Since this damping method associates the damping with the eigenmodes of the system, this damping method can not be used in the nonlinear dynamic analysis procedures where the equations of motion of the system are integrated directly, and the natural frequencies of the system are constantly changing. [6][2]

The second damping method was "Rayleigh" damping. When the Rayleigh damping method is used the damping is defined using a damping matrix ([C]). This damping matrix is a linear combination of the mass and stiffness matrices:

$$[C] = \alpha[M] + \beta[K]$$

Where  $\alpha$  is the mass damping factor and  $\beta$  is the stiffness damping factor. In ABAQUS standard modal dynamic analysis procedures Rayleigh damping is converted into critical damping fractions for each mode. The  $\alpha$  and  $\beta$  damping factors are defined independently for each mode included in the analysis. For each mode, the fraction of critical damping is given as :

$$\xi_i = \frac{\alpha_i}{2\omega_i} + \frac{\beta_i \omega_i}{2}$$

For this analysis the equation above was entered in a MathCadd spreadsheet and then  $\alpha$  and  $\beta$  factors were selected such that 10 percent critical damping was used for the first three modes as follows:

$\alpha_i :=$	$\beta_i :=$	$\omega_i :=$	$\xi_i$
3.4	.0008	18.4	0.1
6.4	.0005	35.2	0.1
9.5	.0008	63.6	0.1

The third modal damping method was “composite” damping. When composite damping is used a damping value can be defined for each material in the model. The amount of dampening is entered as a fraction of critical damping. These values are then converted into a weighted average for each eigenmode. In this analysis there is only one material property set used for the entire model, so only one damping value was used: 10 percent of critical. The first three modes were included in the analysis. When this method is used the damping ratio is defined as:

$$\xi_{\alpha} = \frac{1}{m_{\alpha}} \Phi_{\alpha}^M \xi_m M_m^{MN} \Phi_{\alpha}^N$$

Where  $\xi_{\alpha}$  is the critical damping ratio used in mode  $\alpha$ ;  $\xi_m$  is the critical damping fraction defined for material  $m$ ;  $M_m^{MN}$  is the mass matrix associated with material  $m$ ;  $\phi_{\alpha}^M$  is the eigenvector of the  $\alpha$  th mode; and  $m_{\alpha}$  is the generalized mass associated with the  $\alpha$  th mode. This equation is summed over all the materials for each mode. In this study the model has only one material, so the equation reduces to defining the critical damping ratio for each mode as in the direct damping method. In this case a 10 percent damping ration was used for the first three modes and only three modes were included in the analysis.[6]

Figures H.18 and H.19 show the peak accelerations and displacements from these analyses, while Figures H.20 and H.21 show the acceleration and displacement time histories. The accelerations and displacements resulting from the analyses using modal and composite damping were identical as they should be since there is since the model includes only one material. The results from the analysis using Rayleigh damping were also nearly identical. The CPU times were also nearly the same for all three analyses. These results simply verify that all three modal damping methods will produce the same results when the same amount of damping is specified, as they should.

## VI.6 Sensitivity of Results to Variation Analysis Time Increment

Two sensitivity studies were completed to determine the effect of analysis parameters controlling the analysis time step in direct-integration dynamic analysis procedures. When the modal dynamic analysis method was used the selection of the appropriate time step was very straightforward. The time increment used in the dynamic procedure was selected to match the time increment of the seismic input record. Input accelerations were assumed to vary linearly between these values. There are two methods of controlling the analysis time increment available when the implicit direct-integration dynamic analysis procedure is used.

The first method is direct user control of increment size, in this case the increment is entered in the input file and can not change during the analysis. This method is not

recommended because when the direct time incrementation parameter is used the time increment can not be reduced to obtain a converged solution. In this case, if convergence is not achieved within the maximum number of iterations allowed in the program the analysis stops. It would be particularly difficult to select a constant time increment for a nonlinear dynamic analysis. The first sensitivity study involving the analysis time increment was completed to determine the effect of varying the analysis time increment using the direct time increment parameter. Three linear-elastic direct integration dynamic analysis were completed using analysis time increments of .0001, .003, and .01 seconds. One second of the input record SHAKEA, from 279 to 280 seconds, was used as input accelerations for these analyses. The material properties used in these analyses were an elastic modulus of 210 ksi and a material density of 140 pcf. Rayleigh material damping was used in these analyses, with  $\alpha = 8.936$  and  $\beta = .000132$ (10% of critical). Accelerations and displacements were compared.

Figures I.1 and I.2 show the peak acceleration and displacement values for the three analyses in which the time increment was varied, while Figures I.3 and I.4 show the acceleration and displacement time histories. The results show that the accelerations and displacements calculated in the ABAQUS analyses do more closely match the measured values as the time increment decreases, but the values shown for the CPU time required to complete the analyses showed a marked increase in computation time as the time increment was reduced. When a .01 second time increment was used the required CPU time was 557 seconds( $\approx 10$  minutes). This is more CPU time that was required in any of the modal dynamic analyses, but is still not an unreasonable time period. When the time increment was decreased to .003 seconds the CPU time increased to 1441 seconds( $\approx 24$  minutes). When the time increment was further decreased to .0001 sec the CPU time was 39564 seconds( $\approx 11$  hours).

The CPU times reported here are the time used when the workstations CPU was actually working on this job. The workstation used for this study was far from a single user machine. When several jobs are running on the system at the same time the CPU cycles through them; they share the processing time. As a result during the course of this study processes reporting CPU times of  $\approx 557$  seconds actually took  $\approx 24$  hours to complete, and jobs requiring 11 hours of CPU time actually took 4 or 5 days to complete. Therefore considering the amount of improvement in the results and the additional time required when the analysis time increment was decreased, a time increment of .01 seconds was considered satisfactory for this analysis.

The second method of controlling the analysis time increment is to use the "Haftol" parameter for the automatic time incrementation scheme. The Haftol parameter is set equal to the half-step residual tolerance. The Haftol parameter has dimension of force and can be chosen by comparison with typical actual force values, such as applied forces or expected reaction forces. The ABAQUS program manual offers the following guidelines : " For problems where considerable plasticity or other dissipation is expected to damp out the high frequency response, choose Haftol as 10 to 100 times typical actual force values for moderate accuracy and low cost; choose Haftol as 1 to 10 times typical actual force values for higher accuracy. For elastic cases with little damping Haftol values should be smaller than recommended above. Choose Haftol as 1 to 10 times typical actual force values for moderate accuracy; choose Haftol as 0.1 to 1 times actual force values for higher accuracy." [5][6] In dynamic analyses the typical(average) force

applied to the structure is not always obvious. In the case of the Koyna laboratory model study a value for the applied force could be approximated as the mass of the model(17.16 slugs) times the peak acceleration of input record SHAKEA(38.64 in/s<sup>2</sup>), which results in a value of 663 pounds force. Therefore the use of a Haftol parameter equal to 60 to 600 should produce accurate results for the linear elastic analyses. When the Haftol parameter is selected the program uses an automatic time incrementation method. In this case the program monitors the equilibrium residual error(out-of-balance forces) halfway through each time increment and adjusts the time increment accordingly. So if the "half-step residual" is small, it indicates that the accuracy of the solution is high and the time step is automatically increased. If the half-step residual is large, then the time step used in the solution is automatically reduced.

In this study the Koyna model, using Mesh#3 with an elastic modulus of 210 ksi and a material density of 140 pcf, was analyzed using three different values for the Haftol parameter: 5, 50, and 500. Accelerations, Displacements and CPU times were compared. Figures I.5 and I.6 show the peak acceleration and displacement values resulting from these analyses. Figures I.7 and I.8 show the acceleration and displacement time histories. Again the resulting peak accelerations and displacements more closely approach the measured values as the Haftol parameter is reduced, but the CPU time was also greatly increased. The CPU time required when the analysis was completed using a Haftol parameter of 500 was 785 seconds(≈13 hours), while the CPU time required when the analysis was completed using a Haftol parameter of 5 was 3179 seconds(≈53 hours).

## VI.7 Comparison of Modal, Implicit and Explicit Dynamic Analyses Procedures

In the ABAQUS finite element program there are several procedures available for performing dynamic analyses, three of which are the modal, implicit and explicit dynamic analysis procedures. The modal dynamic procedure calculates dynamic time history response for linear problems using the principals of modal superposition. A frequency extraction must be performed prior to performing the modal dynamic analysis since the structures's response is based on the natural modes of the system. As long as the system is linear and is represented correctly by the modes being used the method is very accurate and is usually less expense than the direct integration methods. The implicit dynamic analysis procedure(available in ABAQUS/Standard) and the explicit dynamic analysis procedure(available in ABAQUS/Explicit) differ in the choice of operator used to integrate the equations of motion. The implicit procedure uses the Hilber-Hughes-Taylor operator, which must be inverted and a set of simultaneous linear(or non-linear) dynamic equilibrium equations must be solved at each time increment. This is done iteratively using Newton's method. This can be computationally expensive, but it has an advantage in that the Hilber-Hughes-Taylor operator is unconditionally stable for linear systems so there is no upper limit on the time increment size. In the implicit procedure the dynamic qualities solved at time  $(t + \Delta t)$  are based both on their values at  $t$  and on their values at  $(t + \Delta t)$ . On the other hand, the explicit dynamic analysis procedure obtains the values for dynamic quantities at  $(t + \Delta t)$  based entirely on available values at time  $t$ . Displacement and velocities are calculated in terms of quantities that are known at the beginning of an increment, the global mass and stiffness matrices need not be formed and inverted as in the

implicit integration scheme, therefore the explicit procedure tends to be less expensive. The explicit method uses a central difference operator for integration of the equations of motion. The central difference operator is only conditionally stable, the stability limit being approximately equal to the time required for an elastic wave to cross the smallest element dimension in the model.[5][4]

In this study the Koyna monolithic model was analyzed using each of these three methods. One second of the SHAKEA input record(279 to 280 seconds) was used for the dynamic loading. The elastic modulus was 210 ksi and the density was 140 pcf. The resulting accelerations, displacements and required CPU times were compared. Figures J.1 and J.2 show the peak accelerations and displacements. Figures J.3 and J.4 show the acceleration and displacement time histories. The peak accelerations and displacements were very similar from all three analyses. The CPU times required for the Modal and Explicit analyses were similar, 264 seconds and 203 seconds respectively, while the required CPU time for the Implicit analysis was much longer(3179 seconds).

## VII. NON-LINEAR ANALYSES

A thorough investigation of the concrete non-linear material properties is beyond the scope of this report. The following non-linear mesh sensitivity study is presented here only for comparison with the linear elastic mesh sensitivity study. There were two issues evaluated in this study. The first was to determine to what extent tied contact surfaces, used to change mesh density, influence results in a non-linear concrete cracking analysis. The second was to determine the sensitivity of cracking predictions to variation in mesh density where no contact surfaces were used.

The ABAQUS/Explicit dynamic analysis procedure was used for this study. Four different meshes were used to analyze the uncracked Koyna model. The first meshes used tied contact surfaces to change the mesh density near the area where cracking was expected to occur(Mesh#1 and Mesh#2), while the third and fourth meshes(Mesh#3 and Mesh#5) used no contact surfaces. The same material properties, boundary conditions and loads were used for these three analysis. Each model was analyzed to the point at which complete failure of the structure occurred. Cracking patterns, times at which failure was predicted were compared to laboratory observations of the test in which the monolithic (uncracked) Koyna model was shaken to failure.

A static gravity load was applied in the first second followed by a 280 second dynamic loading. The 14 Hz sinusoidal input motion, which was used to shake the laboratory model to failure (Record SHAKEB), was used for these comparisons. The input acceleration was applied in the upstream-downstream direction only. The entire laboratory test input record is 480 seconds long. For this comparison only the last half of the record was used(from 200 to 480 seconds). The amplitude of the input motion is 1.2 g at 200 sec and increases in steps of 0.2 g approximately every 25 seconds.

Cracking patterns, time of crack initiation, and time of model failure are shown in figures K.1 through K.4 for each of the four mesh definitions. Mesh#1 resulted in crack initiation at 206 sec, which is very early in the input record considering that the laboratory model cracked and then reached failure at around 480 sec. Figure K.1 also shows that the cracks developed along the tied contact surfaces. The analysis of Mesh#1 reached a complete failure at 212 sec. Mesh#2 resulted in crack initiation at 222 seconds, which was also premature. Figure K.2 shows that the crack pattern developed along the tied contact surfaces even when the tied surface was moved farther away from the change in slope on the downstream face. The analysis of Mesh#2 reached completed failure at 235 seconds. Mesh#3 resulted in crack initiation at 401 seconds, which seems much more reasonable. Cracking developed first on the downstream face at the change in slope, then proceeded through the model in the upstream-downstream direction curving downward slightly until the upstream face was reached at 402 seconds and failure was indicated. This cracking pattern is very reasonable and compares well to laboratory observations. Figure C.8 shows the cracking pattern which resulted from the laboratory test.

The results of this study indicate that tied surfaces should not be used for any non-linear cracking analysis of concrete structures. Stress concentrations appear to develop along the tied surfaces causing cracks to develop which would not occur in a model without tied surfaces under the same loading conditions. The two mesh definitions without tied surfaces produced very similar results in terms of both the time of crack initiation and crack orientation. These results suggest that a fairly coarse mesh can be used to analyze non-linear concrete cracking in the ABAQUS/Explicit program.

## VII CONCLUSIONS AND RECOMMENDATIONS

1) The linear elastic material properties of the monolithic Koyna model were successfully calibrated primarily through comparisons of natural frequencies, as calculated in the ABAQUS finite element code, and the resonant frequencies identified from the measured acceleration time history records, and secondarily, through direct comparisons of calculated and measured accelerations and displacements. The most appropriate linear elastic material property set consisted of a dynamic modulus equal to 210 ksi with a material density equal to 140 pcf. The results of this study confirmed that it is very important that the most appropriate value for the dynamic modulus be identified for use in analyzing dams under seismic loading, since the dynamic modulus greatly influences the results. The reason for the decrease in modulus observed in the rapid compression test values still needs to be understood. Whenever forced vibration tests at a dam are available their results should be used to calibrate/verify the value concrete modulus used for the dynamic analysis regardless of whether linear elastic or non-linear analysis methods will be used.

2) The analysts choice of mesh definition also has a significant effect on results. The use of tied contact surfaces to vary mesh density in localized regions is not recommended for either linear elastic or nonlinear cracking analyses. Stress concentrations tend to develop along the tied contact surfaces. It may be possible to effectively use tied contact surfaces for linear elastic analyses providing that they are positioned relatively far away from areas of interest, but they should not be used in non-linear analyses where cracking is important. Variables calculated at element integration points, such as stresses and strains, are sensitive to mesh density regardless of whether or not tied surfaces are included in the mesh design. Stress levels may be significantly underestimated if too coarse of a mesh definition is selected. Mesh density studies can be used to determine the minimum required density for convergence of results, but the time involved in conducting such studies is often a limiting factor. Therefore the energy terms are a particularly useful tool for determination of acceptable mesh density.

3) Selection of an appropriate analysis time increment size is also critical to obtaining reliable results in a reasonable time frame. It is recommended that the Haftol parameter be used to allow the program to automatically select the analysis time increment, except when the modal dynamic procedure is used in which case the time increment of the input record should be used as the analysis increment. Sensitivity studies may still be required to determine the appropriate force tolerance value for a given analysis even when the automatic time increment option is used, but these could be completed using a very short time period selected from the input record.

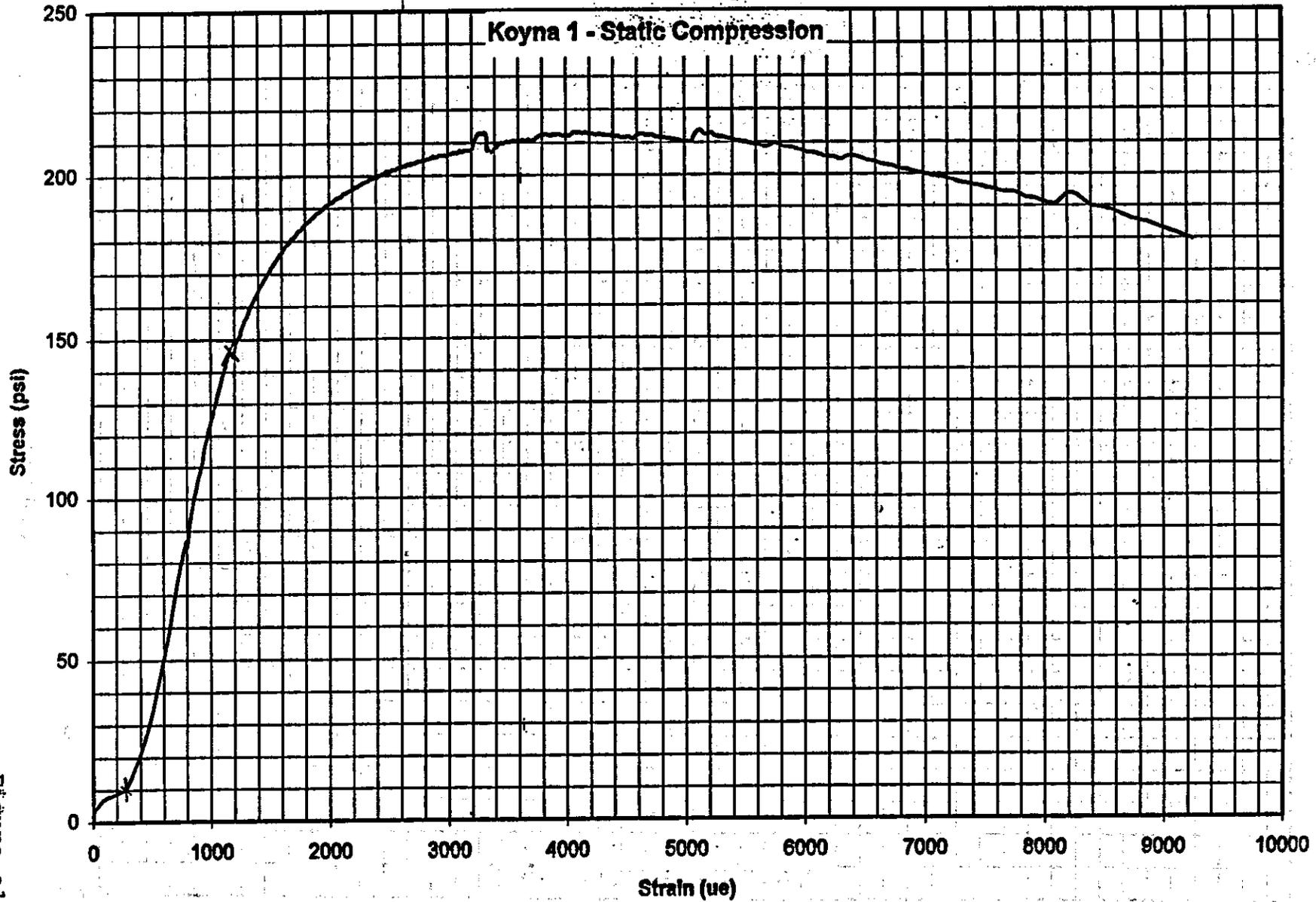
4) The ultimate goal of the shaking table test program is to develop a correlation between the material testing program and the material property requirements of the non-linear numerical concrete cracking model used in the ABAQUS finite element code. In the current phase of the project the linear elastic material properties were successfully calibrated and the effects of various mesh configurations and analysis parameters were investigated. In future work, development of the nonlinear material properties required needs to be completed.

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- 4 Kincaid, David, Numerical Analysis, Mathematics of Scientific Computing, The University of Texas at Austin, Brooks/Cole Publishing Company, 1991.
- 5 Hibbitt, Karlsson and Sorensen, Inc, ABAQUS/Explicit User's Manual, Version 5.7, Pawtucket, RI
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- 9 Harris, David; Snorteland, Nathan and Dolen, Timothy, "Shakeing Table 2-D Models of Concrete Gravity Dam for Computer Code Validation", U.S. Bureau of Reclamation, Materials Engineering and Research Laboratory, Denver, Co.

**Appendix A**  
**Laboratory Material Property Test Results**

Figure a1



Strain (ue)  
 $\frac{147 - 10}{1150 - 275} = .16 \times 10^{-6}$

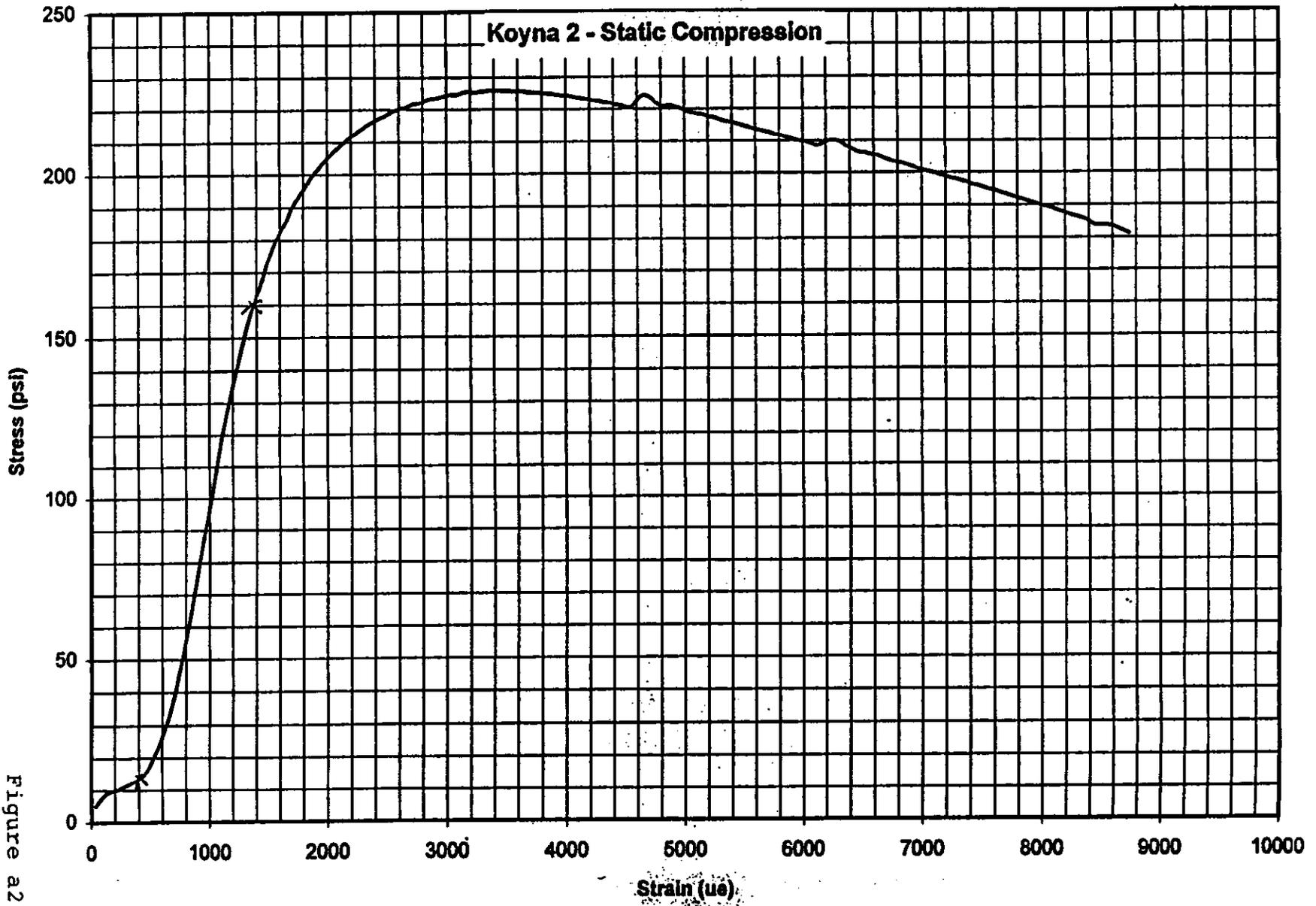
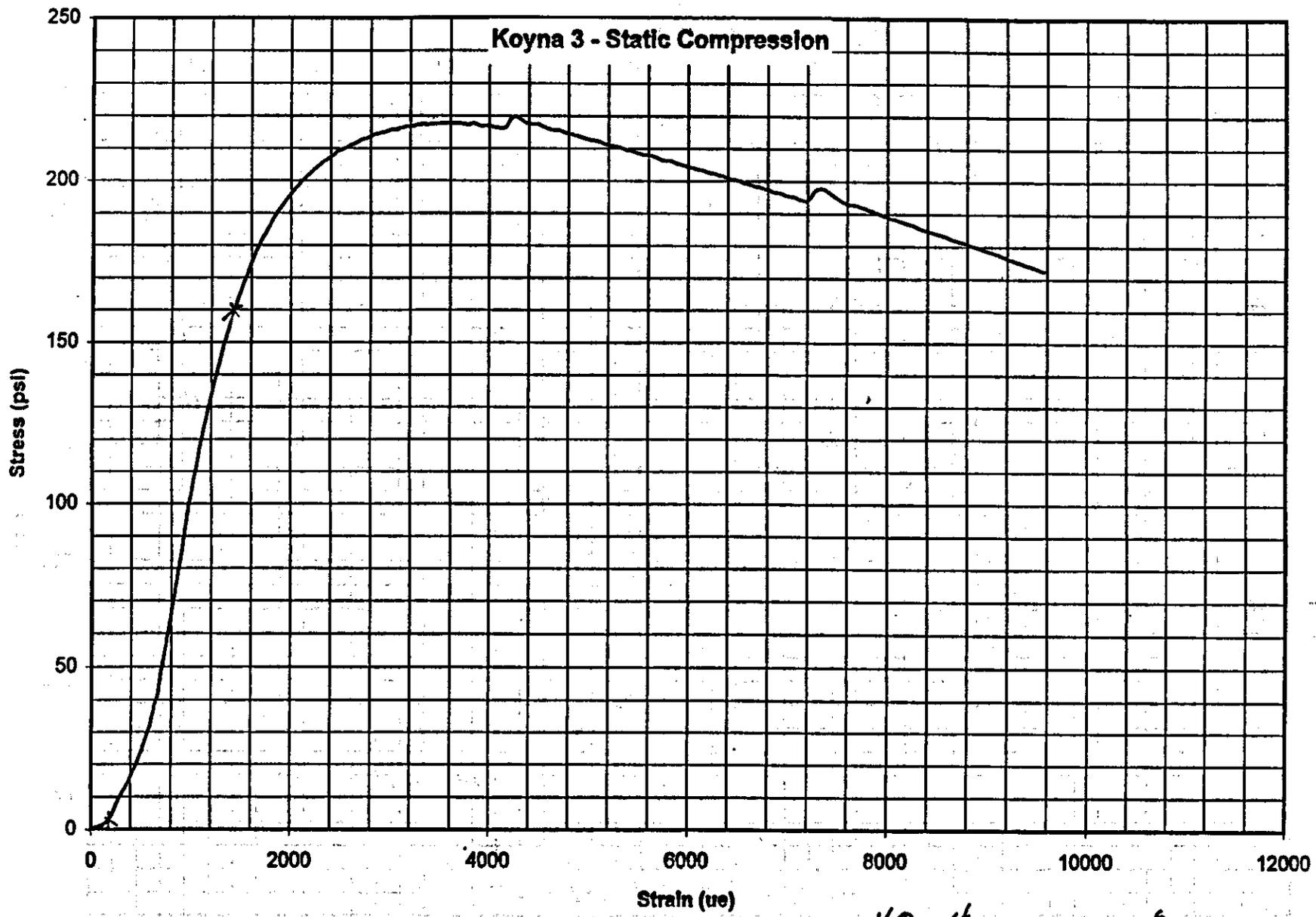


Figure a2

$$\frac{160 - 14}{1350 - 400} = .15$$

Figure a3



$$\frac{160 - 4}{1350 - 175} = .13 \times 10^6$$

\*

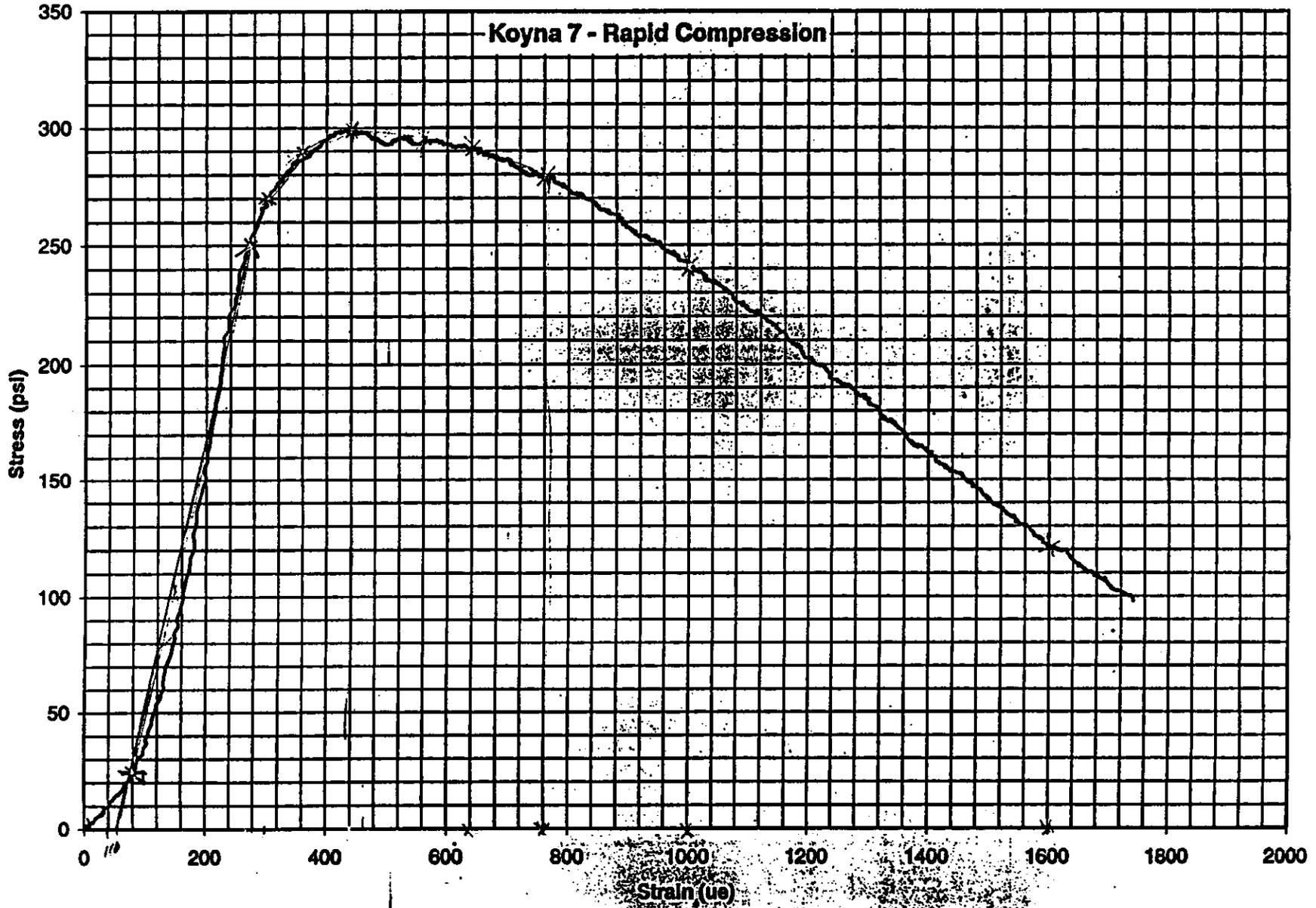
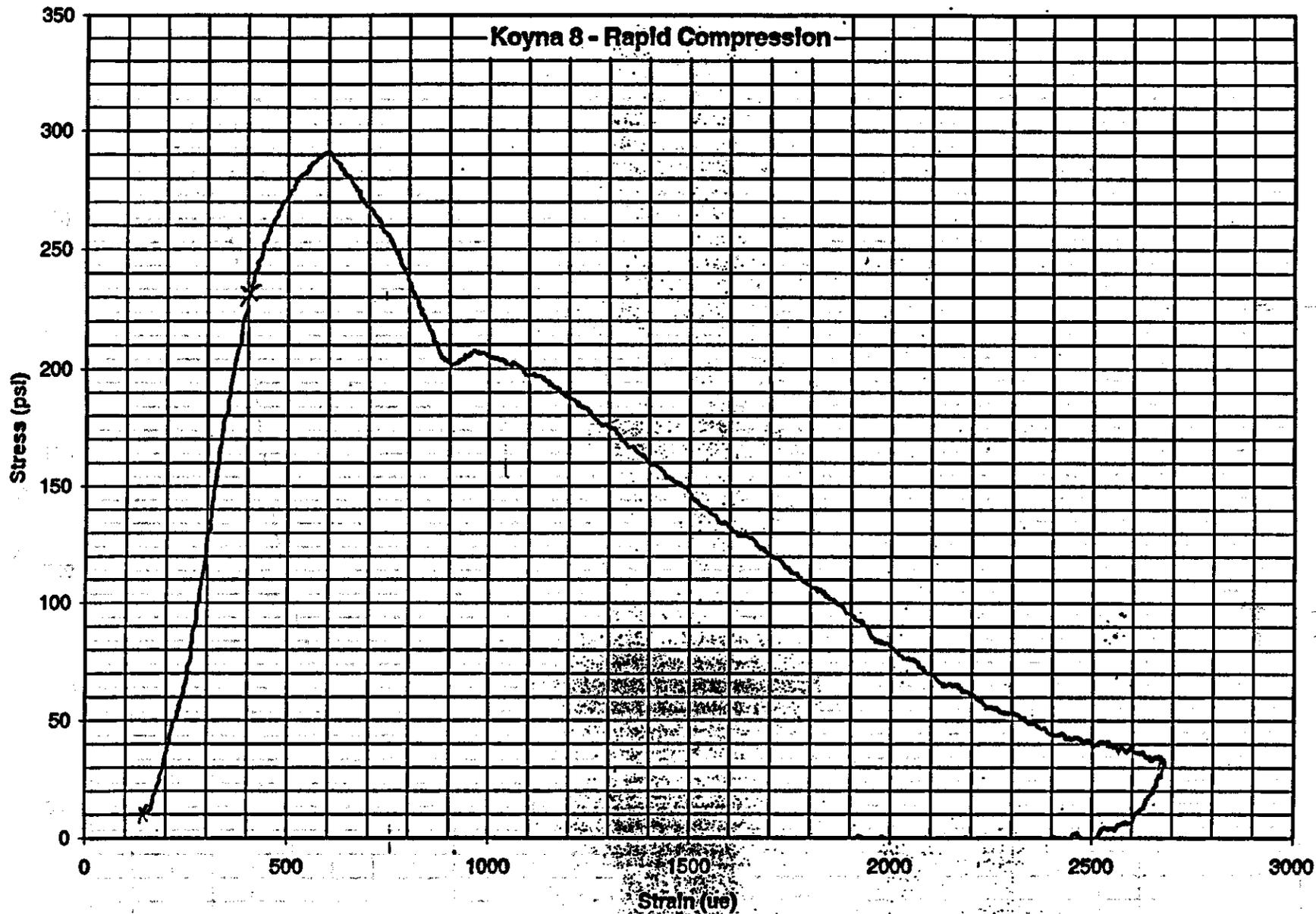


Figure a4

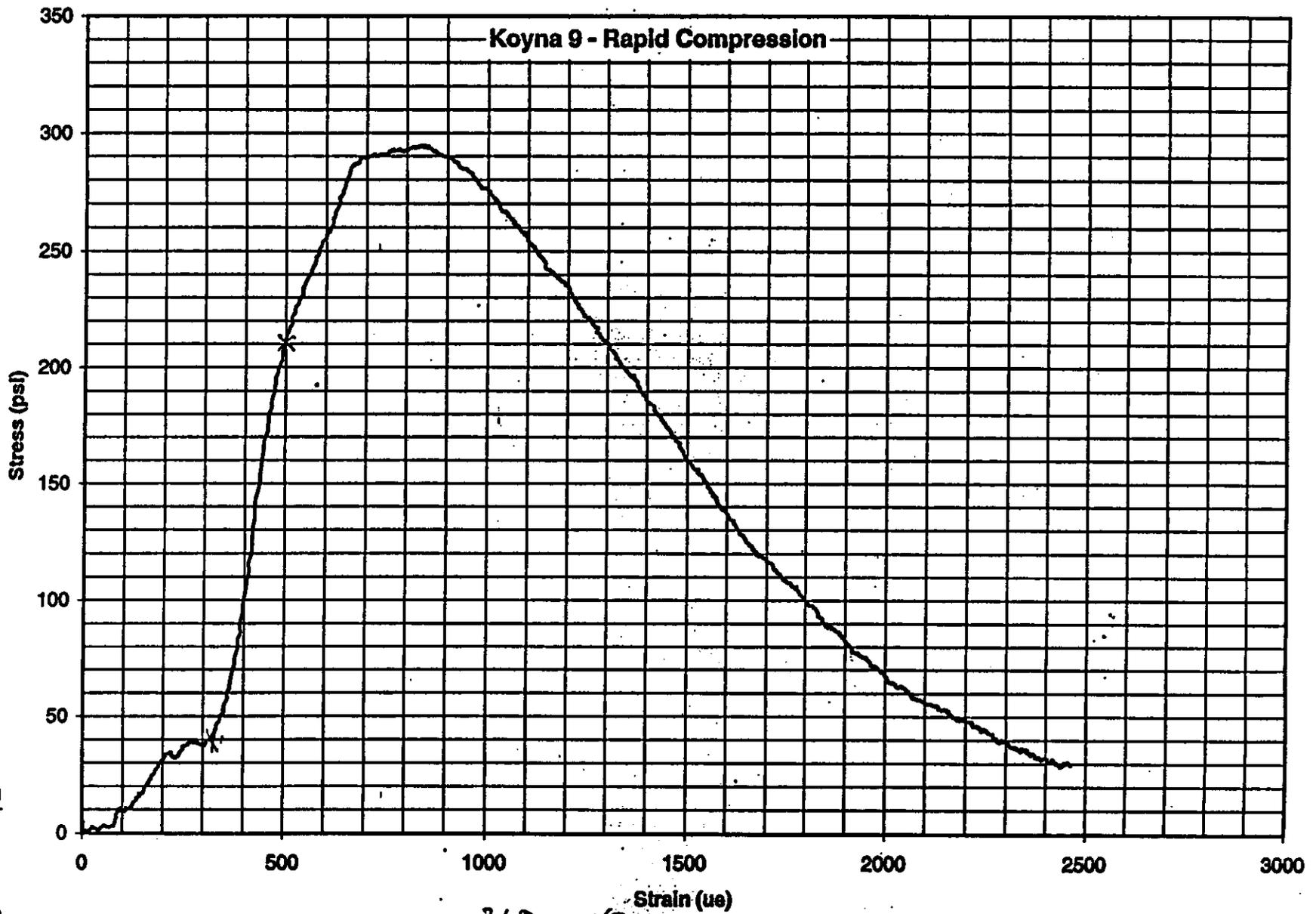
$$\frac{250 - 25}{270 - 80} = .012 \times 10^6$$

Figure a5



$$\frac{410 - 140}{230 - 10} = .012 \times 10^6$$

Figure a6.



$$\frac{210 - 40}{500 - 325} = .97 \times 10^{-6}$$

2

Koyna Dam  
Cyclic Compression Test  
Koyna8

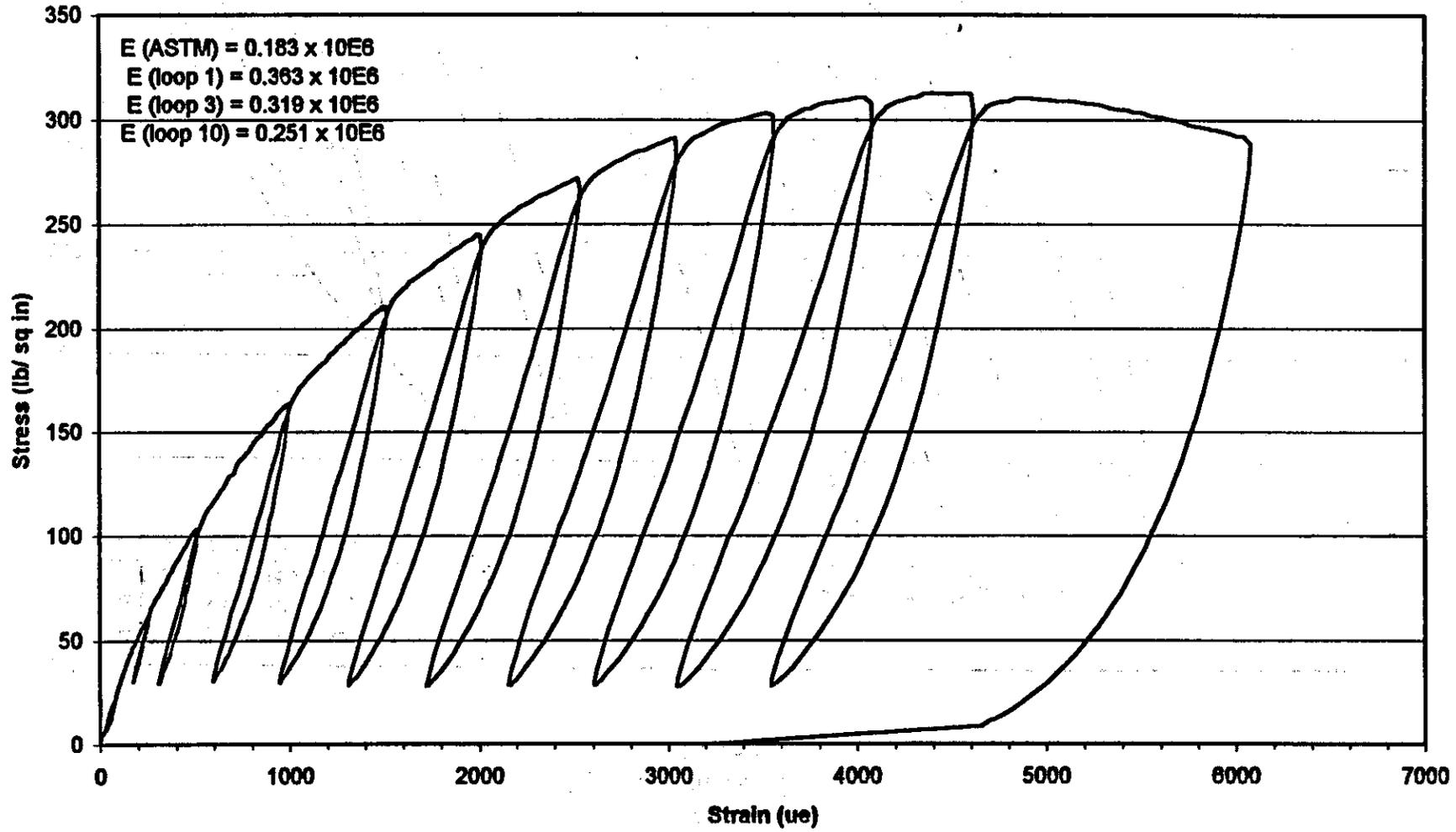


Figure a7

Koyna Dam  
Cyclic Compression Test  
Koyna9

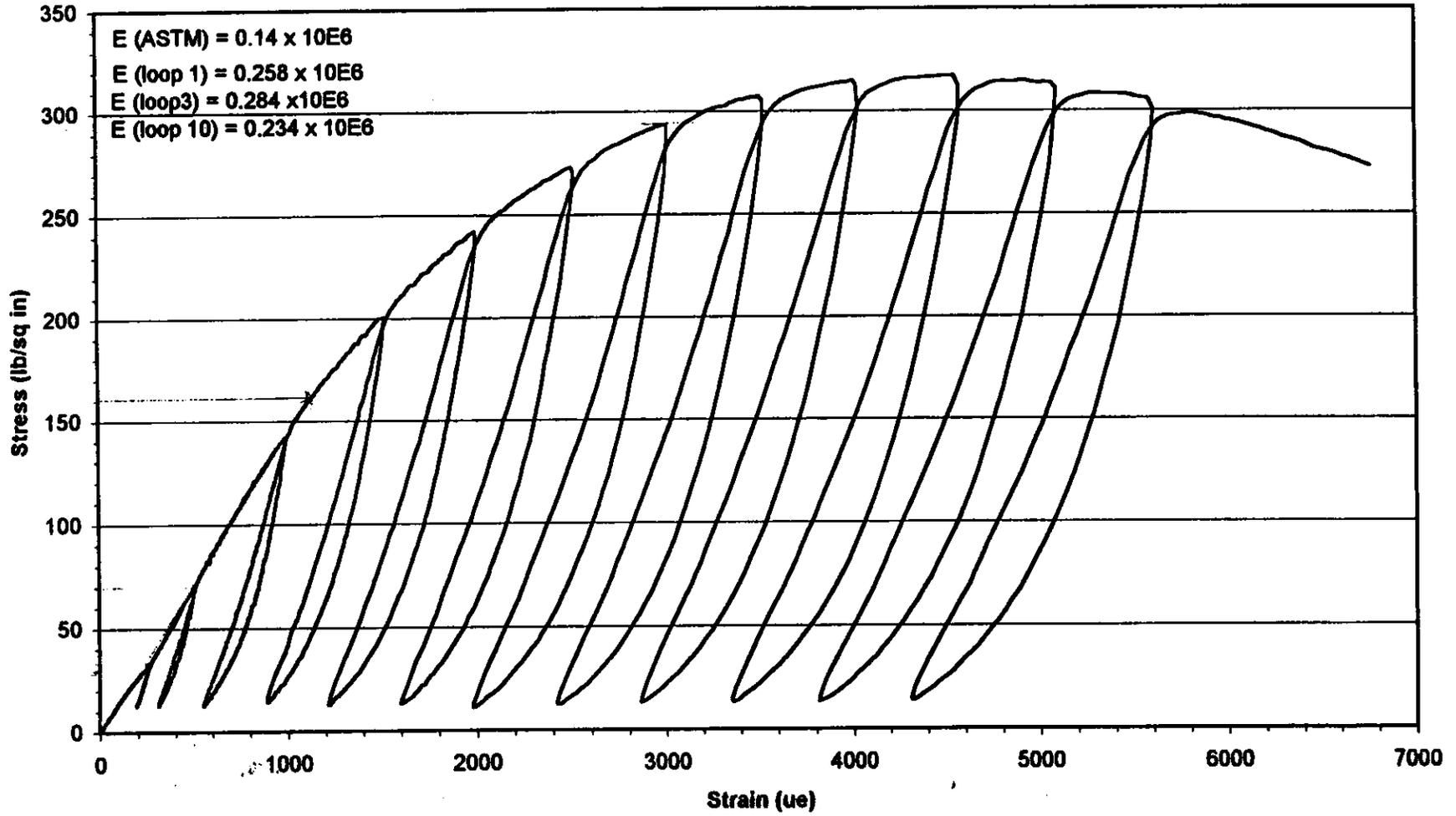


Figure a8

Load vs. Crack Width

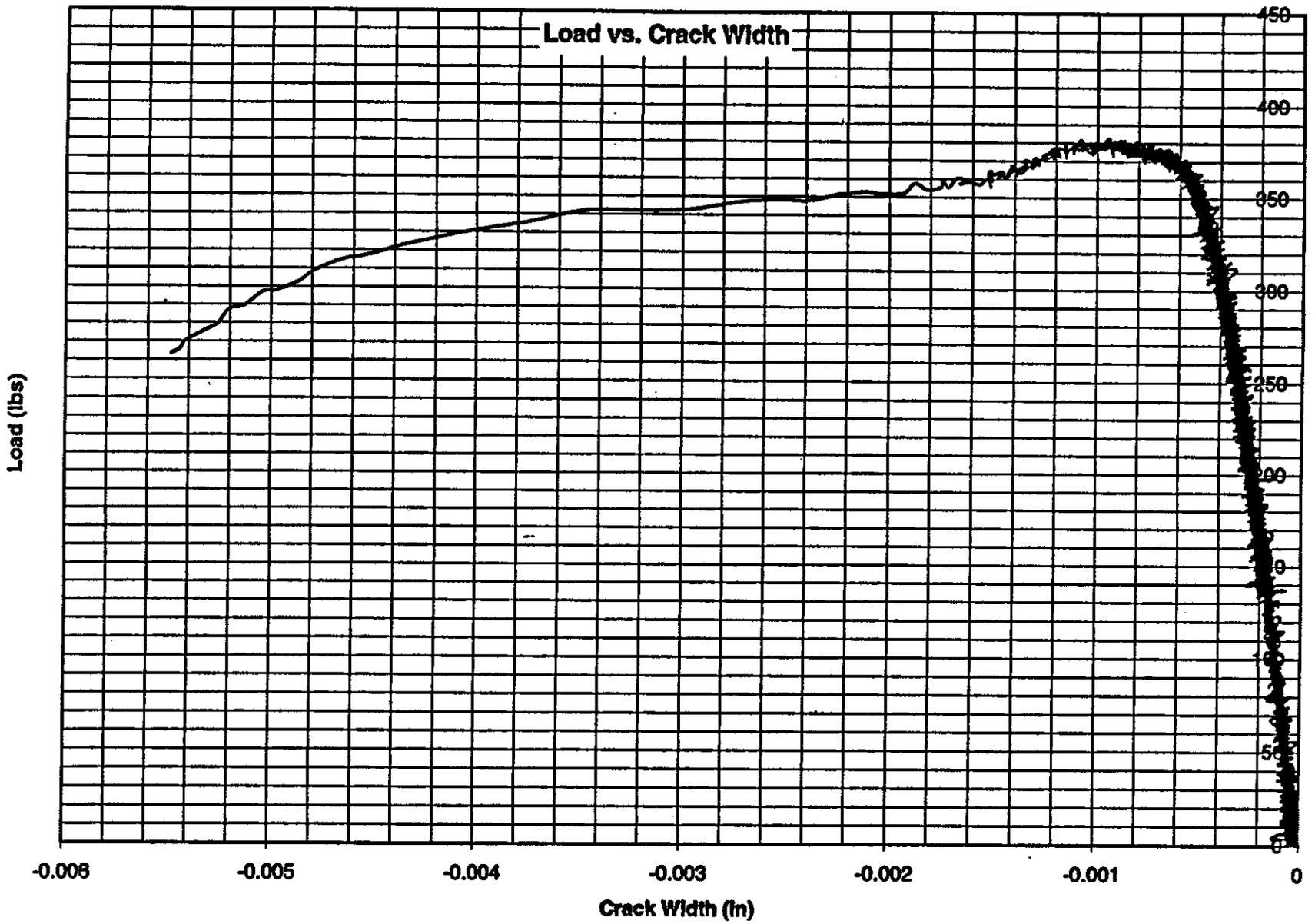


Figure a9

## **Appendix B -Laboratory Test Set-Up**

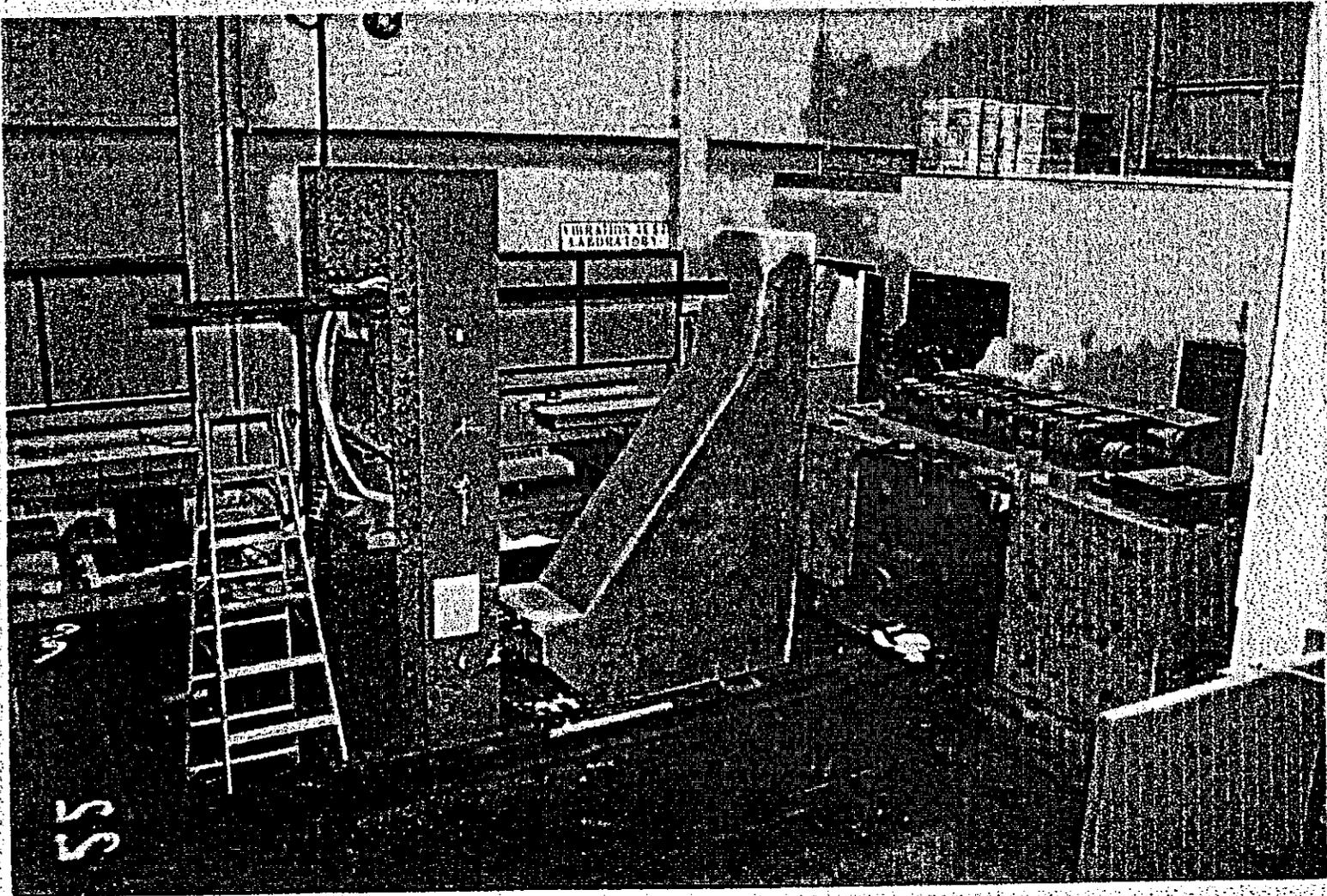


Figure b1

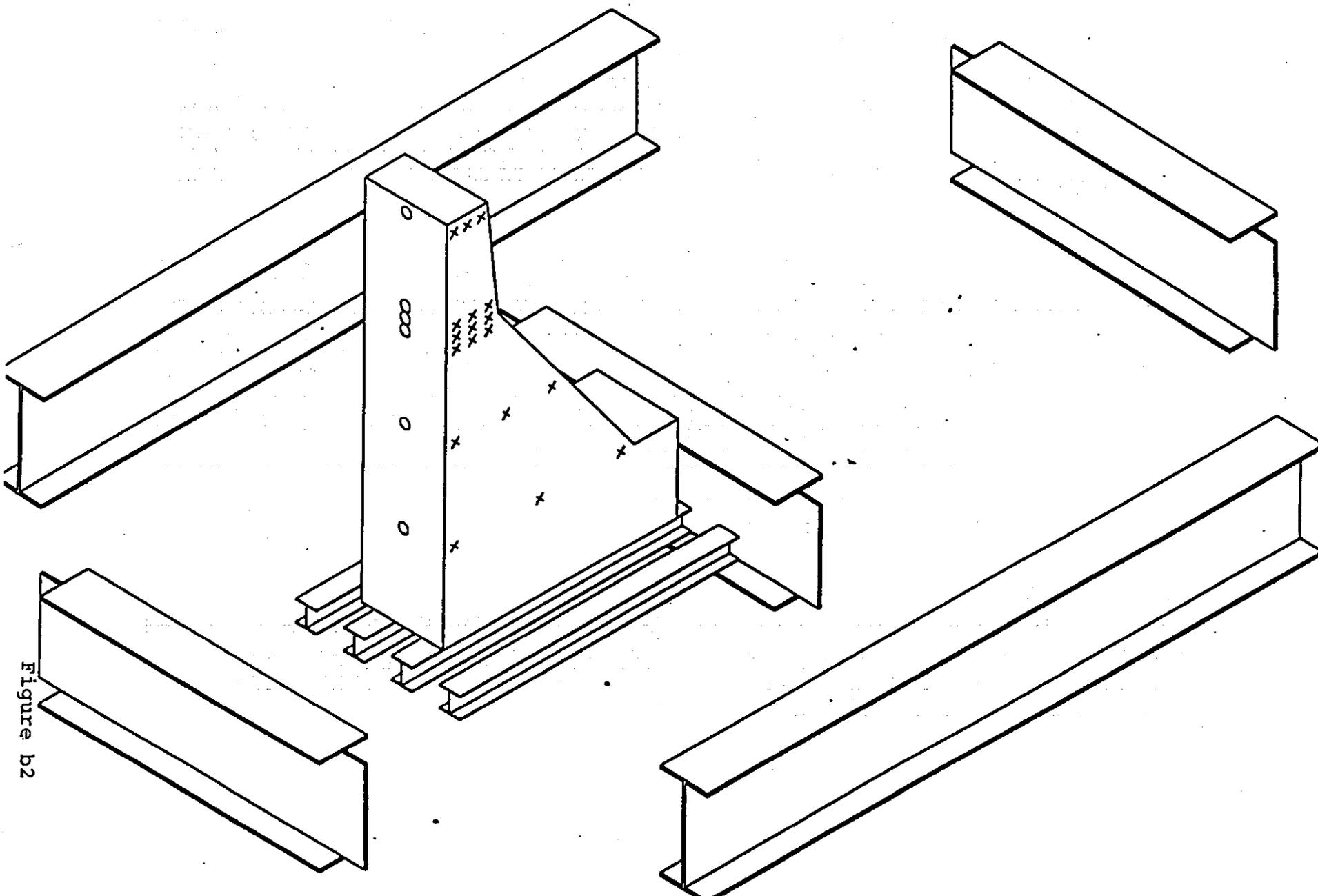


Figure b2

# Koyna "Uncracked" Laboratory Model Geometry

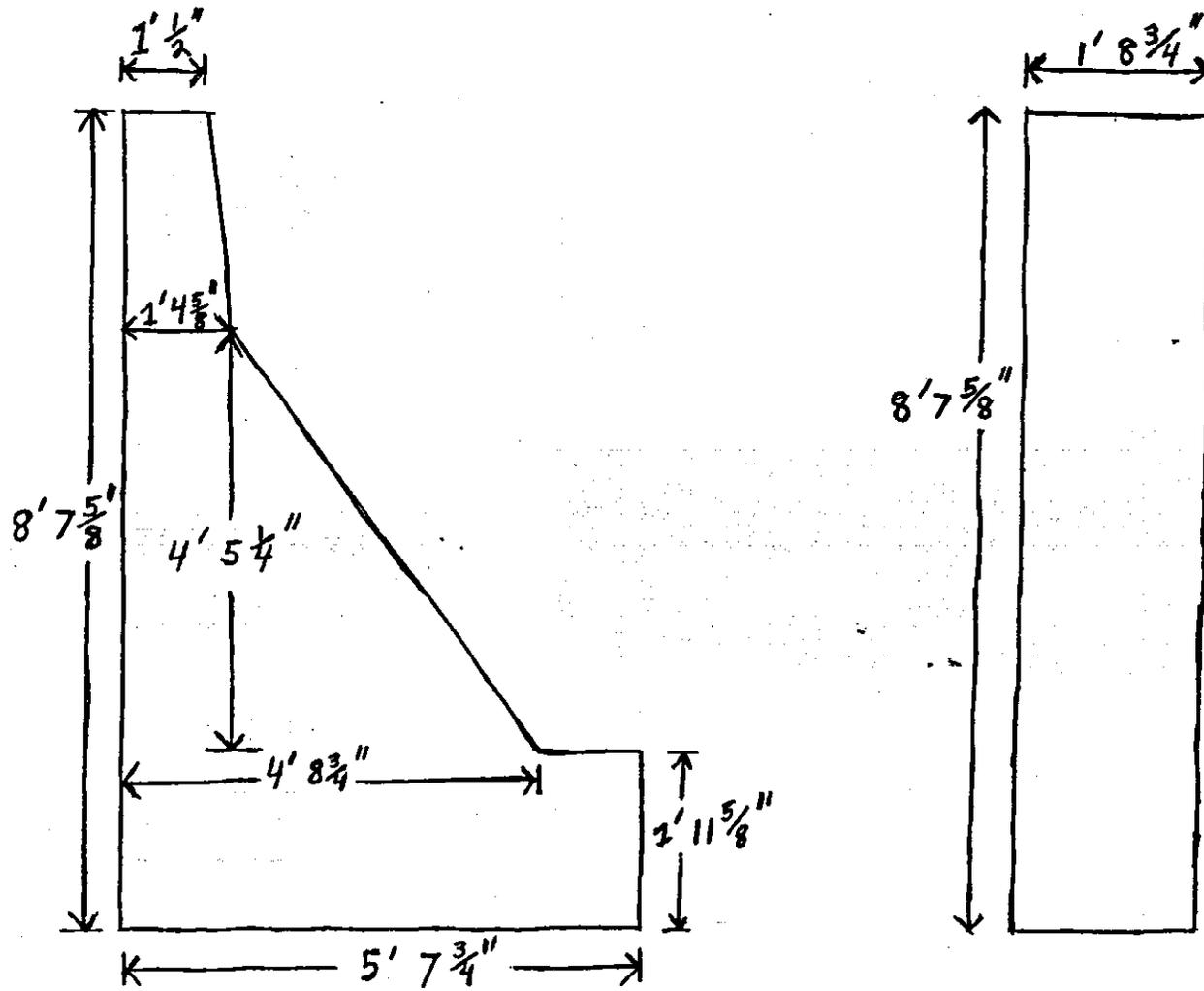


Figure b3

# ABAQUS

— ACCIN

Input Motion

SHAKEA

(inch/sec<sup>2</sup>)

XMIN .000E+00  
XMAX 4.862E+02  
YMIN -1.382E+02  
YMAX 1.253E+02

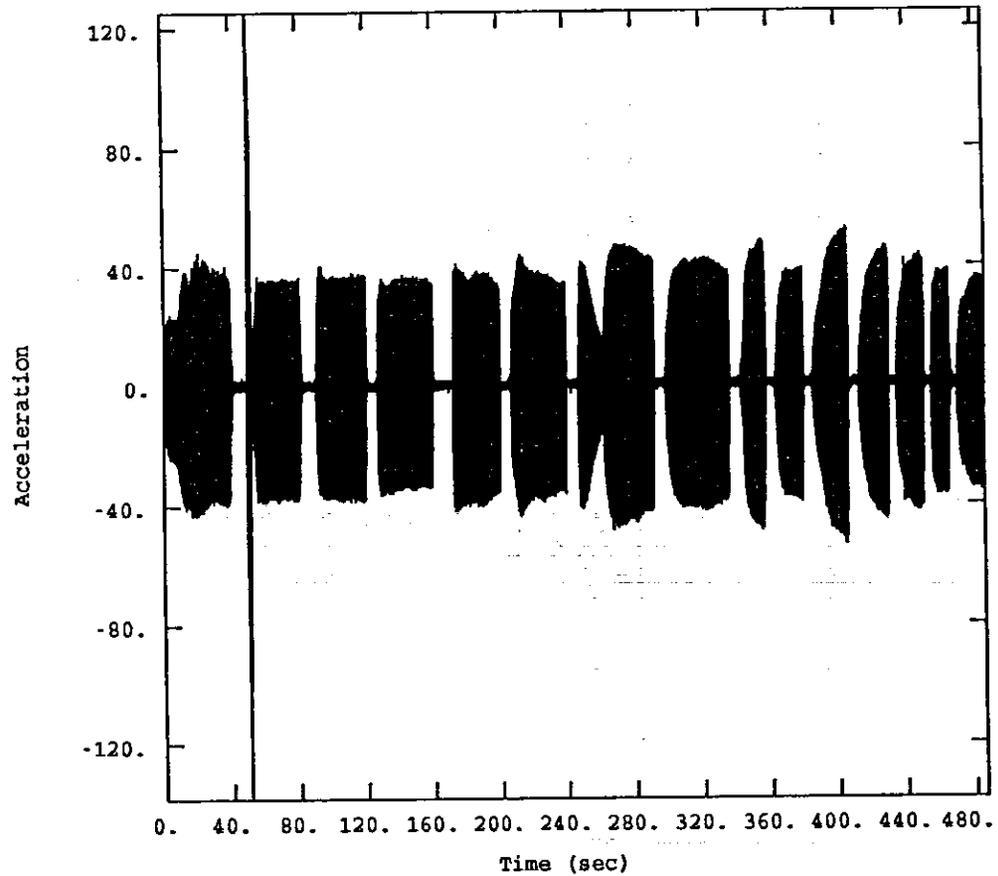


Figure b4

# ABAQUS

— ACCEL1

Input Motion

SHAKEB

Up/downstream

Acceleration

Measured at Model Base

(inch/sec<sup>2</sup>)

XMIN .000E+00  
XMAX 4.722E+02  
YMIN -1.635E+03  
YMAX 1.678E+03

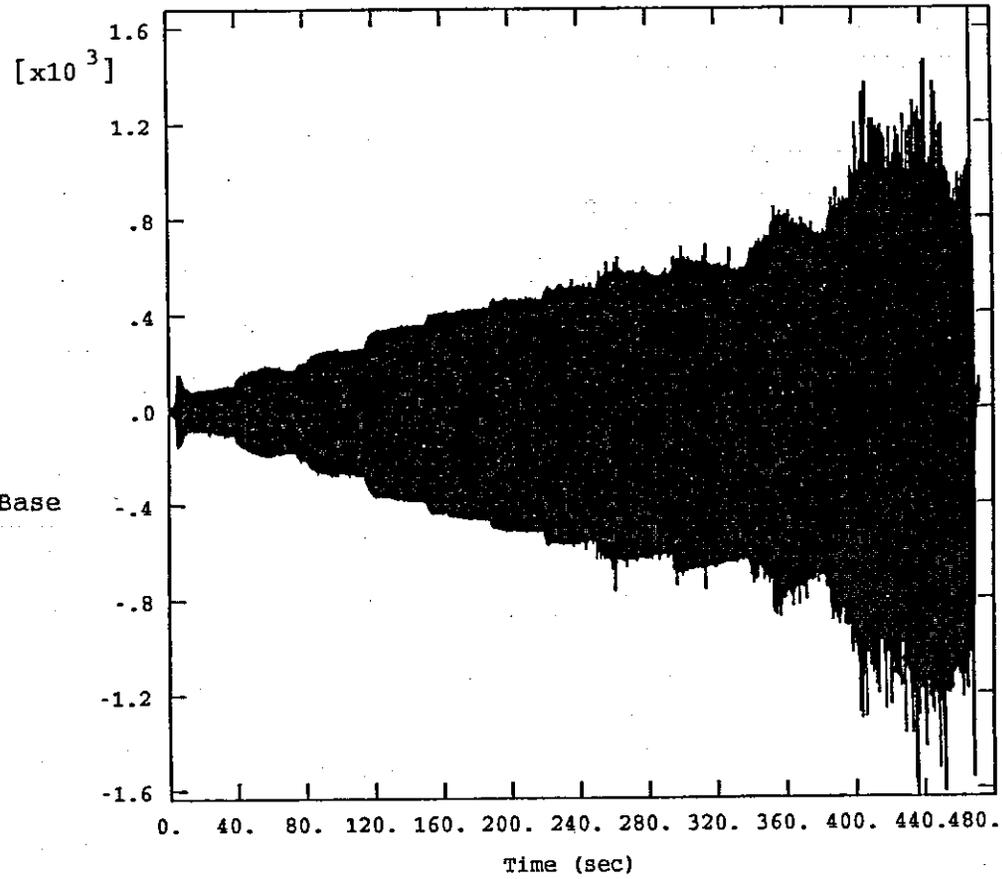


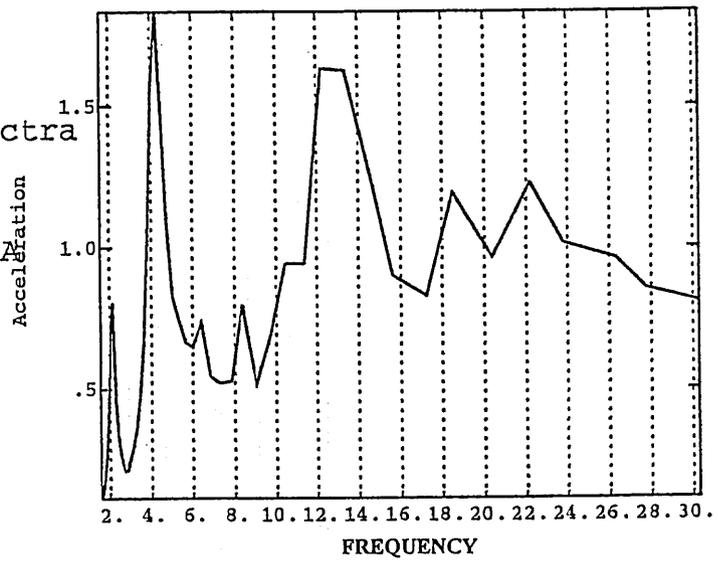
Figure b5

# ABAQUS

— SHAKEA

Response Spectra  
For Input  
Motion SHAKEA

XMIN 1.555E+00  
XMAX 3.030E+01  
YMIN 1.108E-01  
YMAX 1.833E+00



# ABAQUS

— SHAKEB

Response Spectra  
For Input  
Motion SHAKEB

XMIN 1.555E+00  
XMAX 3.030E+01  
YMIN 2.107E+00  
YMAX 2.759E+01

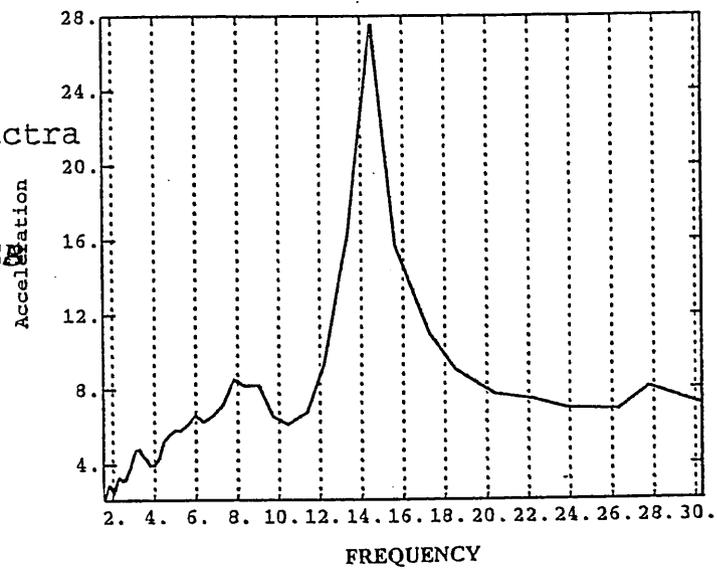


Figure b6

# ABAQUS

— LVDT1

Up/downstream  
Displacement  
Input Motion SHAKEB  
LVDT # 1  
(inches)

XMIN .000E+00  
XMAX 4.722E+02  
YMIN -1.811E-01  
YMAX 4.953E-02

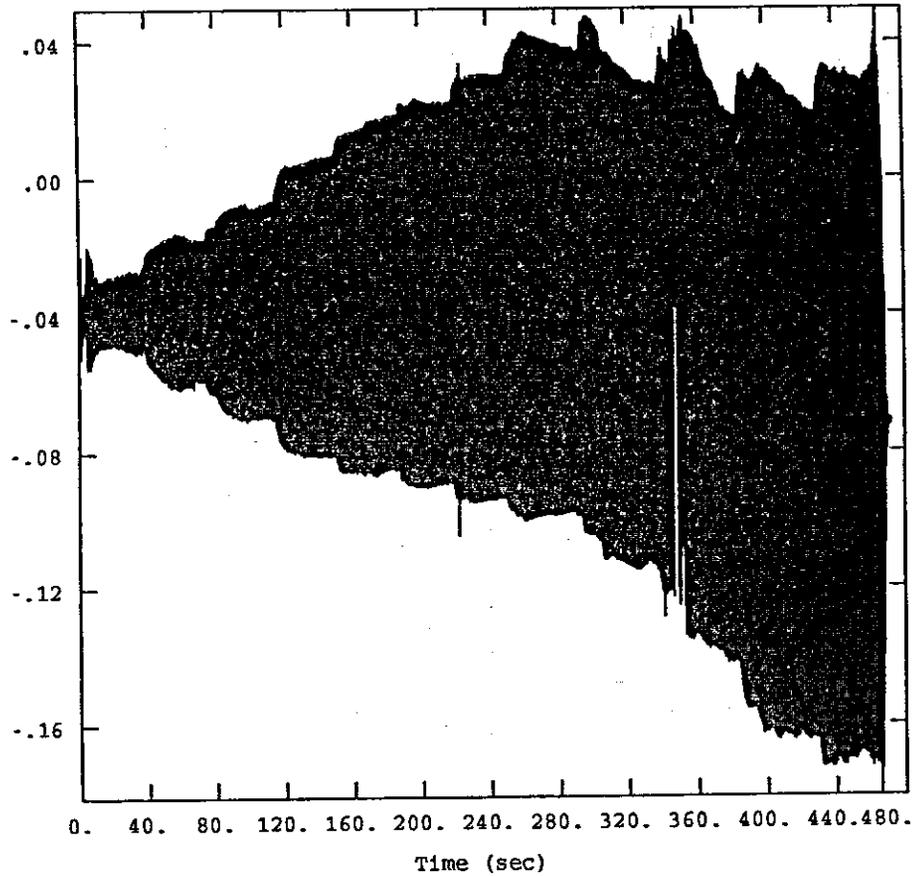
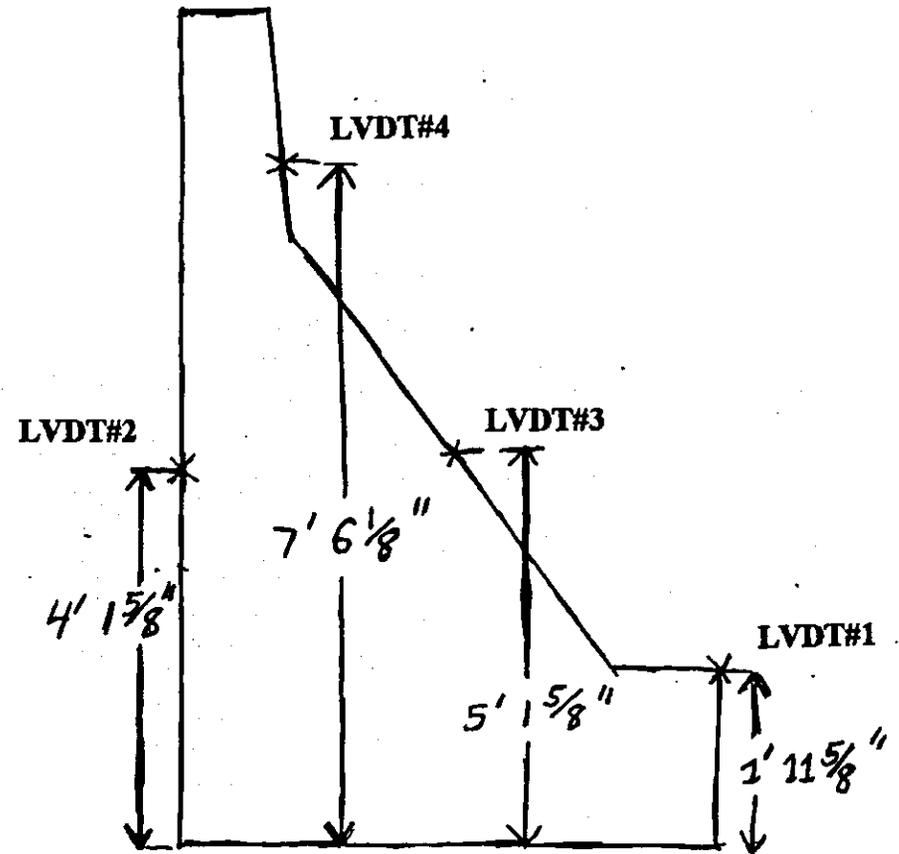
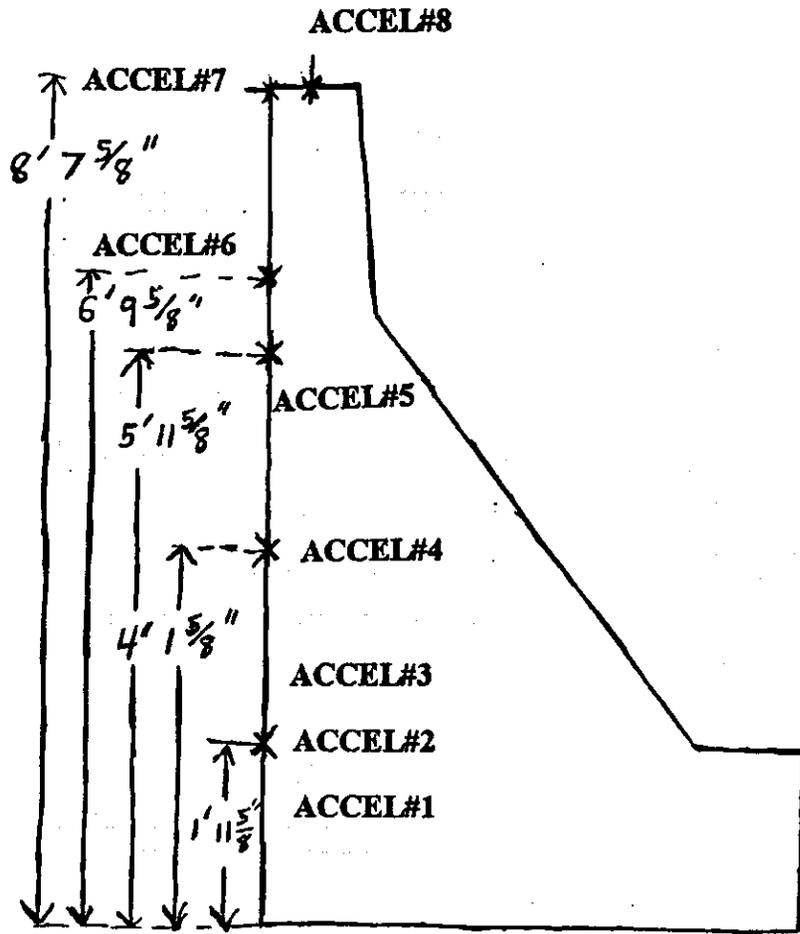


Figure b7

# INSTRUMENTATION LOCATIONS



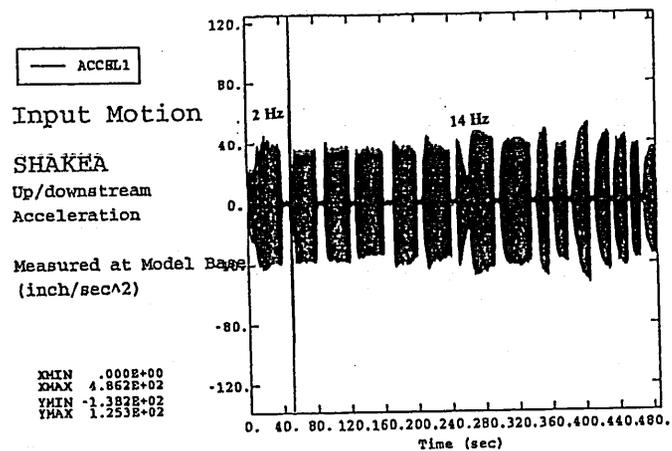
ACCELEROMETERS #1 - #8

LVDT'S #1 - #4

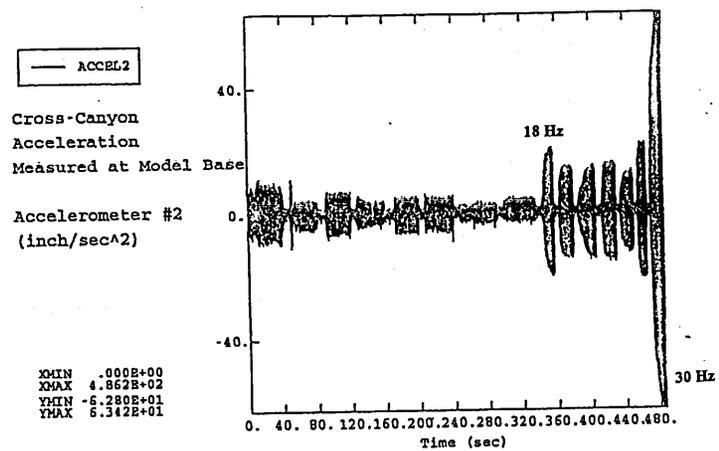
Figure b8

**Appendix C**  
**Laboratory Shake Test Results**

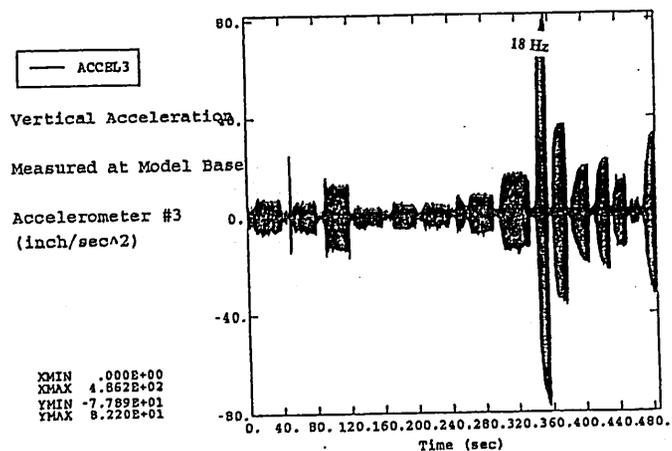
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# ABAQUS



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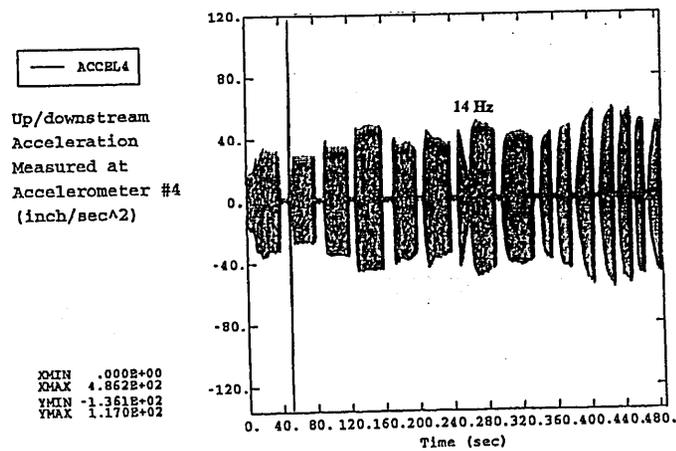
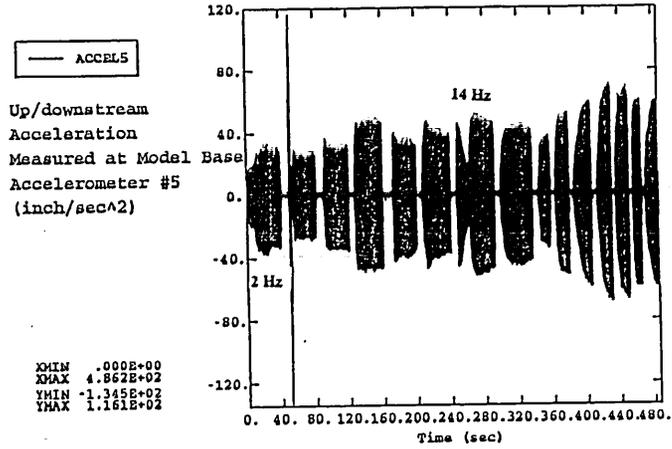
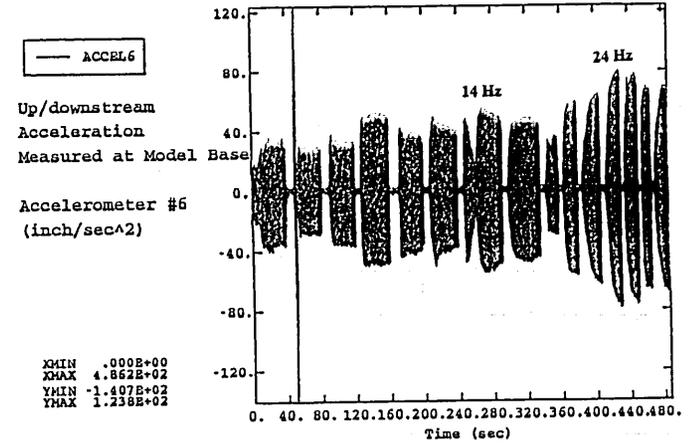


Figure c1

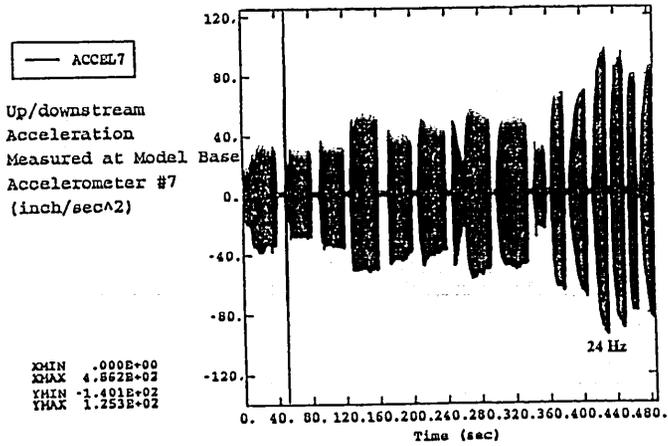
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# ABAQUS



# ABAQUS



# ABAQUS

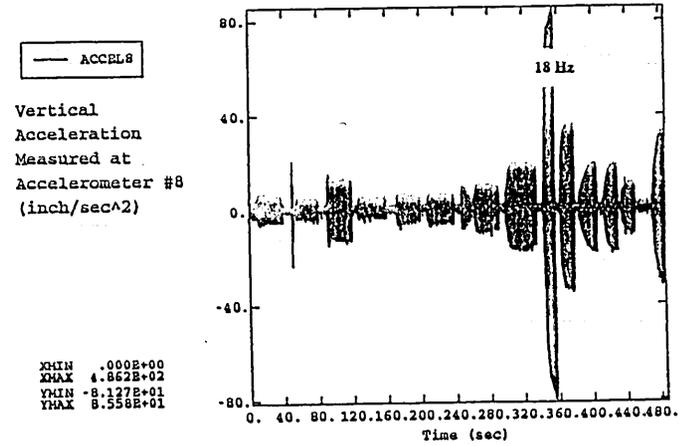


Figure c2

W2: Damping

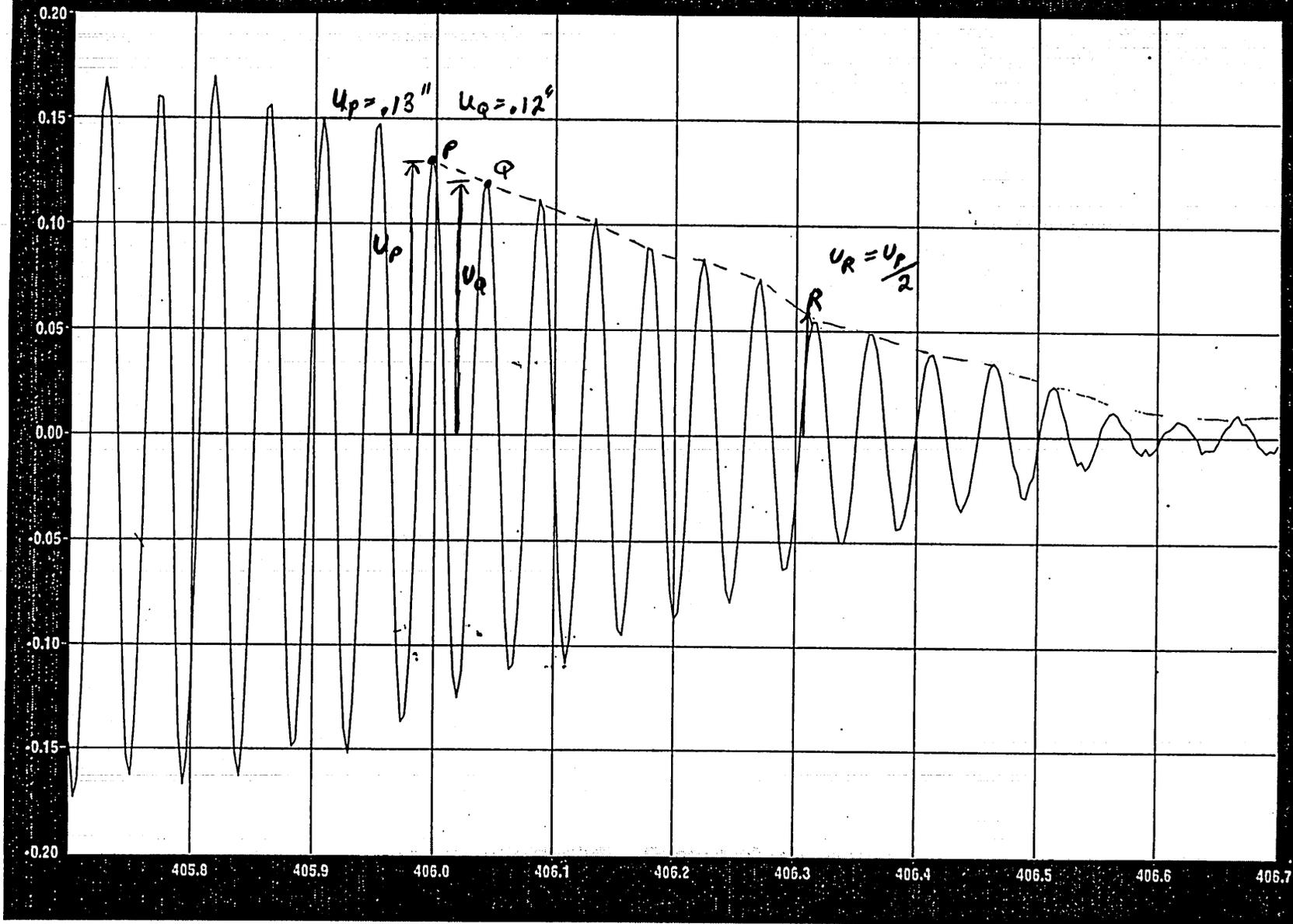
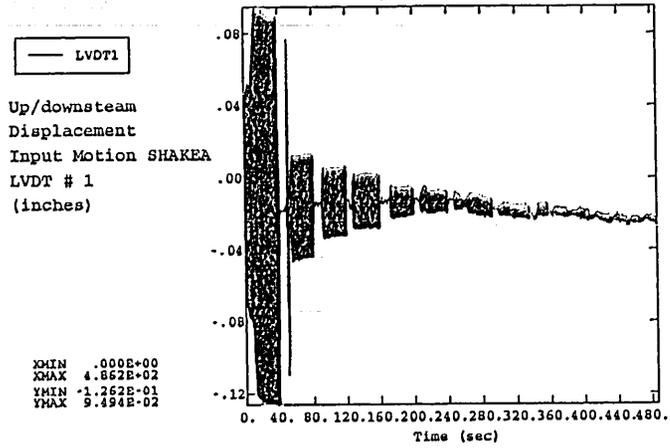
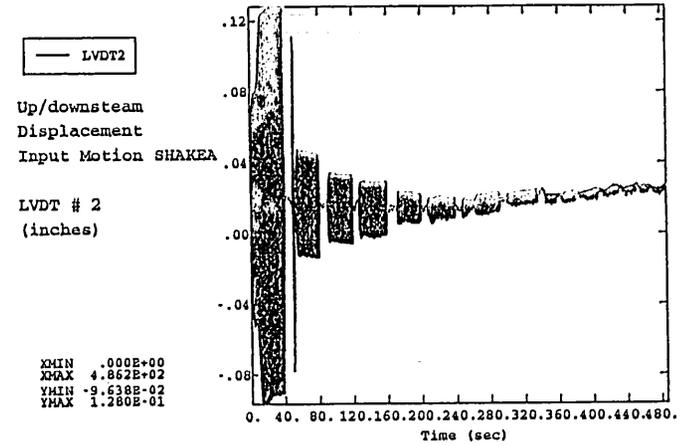


Figure c3

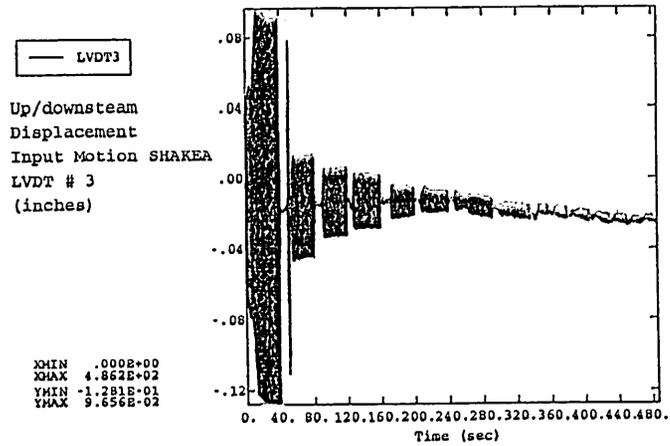
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# ABAQUS



# ABAQUS



# ABAQUS

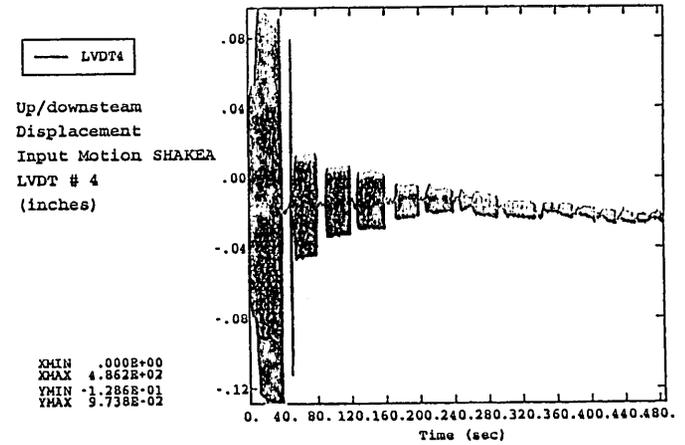
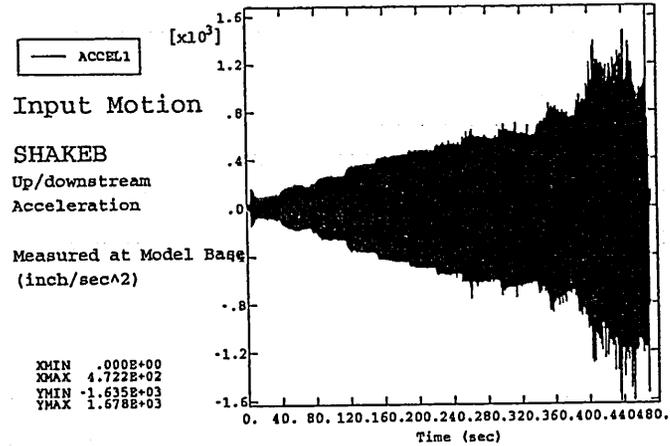
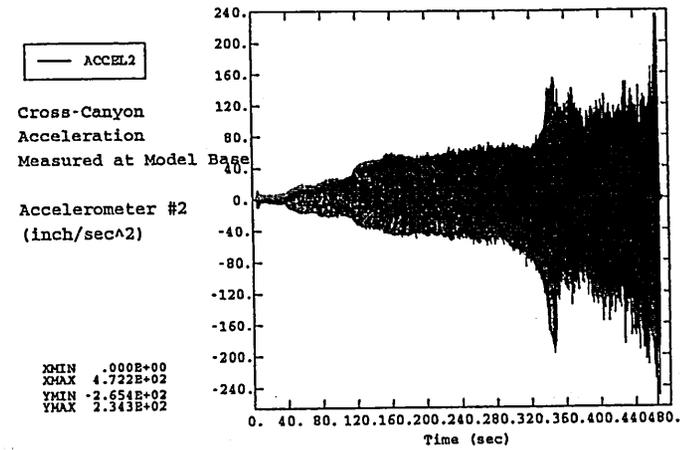


Figure C4

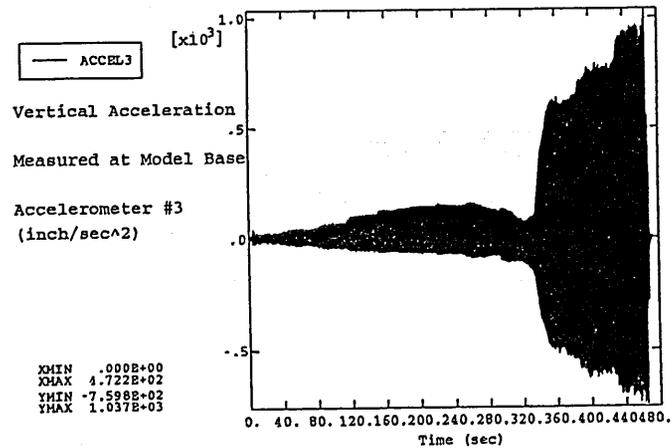
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# ABAQUS



# ABAQUS



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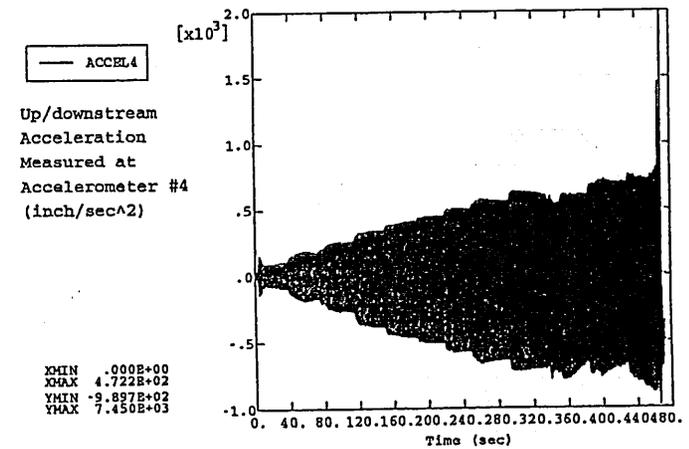
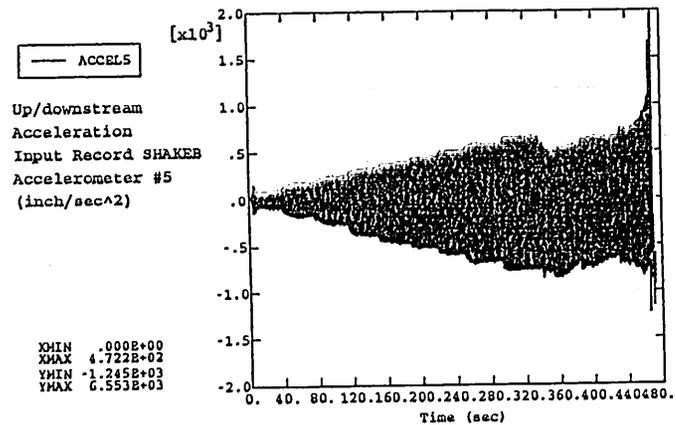
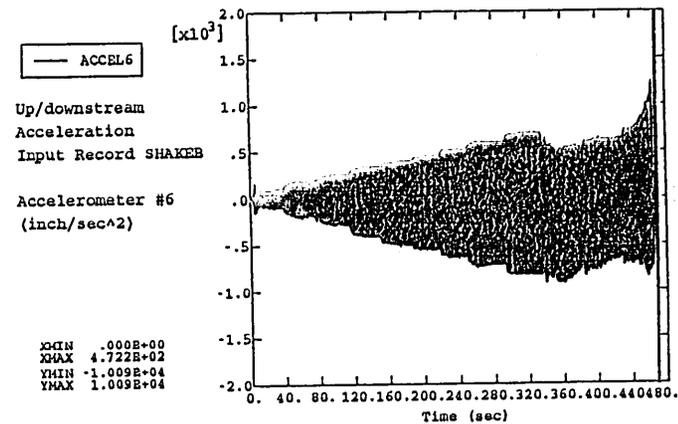


Figure C5

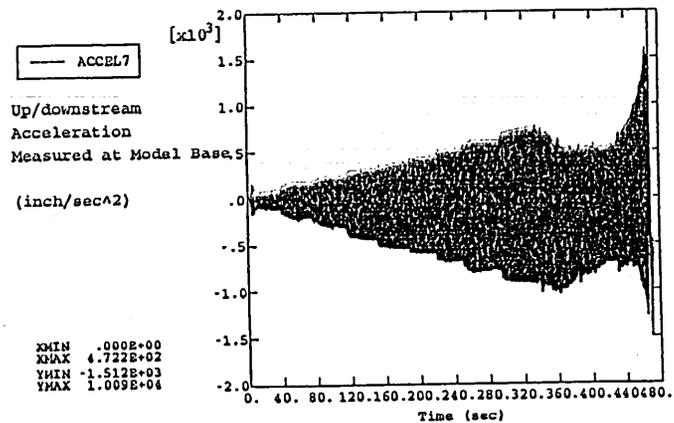
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# ABAQUS



# ABAQUS



# ABAQUS

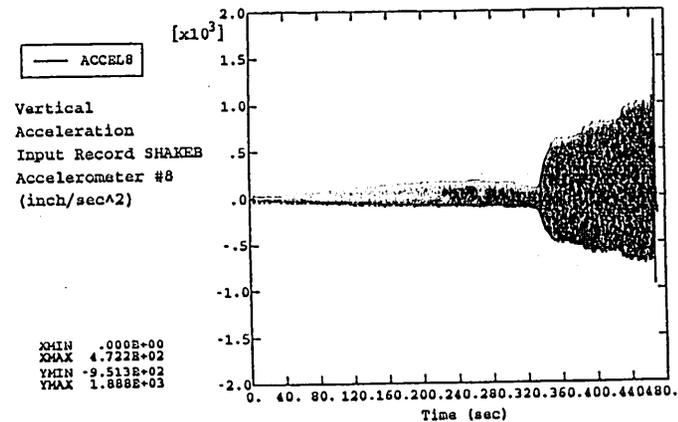
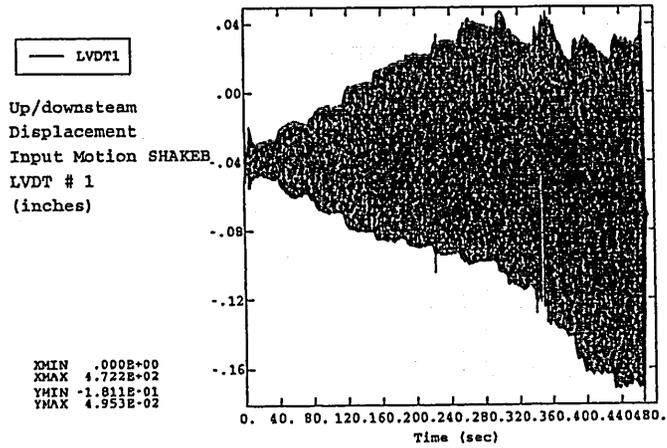
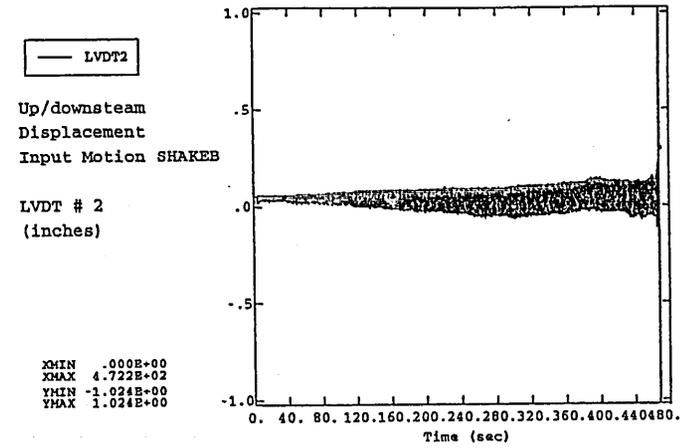


Figure c6

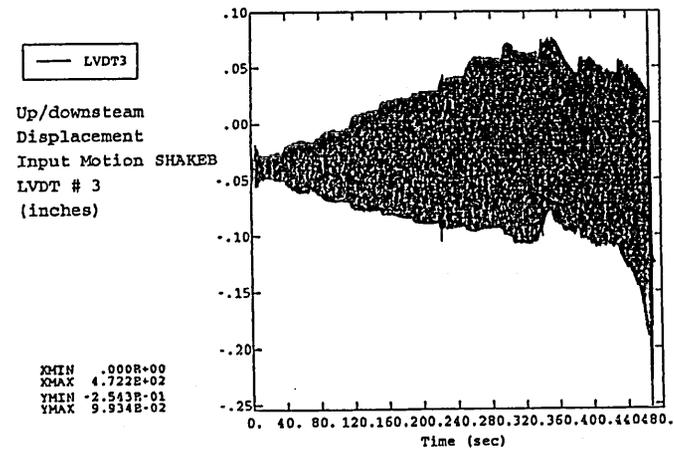
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# ABAQUS



# ABAQUS



# ABAQUS

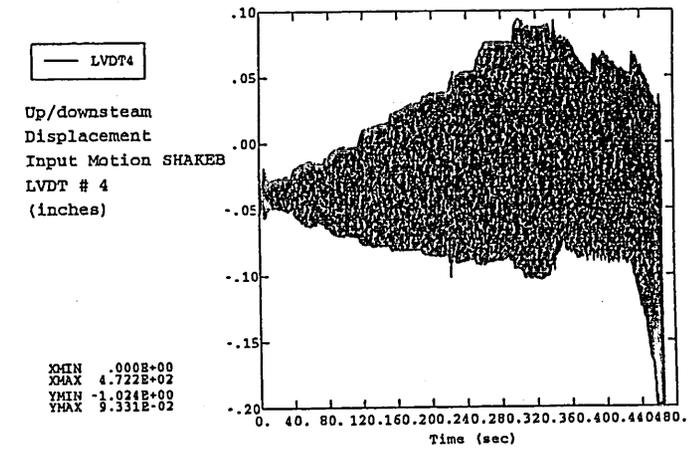


Figure c7



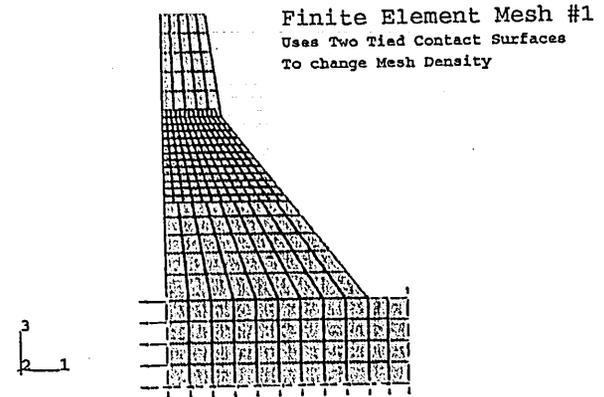
**Appendix D**  
**ABAQUS Finite Element Models**

# ABAQUS

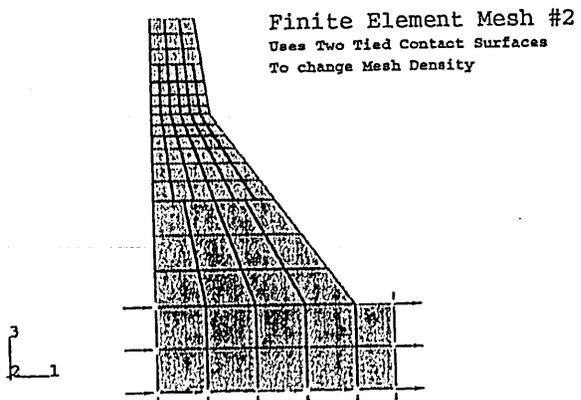
Koyna Laboratory Model Study  
Uncracked Model Study  
Used to Evaluate  
Linear and Non-linear  
Material Propertys  
For  
ABAQUS STANDARD & EXPLICIT

Determination of Mesh Sensitivity  
Non-linear Material Propertys  
Failure Stress = 55 psi  
Mode I Fracture Energy = 0.2012  
Crack Opening Strain = .001375

# ABAQUS



# ABAQUS



# ABAQUS

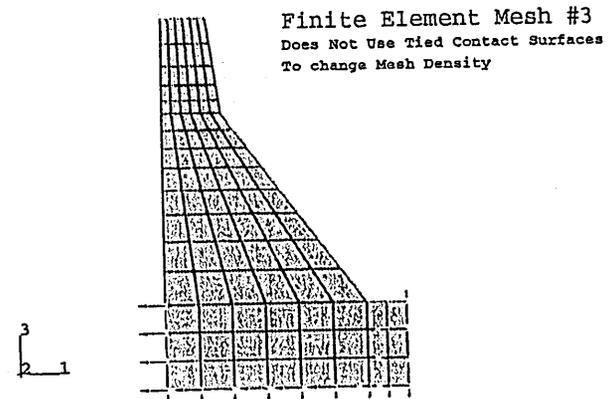


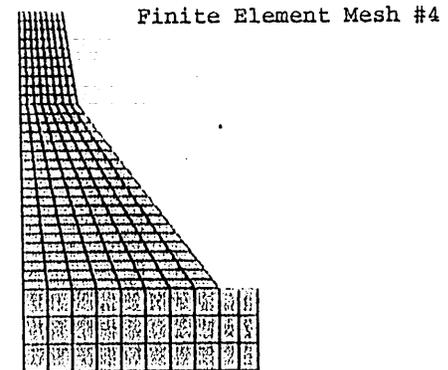
Figure d1

# ABAQUS

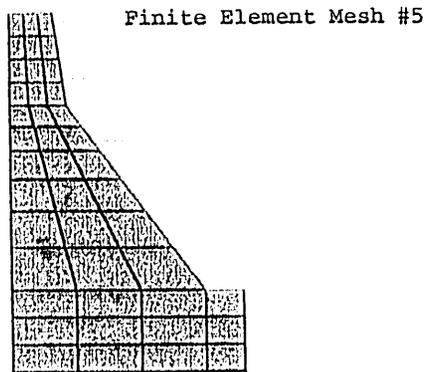
Koyna Laboratory Model Study  
Uncracked Model Study  
Used to Evaluate  
Linear and Non-linear  
Material Propertys  
For  
ABAQUS STANDARD & EXPLICIT

Determination of Mesh Sensitivity

# ABAQUS



# ABAQUS



# ABAQUS

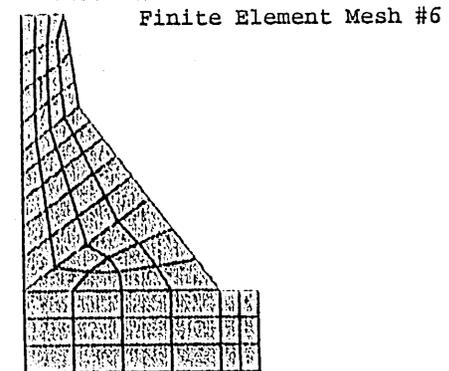


Figure d2

# ABAQUS

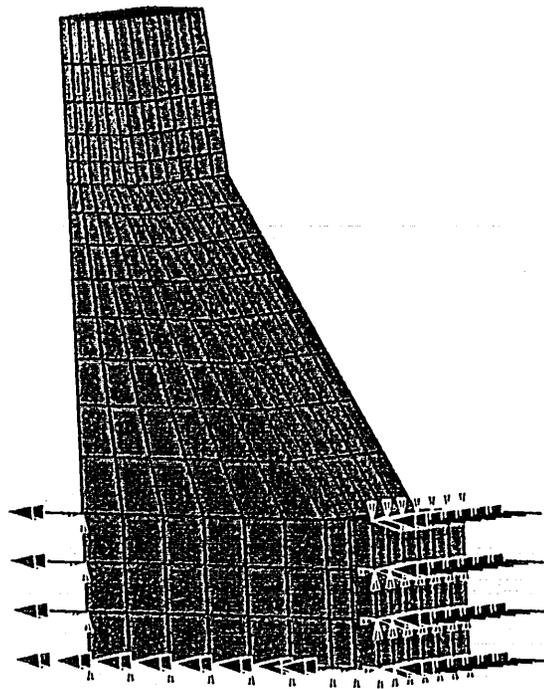


Figure d3

# ABAQUS

Koyna Laboratory Model Study  
Locations of Instrumentation  
Uncracked Model Study

Laboratory Test Model

Instrument	Elevation	Face	Corresponding Node
Accel04	49.6 inches	Upstream	503
Accel05	71.5 inches	Upstream	1534
Accel06	81.6 inches	Upstream	1955
Accel07	103.6 inches	Upstream	2075
Accel08	103.6 inches	Top	2085
LVDT01	23.6 inches	Downstream	298
LVDT02	49.6 inches	Upstream	503
LVDT03	61.6 inches	Downstream	1135
LVDT04	90.1 inches	Downstream	2010

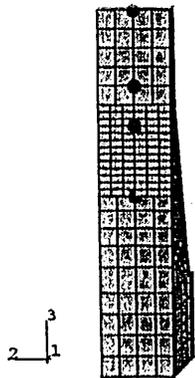
# ABAQUS

Location of Nodes in ABAQUS Model ( Mesh #1 )  
Used for Comparisons  
of Disp. and Accel. Time Histories  
Vertical Accelerometer ACCEL08



2  
Plan View - Node 2085 - Center of Top Face

# ABAQUS



Location of Nodes in  
ABAQUS Model ( Mesh #1 )  
Elev. View - Vertical Face  
Used for Comparisons of  
Disp. and Accel. Time Histories  
Horizontal Accelerometers

Node	Elevation
2075	103.6 inches
1955	82.3 inches
1534	70.9 inches
503	50.9 inches

# ABAQUS

Location of Nodes in  
ABAQUS Model ( Mesh #1 )  
Elev. View  
Downstream (Sloped) Face  
Used for Comparisons of  
Disp. and Accel. Time Histories



Horizontal LVDT's

Node	Elevation
2010	87.6 inches
1135	60.8 inches
298	23.6 inches

# ABAQUS

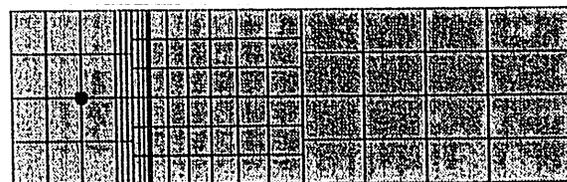
Koyna Laboratory Model Study  
Locations of Instrumentation  
Uncracked Model Study

Laboratory Test Model

Instrument	Elevation	Face	Corresponding Node
Accel04	49.6 inches	Upstream	118
Accel05	71.5 inches	Upstream	267
Accel06	81.6 inches	Upstream	610
Accel07	103.6 inches	Upstream	707
Accel08	103.6 inches	Top	717
LVDT01	23.6 inches	Downstream	8
LVDT02	49.6 inches	Upstream	118
LVDT03	61.6 inches	Downstream	407
LVDT04	90.1 inches	Downstream	762

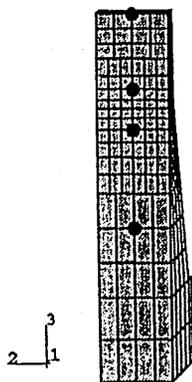
# ABAQUS

Location of Nodes in ABAQUS Model ( Mesh #2 )  
Used for Comparisons  
of Disp. and Accel. Time Histories  
Vertical Accelerometer ACCEL08



Plan View - Node 717 - Center of Top Face

# ABAQUS

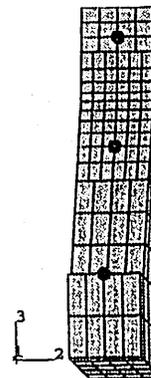


Location of Nodes in  
ABAQUS Model ( Mesh #2 )  
Elev. View - Vertical Face  
Used for Comparisons of  
Disp. and Accel. Time Histories  
Horizontal Accelerometers

Node	Elevation
707	103.6 inches
610	82.3 inches
267	70.9 inches
118	43.1 inches

# ABAQUS

Location of Nodes in  
ABAQUS Model ( Mesh #2 )  
Elev. View  
Downstream (Sloped) Face  
Used for Comparisons of  
Disp. and Accel. Time Histories



Horizontal LVDT's

Node	Elevation
762	95.1 inches
407	63.2 inches
8	23.6 inches

# ABAQUS

Koyna Laboratory Model Study  
Locations of Instrumentation  
Uncracked Model Study

Laboratory Test Model

Instrument	Elevation	Face	Corresponding Node
Accel04	49.6 inches	Upstream	519
Accel05	71.5 inches	Upstream	419
Accel06	81.6 inches	Upstream	204
Accel07	103.6 inches	Upstream	176
Accel08	103.6 inches	Top	179
LVDT01	23.6 inches	Downstream	859
LVDT02	49.6 inches	Upstream	519
LVDT03	61.6 inches	Downstream	511
LVDT04	90.1 inches	Downstream	196

# ABAQUS

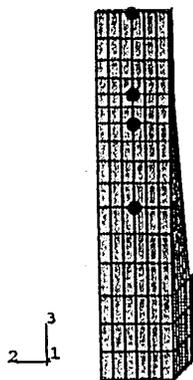
Location of Nodes in ABAQUS Model ( Mesh#3 )  
Used for Comparisons  
of Disp. and Accel. Time Histories  
Vertical Accelerometer ACCEL08



Plan View - Node 179 - Center of Top Face

# ABAQUS

Location of Nodes in  
ABAQUS Model ( Mesh #3 )  
Elev. View - Vertical Face  
Used for Comparisons of  
Disp. and Accel. Time Histories  
Horizontal Accelerometers



Node	Elevation
176	103.6 inches
204	80.6 inches
491	72.3 inches
519	48.6 inches

# ABAQUS

Location of Nodes in  
ABAQUS Model ( Mesh#3 )  
Elev. View  
Downstream (Sloped) Face  
Used for Comparisons of  
Disp. and Accel. Time Histories

Horizontal LVDT's

Node	Elevation
196	90.1 inches
511	61.6 inches
859	23.6 inches



# ABAQUS

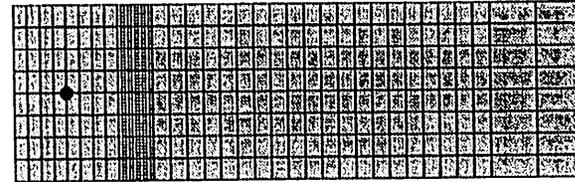
Koyna Laboratory Model Study  
Locations of Instrumentation  
Uncracked Model Study

Laboratory Test Model

Instrument	Elevation	Face	Corresponding Node
Accel104	49.6 inches	Upstream	118
Accel105	71.5 inches	Upstream	267
Accel106	81.6 inches	Upstream	610
Accel107	103.6 inches	Upstream	707
Accel108	103.6 inches	Top	717
LVDT01	23.6 inches	Downstream	8
LVDT02	49.6 inches	Upstream	118
LVDT03	61.6 inches	Downstream	407
LVDT04	90.1 inches	Downstream	762

# ABAQUS

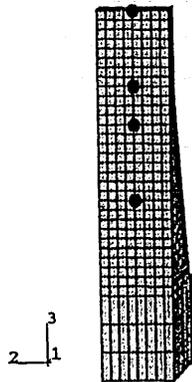
Location of Nodes in ABAQUS Model ( Mesh #4 )  
Used for Comparisons  
of Disp. and Accel. Time Histories  
Vertical Accelerometer ACCEL08



2  
Plan View - Node 401 - Center of Top Face

# ABAQUS

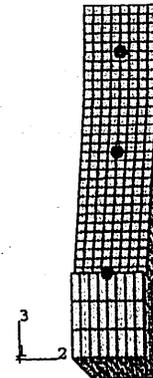
Location of Nodes in  
ABAQUS Model ( Mesh #2 )  
Elev. View - Vertical Face  
Used for Comparisons of  
Disp. and Accel. Time Histories  
Horizontal Accelerometers



Node	Elevation
397	103.6 inches
469	82.2 inches
1621	71.6 inches
1693	50.3 inches

# ABAQUS

Location of Nodes in  
ABAQUS Model ( Mesh #4 )  
Elev. View  
Downstream (Sloped) Face  
Used for Comparisons of  
Disp. and Accel. Time Histories



Horizontal LVDT's

Node	Elevation
450	90.3 inches
1665	60.9 inches
2788	23.6 inches

# ABAQUS

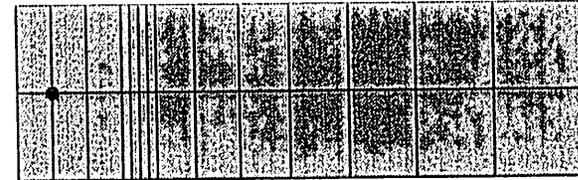
## Koyna Laboratory Model Study Locations of Instrumentation Uncracked Model Study

### Laboratory Test Model

Instrument	Elevation	Face	Corresponding Node
Accel04	49.6 inches	Upstream	118
Accel05	71.5 inches	Upstream	267
Accel06	81.6 inches	Upstream	610
Accel07	103.6 inches	Upstream	707
Accel08	103.6 inches	Top	717
LVDT01	23.6 inches	Downstream	8
LVDT02	49.6 inches	Upstream	118
LVDT03	61.6 inches	Downstream	407
LVDT04	90.1 inches	Downstream	762

# ABAQUS

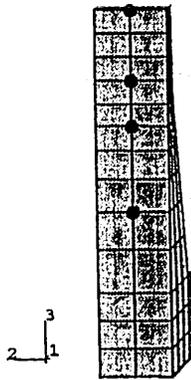
Location of Nodes in ABAQUS Model ( Mesh #5 )  
Used for Comparisons  
of Disp. and Accel. Time Histories  
Vertical Accelerometer ACCEL08



Plan View - Node 22 - Center of Top Face

# ABAQUS

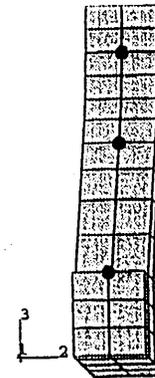
Location of Nodes in  
ABAQUS Model ( Mesh #5 )  
Elev. View - Vertical Face  
Used for Comparisons of  
Disp. and Accel. Time Histories  
Horizontal Accelerometers



Node	Elevation
21	103.6 inches
33	83.6 inches
85	70.7 inches
97	46.4 inches

# ABAQUS

Location of Nodes in  
ABAQUS Model ( Mesh #5 )  
Elev. View  
Downstream (Sloped) Face  
Used for Comparisons of  
Disp. and Accel. Time Histories



### Horizontal LVDT's

Node	Elevation
32	90.3 inches
92	63.8 inches
173	23.6 inches

# ABAQUS

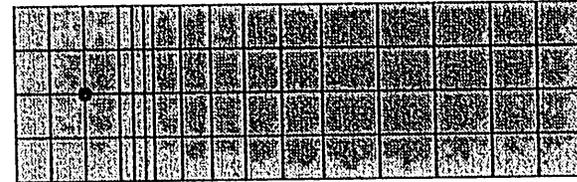
Koyna Laboratory Model Study  
Locations of Instrumentation  
Uncracked Model Study

Laboratory Test Model

Instrument	Elevation	Face	Corresponding Node
Accel04	49.6 inches	Upstream	196
Accel05	71.5 inches	Upstream	104
Accel06	81.6 inches	Upstream	124
Accel07	103.6 inches	Upstream	163
Accel08	103.6 inches	Top	165
LVDT01	23.6 inches	Downstream	289
LVDT02	49.6 inches	Upstream	196
LVDT03	61.6 inches	Downstream	232
LVDT04	90.1 inches	Downstream	140

# ABAQUS

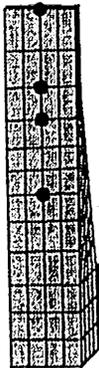
Location of Nodes in ABAQUS Model ( Mesh#6 )  
Used for Comparisons  
of Disp. and Accel. Time Histories  
Vertical Accelerometer ACCEL08



Plan View - Node 165 - Center of Top Face

# ABAQUS

Location of Nodes in  
ABAQUS Model ( Mesh #6 )  
Elev. View - Vertical Face  
Used for Comparisons of  
Disp. and Accel. Time Histories  
Horizontal Accelerometers



Node	Elevation
163	103.6 inches
124	80.8 inches
104	71.5 inches
196	49.8 inches

# ABAQUS

Location of Nodes in  
ABAQUS Model ( Mesh#6 )  
Elev. View  
Downstream (Sloped) Face  
Used for Comparisons of  
Disp. and Accel. Time Histories



Horizontal LVDT's

Node	Elevation
140	92.8 inches
232	62.5 inches
289	23.6 inches

**Appendix E**  
**Sensitivity of Results to the**  
**Number of Modes Extracted in the**  
**Frequency Analysis**

# ABAQUS

— ACTLVDT

LVDT Displacement

Record In

Actuator

(inches)

XMIN .000E+00  
XMAX 4.862E+02  
YMIN -1.056E-01  
YMAX 1.397E-01

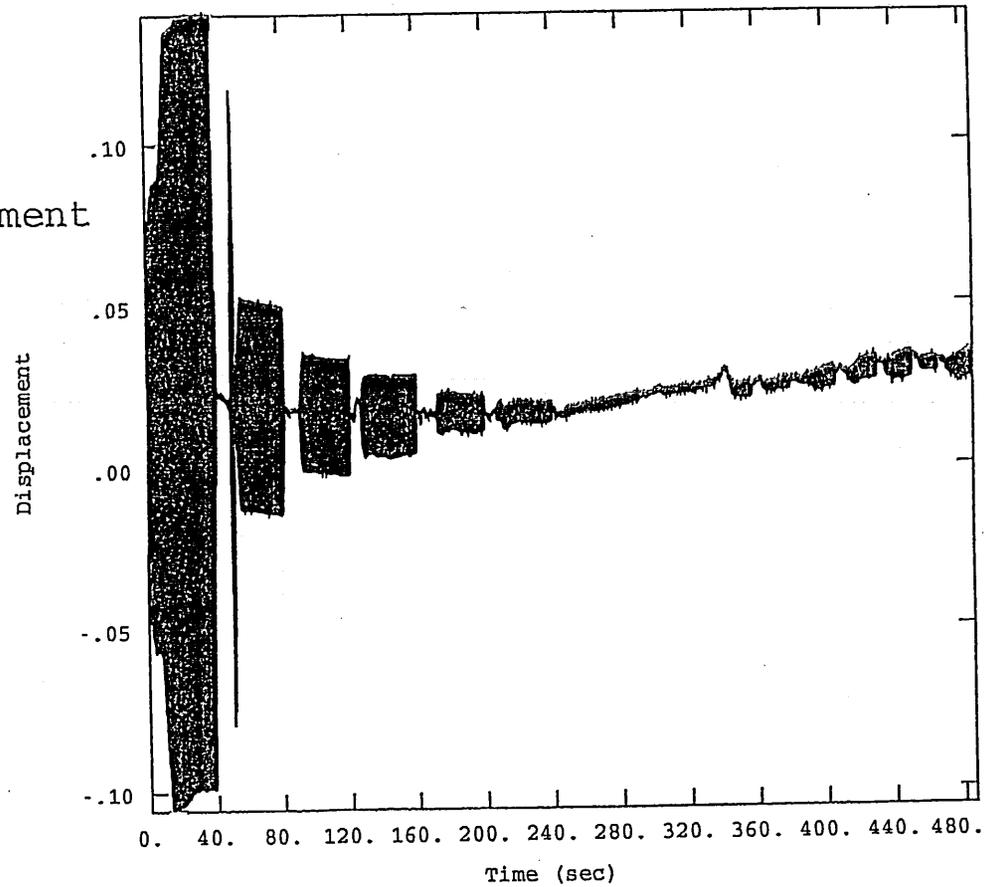


Figure e1

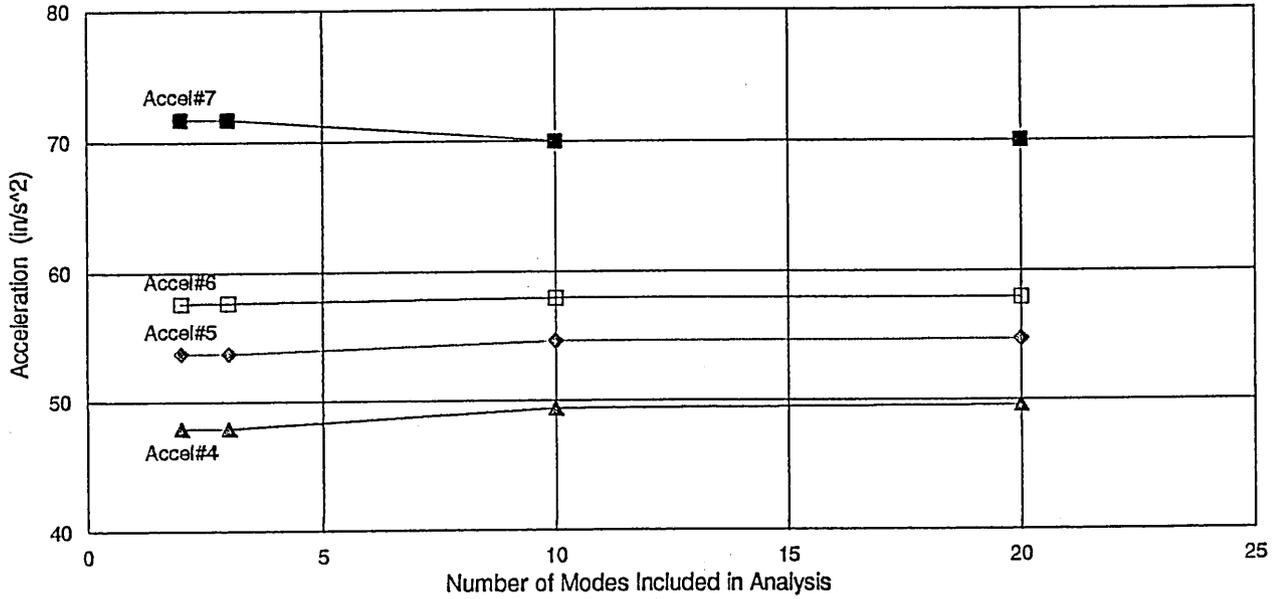
Uncracked Koyna Laboratory Study  
 Determination of the Number of Modes Required  
 Mesh#3

Material Properties

E = 150 ksi  
 Material Density = 138.2 pcf

Damping = 5% critical  
 Rayleigh Damping Factors  
 Alpha=2.827433, Beta=.000318

**Peak Accelerations**  
 Number of Modes Varied



Peak Accelerations ( inch / sec ^ 2 )

Number of Modes Used	2	3	10	20	LAB
Accel#7	71.71	71.71	69.98	69.99	53.26
Accel#6	57.60	57.66	57.99	57.99	51.72
Accel#5	53.67	53.67	54.55	54.64	49.26
Accel#4	47.89	47.89	49.35	49.56	47.72
CPU Time (sec)	53.04	56.91	163.21	210.94	

Figure e2

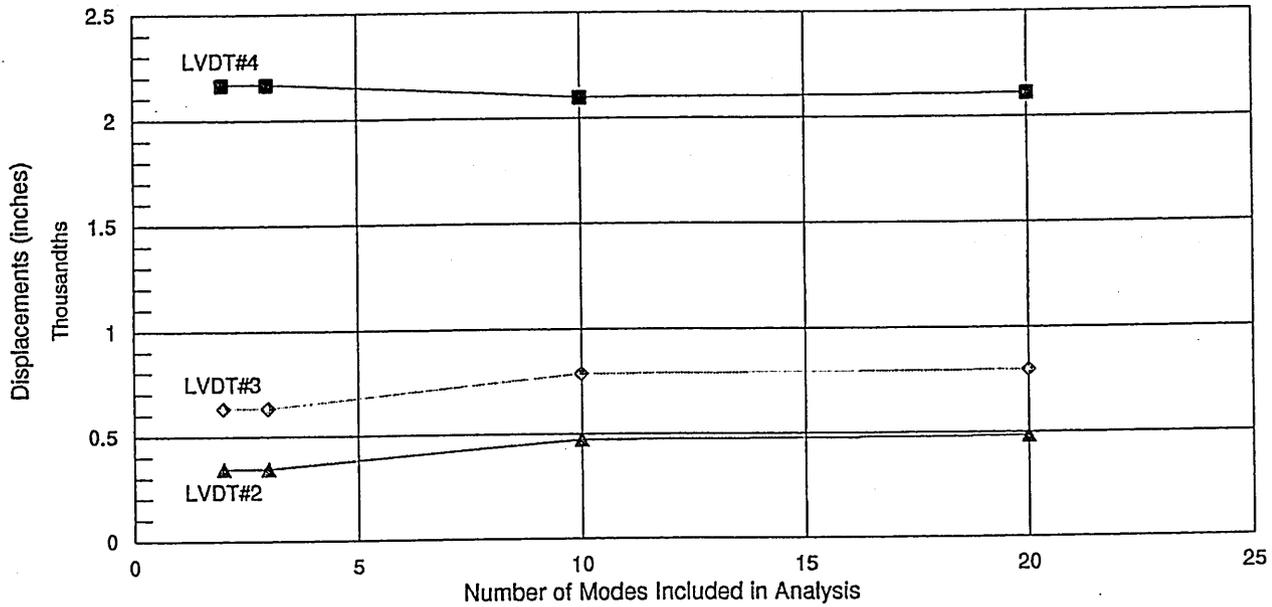
Uncracked Koyna Laboratory Study  
 Determination of the Number of Modes Required  
 Mesh#3

Material Properties

E = 150 ksi  
 Material Density = 138.2 pcf

Damping = 5% critical  
 Rayleigh Damping Factors  
 Alpha=2.827433, Beta=.000318

**Peak Displacements**  
 Number of Modes Varied



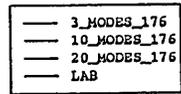
Peak Displacements ( inches )

Number of Modes Used	2	3	10	20	LAB
LVDT#4	2.2E-03	2.2E-03	2.1E-03	2.1E-03	7.2E-04
LVDT#3	6.3E-04	6.3E-04	7.9E-04	7.9E-04	3.1E-04
LVDT#2	3.4E-04	3.4E-04	4.7E-04	4.8E-04	2.1E-04

Figure e3

# ABAQUS

Number of Modes Extracted in Frequency Analysis Varied



Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model

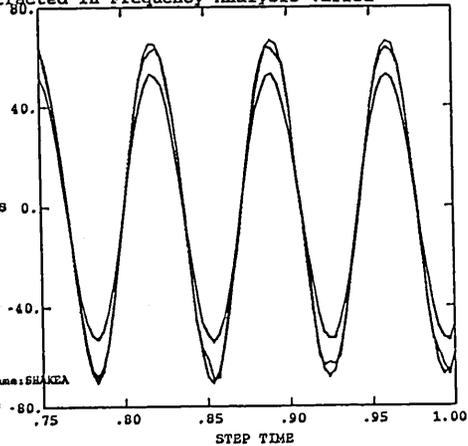
Acceleration  
at ACCEL#7

Modal Damping, 5%

Density = 138 pcf

Input Freq = 14 Hz Filename:SHAKEA

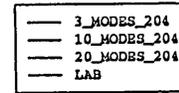
Total Time : 279.75 to 280 sec



ABAQUS Modal Dynamic Analyses vs Laboratory Measurements

# ABAQUS

Number of Modes Extracted in Frequency Analysis Varied



Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model

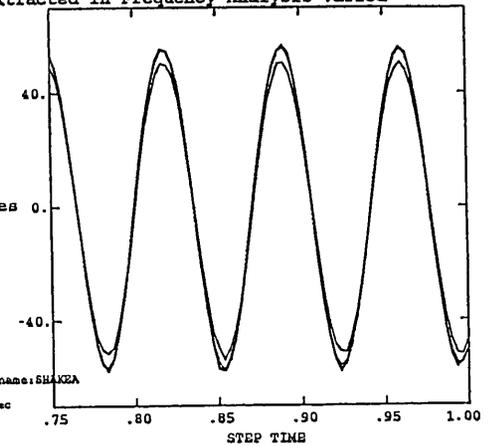
Acceleration  
at ACCEL#6

Modal Damping, 5%

Density = 138 pcf

Input Freq = 14 Hz Filename:SHAKEA

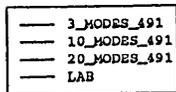
Total Time : 279.75 to 280 sec



ABAQUS Modal Dynamic Analyses vs Laboratory Measurements

# ABAQUS

Number of Modes Extracted in Frequency Analysis Varied



Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model

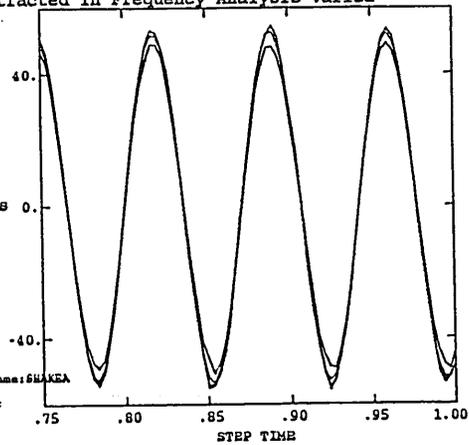
Acceleration  
at ACCEL#5

Modal Damping, 5%

Density = 138 pcf

Input Freq = 14 Hz Filename:SHAKEA

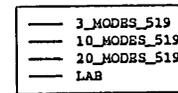
Total Time : 279.75 to 280 sec



ABAQUS Modal Dynamic Analyses vs Laboratory Measurements

# ABAQUS

Number of Modes Extracted in Frequency Analysis Varied



Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model

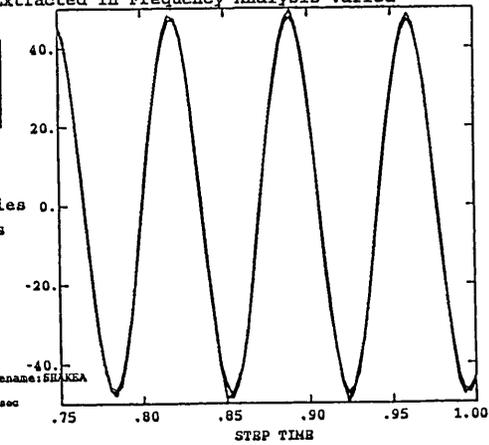
Acceleration  
at ACCEL#4

Modal Damping, 5%

Density = 138 pcf

Input Freq = 14 Hz Filename:SHAKEA

Total Time : 279.75 to 280 sec



ABAQUS Modal Dynamic Analyses vs Laboratory Measurements

Figure e4

**Appendix F**  
**Sensitivity to Variation in Mesh Definition**

Uncracked Koyna Laboratory Study  
Determination of Mesh Sensitivity  
Six Different Mesh Densities Evaluated

Material Properties

Elastic Modulus = 150,000 psi  
Material Density = 138.2 pcf

Damping = 5% critical  
Rayleigh Damping Factors  
Alpha = 2.827433; Beta = .000318

Natural Frequencies (Hz)

Mode	Mesh#5	Mesh#6	Mesh#2	Mesh#1	Mesh#3	Mesh#4
1	14.1	14.8	15.4	15.5	15.7	15.7
2	28.7	29.2	29.0	29.3	29.9	30.2
3	33.7	49.4	43.6	53.8	54.2	54.4
4	38.0	55.9	51.3	68.3	64.5	70.2
5	40.5	57.8	52.4	74.6	67.3	76.3
6	42.7	59.8	58.2	88.5	69.4	78.5
7	46.9	60.3	59.3	90.5	73.7	81.5
8	48.4	63.0	67.2	91.2	74.6	84.7
9	49.1	63.2	74.6	93.3	75.4	88.2
10	49.1	66.7	88.6	94.0	76.8	91.2

Peak Accelerations ( inch / sec ^ 2 )

Instrument	Mesh#5	Mesh#6	Mesh#2	Mesh#1	Mesh#3	Mesh#4
Accel#7	71.0	71.4	69.5	70.2	70.0	69.4
Accel#6	58.8	57.5	58.4	58.5	58.0	58.8
Accel#5	52.9	53.3	54.5	54.3	54.6	54.6
Accel#4	47.9	48.2	48.4	49.8	49.4	49.9

Peak Displacements ( inches )

Instrument	Mesh#5	Mesh#6	Mesh#2	Mesh#1	Mesh#3	Mesh#4
LVDT#4	2.5E-03	2.5E-03	2.6E-03	2.1E-03	2.1E-03	2.1E-03
LVDT#3	8.2E-04	7.3E-04	9.0E-04	7.8E-04	7.9E-04	7.6E-04
LVDT#2	1.5E-04	4.1E-04	3.7E-04	5.4E-04	4.7E-04	5.1E-04

CPU Seconds

	Mesh#5	Mesh#6	Mesh#2	Mesh#1	Mesh#3	Mesh#4
CPU Sec	20.48	105.79	208.34	895.43	163.21	446.58

Figure f1

# ABAQUS

## Mesh Sensitivity

- MESH1\_2075
- MESH2\_707
- MESH3\_176
- MESH4\_397
- MESH5\_21
- MESH6\_163
- LAB

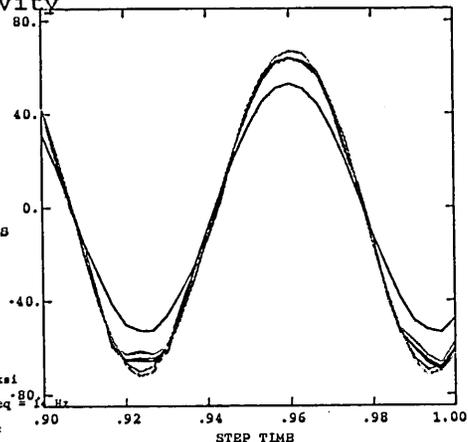
Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model  
Acceleration  
at ACCEL#7

Modal Damping, 5%

Density=138 pcf, E = 150 ksi

Filename:SHAKEA, Input Freq = 1 Hz

Total Time : 279.75 to 280 sec



ABAQUS Modal Dynamic Analyses & Laboratory Measurements

# ABAQUS

## Mesh Sensitivity

- MESH1\_1955
- MESH2\_610
- MESH3\_204
- MESH4\_469
- MESH5\_33
- MESH6\_124
- LAB

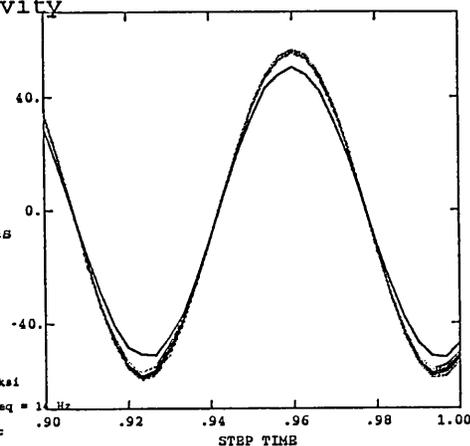
Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model  
Acceleration  
at ACCEL#6

Modal Damping, 5%

Density=138 pcf, E = 150 ksi

Filename:SHAKEA, Input Freq = 1 Hz

Total Time : 279.75 to 280 sec



ABAQUS Modal Dynamic Analyses & Laboratory Measurements

# ABAQUS

## Mesh Sensitivity

- MESH1\_1534
- MESH2\_267
- MESH3\_491
- MESH4\_1621
- MESH5\_85
- MESH6\_104
- LAB

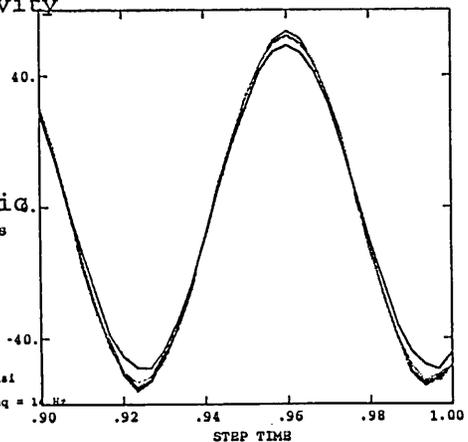
Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model  
Acceleration  
at ACCEL#5

Modal Damping, 5%

Density=138 pcf, E = 150 ksi

Filename:SHAKEA, Input Freq = 1 Hz

Total Time : 279.75 to 280 sec



ABAQUS Modal Dynamic Analyses & Laboratory Measurements

# ABAQUS

## Mesh Sensitivity

- MESH1\_503
- MESH2\_118
- MESH3\_519
- MESH4\_1693
- MESH5\_97
- MESH6\_196
- LAB

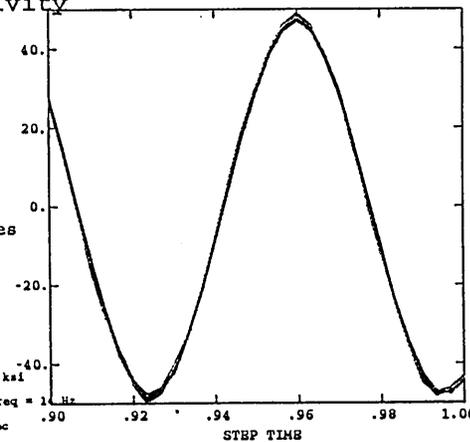
Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model  
Acceleration  
at ACCEL#4

Modal Damping, 5%

Density=138 pcf, E = 150 ksi

Filename:SHAKEA, Input Freq = 1 Hz

Total Time : 279.75 to 280 sec



ABAQUS Modal Dynamic Analyses & Laboratory Measurements

# ABAQUS

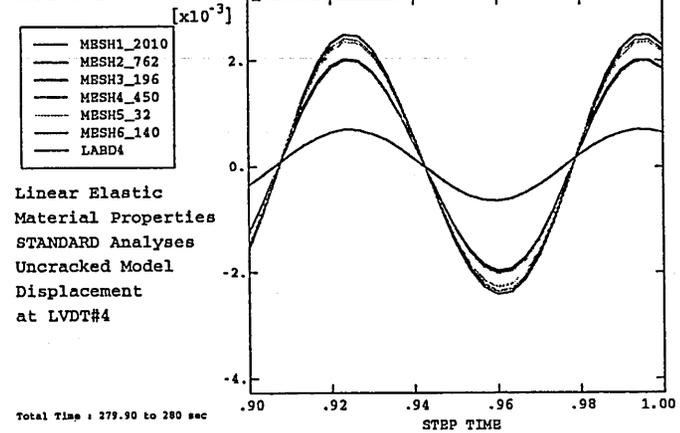
Koyna Laboratory Model Study  
 Uncracked Model Study  
 Sensitivity Study  
 Mesh Density

Comparison of Displacements  
 ABAQUS STANDARD  
 Modal Dynamic Analysis

Input Record SHAKEA  
 Modal Damping, 3.5%  
 Elastic Modulus = 150 ksi  
 Density = 138.2 pcf

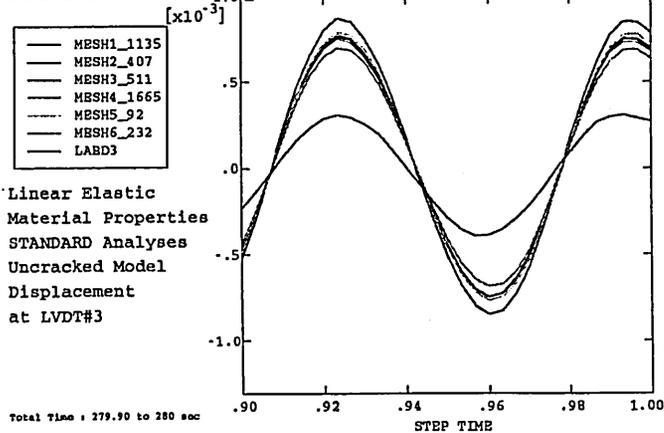
# ABAQUS

## Mesh Sensitivity



# ABAQUS

## Mesh Sensitivity



# ABAQUS

## Mesh Sensitivity

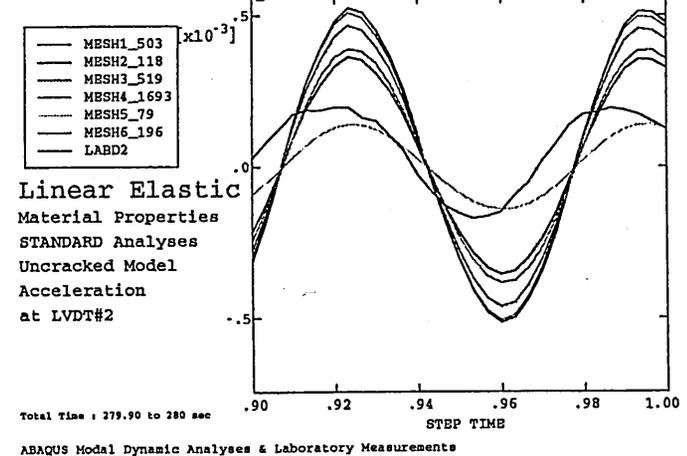


Figure f3

Uncracked Koyna Laboratory Study  
Determination of Mesh Sensitivity  
Six Different Mesh Densities Evaluated

Material Properties

Elastic Modulus = 150,000 psi  
Material Density = 138.2 pcf

Damping = 5% of critical  
Rayleigh Damping Factors

Alpha = 2.827433; Beta = .000318

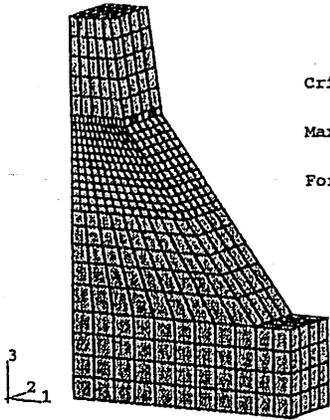
Whole Model Energy Quantities

	"Artificial" Strain Energy "hourglass control"	Total Strain Energy	Kinetic Energy	External Work	Total Energy Balance
Mesh#1					
Static	0.00496	2.45500	0.00000	2.45500	-0.00001500
Dynamic	0.00000	2.45500	0.00646	2.72500	-0.00001500
Response Spectrum	0.00000	1.80000	0.00000	0.00000	-0.00000841
Mesh#2					
Static	0.01096	2.55300	0.00000	2.55300	-0.00001600
Dynamic	0.00000	2.55300	0.00728	0.67020	-0.00001600
Response Spectrum	0.00000	1.87000	0.00000	0.00000	-0.00000851
Mesh#3					
Static	0.00981	2.51600	0.00000	2.51600	-0.00001600
Dynamic	0.00000	2.51600	0.00568	0.55240	-0.00001600
Response Spectrum	0.00000	1.84000	0.00000	0.00000	-0.00000853
Mesh#4					
Static	0.00552	2.51600	0.00000	2.51600	-0.00001600
Dynamic	0.00000	2.51600	0.00538	2.63800	-0.00001600
Response Spectrum	0.00000	1.84000	0.00000	0.00000	-0.00000867
Mesh#5					
Static	0.02687	2.53900	0.00000	2.53900	-0.00001490
Dynamic	0.00000	2.53900	0.00793	-0.57200	-0.00001490
Response Spectrum	0.00000	1.86000	0.00000	0.00000	-0.00000795
Mesh#6					
Static	0.15860	4.43900	0.00000	4.43900	-0.00002500
Dynamic	0.00000	4.43900	0.00716	4.43900	-0.00002500
Response Spectrum	0.00000	3.25400	0.00000	0.00000	-0.00001327

Figure f4

ABAQUS

Response Spectrum Analysis



Mesh#1

Critical Element #1366,1369

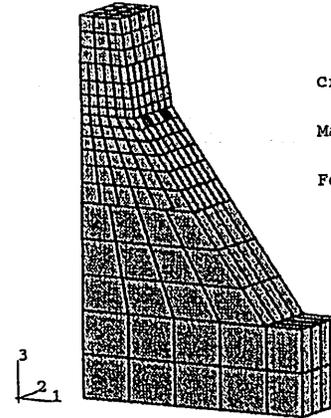
Maximum Principal Stress

For Input Record SHAKEA

23.04 psi

ABAQUS

Response Spectrum Analysis



Mesh#2

Critical Elements #120 & #123

Maximum Principal Stress

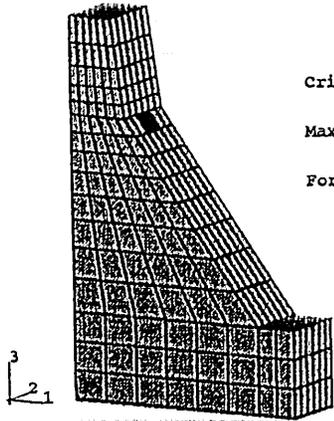
For Input Record SHAKEA

15.22 psi

Figure 55

# ABAQUS

## Response Spectrum Analysis



Mesh#3

Critical Element #282 & #330

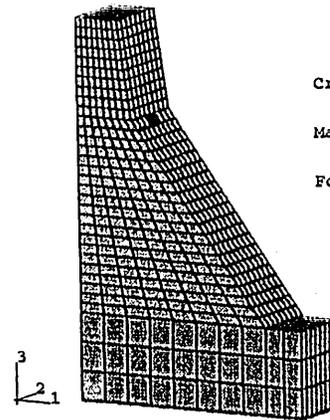
Maximum Principal Stress

For Input Record SHAKEA

14.59 psi

# ABAQUS

## Response Spectrum Analysis



Mesh#4

Critical Elements #1128 & #1288

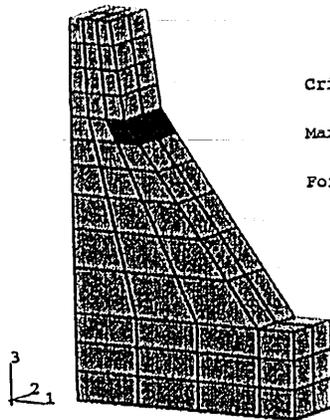
Maximum Principal Stress

For Input Record SHAKEA

17 psi

# ABAQUS

## Response Spectrum Analysis



Mesh#5

Critical Elements #27 & #45

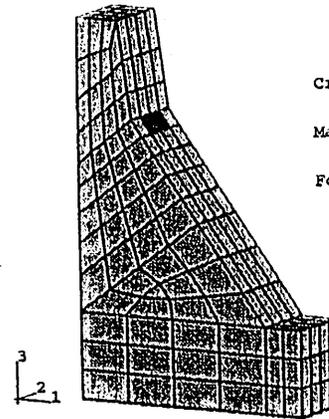
Maximum Principal Stress

For Input Record SHAKEA

9.42 psi

# ABAQUS

## Response Spectrum Analysis



Mesh#6

Critical Elements #74 & #75

Maximum Principal Stress

For Input Record SHAKEA

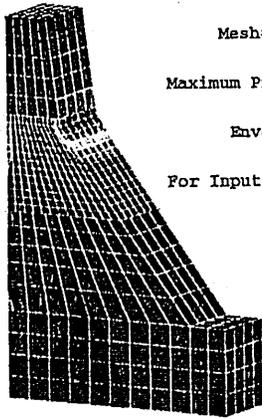
9.35 psi

Figure F6

ABAQUS

Response Spectrum Analysis

SP3	VALUE
	+6.20E-01
	+2.18E+00
	+3.74E+00
	+5.30E+00
	+6.85E+00
	+8.41E+00
	+9.97E+00
	+1.15E+01
	+1.31E+01
	+1.46E+01
	+1.62E+01
	+1.78E+01
	+1.93E+01
	+2.09E+01



Mesh#1

Maximum Principal Stress

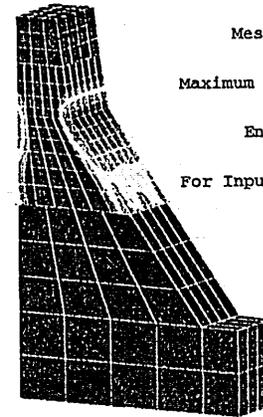
Envelope

For Input Record SHAKEA

ABAQUS

Response Spectrum Analysis

SP3	VALUE
	+4.91E-01
	+1.59E+00
	+2.68E+00
	+3.78E+00
	+4.88E+00
	+5.97E+00
	+7.07E+00
	+8.16E+00
	+9.26E+00
	+1.04E+01
	+1.15E+01
	+1.25E+01
	+1.36E+01
	+1.47E+01



Mesh#2

Maximum Principal Stress

Envelope

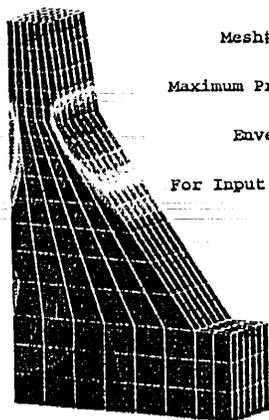
For Input Record SHAKEA

Figure F7

# ABAQUS

## Response Spectrum Analysis

SP3	VALUE
	+6.94E-01
	+1.71E+00
	+2.73E+00
	+3.74E+00
	+4.76E+00
	+5.78E+00
	+6.79E+00
	+7.81E+00
	+8.83E+00
	+9.84E+00
	+1.09E+01
	+1.19E+01
	+1.29E+01
	+1.39E+01

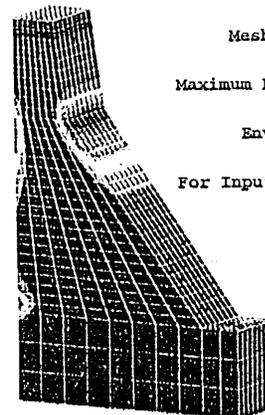


Mesh#3  
Maximum Principal Stress  
Envelope  
For Input Record SHAKEA

# ABAQUS

## Response Spectrum Analysis

SP3	VALUE
	+2.01E-01
	+1.44E+00
	+2.67E+00
	+3.90E+00
	+5.14E+00
	+6.37E+00
	+7.61E+00
	+8.84E+00
	+1.01E+01
	+1.13E+01
	+1.25E+01
	+1.38E+01
	+1.50E+01
	+1.62E+01

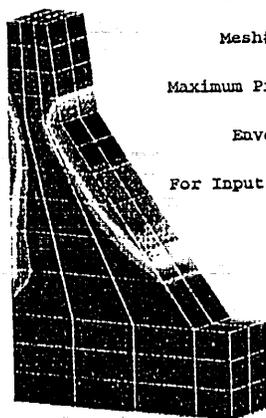


Mesh#4  
Maximum Principal Stress  
Envelope  
For Input Record SHAKEA

# ABAQUS

## Response Spectrum Analysis

SP3	VALUE
	+4.49E-01
	+1.10E+00
	+1.74E+00
	+2.39E+00
	+3.03E+00
	+3.68E+00
	+4.33E+00
	+4.97E+00
	+5.62E+00
	+6.27E+00
	+6.91E+00
	+7.56E+00
	+8.20E+00
	+8.85E+00

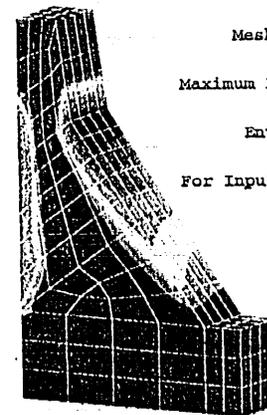


Mesh#5  
Maximum Principal Stress  
Envelope  
For Input Record SHAKEA

# ABAQUS

## Response Spectrum Analysis

SP3	VALUE
	+5.71E-01
	+1.20E+00
	+1.82E+00
	+2.45E+00
	+3.07E+00
	+3.70E+00
	+4.33E+00
	+4.95E+00
	+5.58E+00
	+6.20E+00
	+6.83E+00
	+7.46E+00
	+8.08E+00
	+8.71E+00

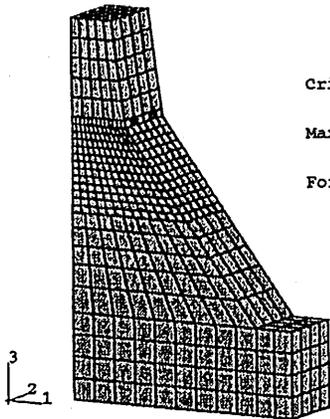


Mesh#6  
Maximum Principal Stress  
Envelope  
For Input Record SHAKEA

Figure F8

ABAQUS

Response Spectrum Analysis



Mesh#1

Critical Element #1366, 1369

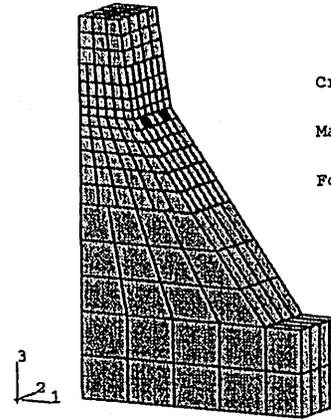
Maximum Principal Stress

For Input Record SHAKEB

227.60 psi

ABAQUS

Response Spectrum Analysis



Mesh#2

Critical Elements #120 & #123

Maximum Principal Stress

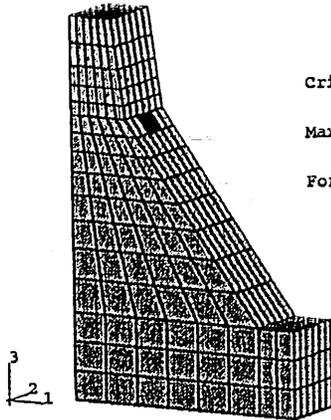
For Input Record SHAKEB

149 psi

Figure F9

# ABAQUS

## Response Spectrum Analysis



Mesh#3

Critical Element #282 & #330

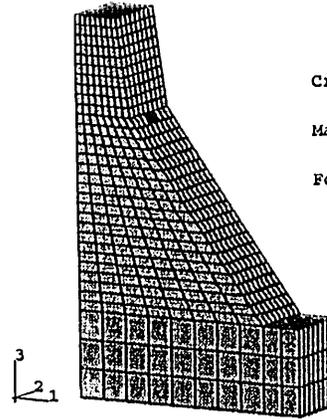
Maximum Principal Stress

For Input Record SHAKEB

143.20 psi

# ABAQUS

## Response Spectrum Analysis



Mesh#4

Critical Elements #1128 & #1288

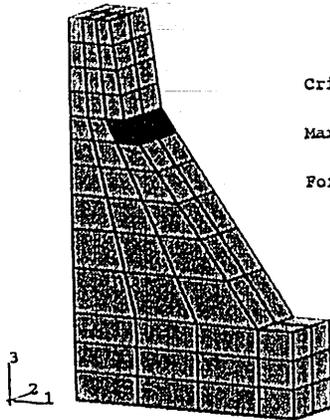
Maximum Principal Stress

For Input Record SHAKEB

168 psi

# ABAQUS

## Response Spectrum Analysis



Mesh#5

Critical Elements #27 & #45

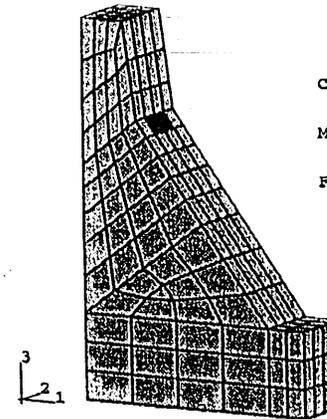
Maximum Principal Stress

For Input Record SHAKEB

88.98 psi

# ABAQUS

## Response Spectrum Analysis



Mesh#6

Critical Elements #74 & #75

Maximum Principal Stress

For Input Record SHAKEB

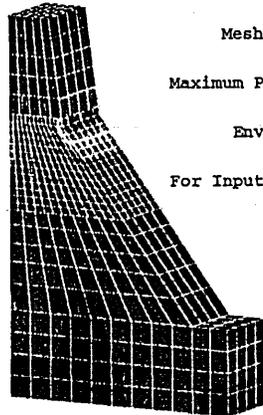
88 psi

Figure F10

ABAQUS

Response Spectrum Analysis

SP3	VALUE
	+6.22E+00
	+2.15E+01
	+3.69E+01
	+5.22E+01
	+6.75E+01
	+8.28E+01
	+9.81E+01
	+1.13E+02
	+1.29E+02
	+1.44E+02
	+1.59E+02
	+1.75E+02
	+1.90E+02
	+2.05E+02

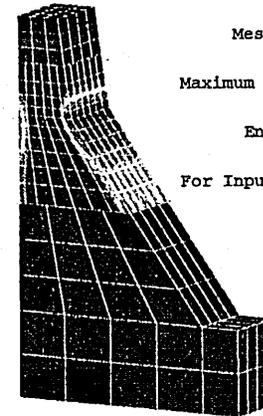


Mesh#1  
Maximum Principal Stress  
Envelope  
For Input Record SHAKEB

ABAQUS

Response Spectrum Analysis

SP3	VALUE
	+4.89E+00
	+1.56E+01
	+2.64E+01
	+3.71E+01
	+4.78E+01
	+5.86E+01
	+6.93E+01
	+8.01E+01
	+9.08E+01
	+1.02E+02
	+1.12E+02
	+1.23E+02
	+1.34E+02
	+1.44E+02



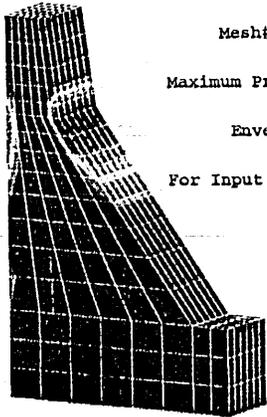
Mesh#2  
Maximum Principal Stress  
Envelope  
For Input Record SHAKEB

Figure f11

# ABAQUS

## Response Spectrum Analysis

SP3	VALUE
	+6.87E+00
	+1.69E+01
	+2.69E+01
	+3.69E+01
	+4.69E+01
	+5.69E+01
	+6.69E+01
	+7.69E+01
	+8.69E+01
	+9.69E+01
	+1.07E+02
	+1.17E+02
	+1.27E+02
	+1.37E+02

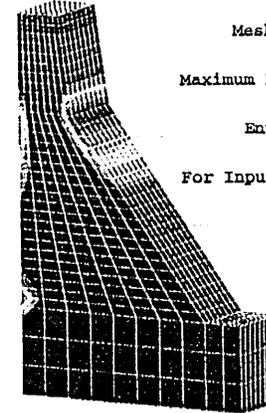


Mesh#3  
Maximum Principal Stress  
Envelope  
For Input Record SHAKEB

# ABAQUS

## Response Spectrum Analysis

SP3	VALUE
	+2.03E+00
	+1.43E+01
	+2.65E+01
	+3.87E+01
	+5.10E+01
	+6.32E+01
	+7.55E+01
	+8.77E+01
	+9.99E+01
	+1.12E+02
	+1.24E+02
	+1.37E+02
	+1.49E+02
	+1.61E+02

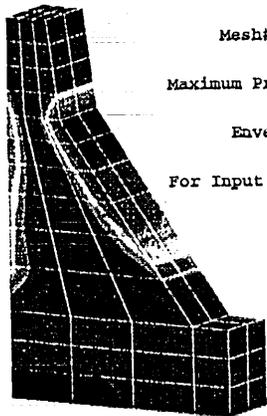


Mesh#4  
Maximum Principal Stress  
Envelope  
For Input Record SHAKEB

# ABAQUS

## Response Spectrum Analysis

SP3	VALUE
	+4.24E+00
	+1.03E+01
	+1.65E+01
	+2.26E+01
	+2.87E+01
	+3.48E+01
	+4.09E+01
	+4.70E+01
	+5.31E+01
	+5.92E+01
	+6.53E+01
	+7.14E+01
	+7.75E+01
	+8.36E+01

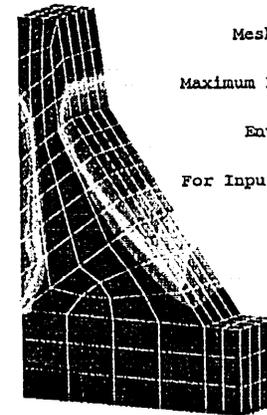


Mesh#5  
Maximum Principal Stress  
Envelope  
For Input Record SHAKEB

# ABAQUS

## Response Spectrum Analysis

SP3	VALUE
	+5.46E+00
	+1.14E+01
	+1.73E+01
	+2.32E+01
	+2.91E+01
	+3.51E+01
	+4.10E+01
	+4.69E+01
	+5.28E+01
	+5.87E+01
	+6.47E+01
	+7.06E+01
	+7.65E+01
	+8.24E+01



Mesh#6  
Maximum Principal Stress  
Envelope  
For Input Record SHAKEB

Figure F12

**Appendix G**  
**Sensitivity to Variation in**  
**Linear Elastic Material Properties**

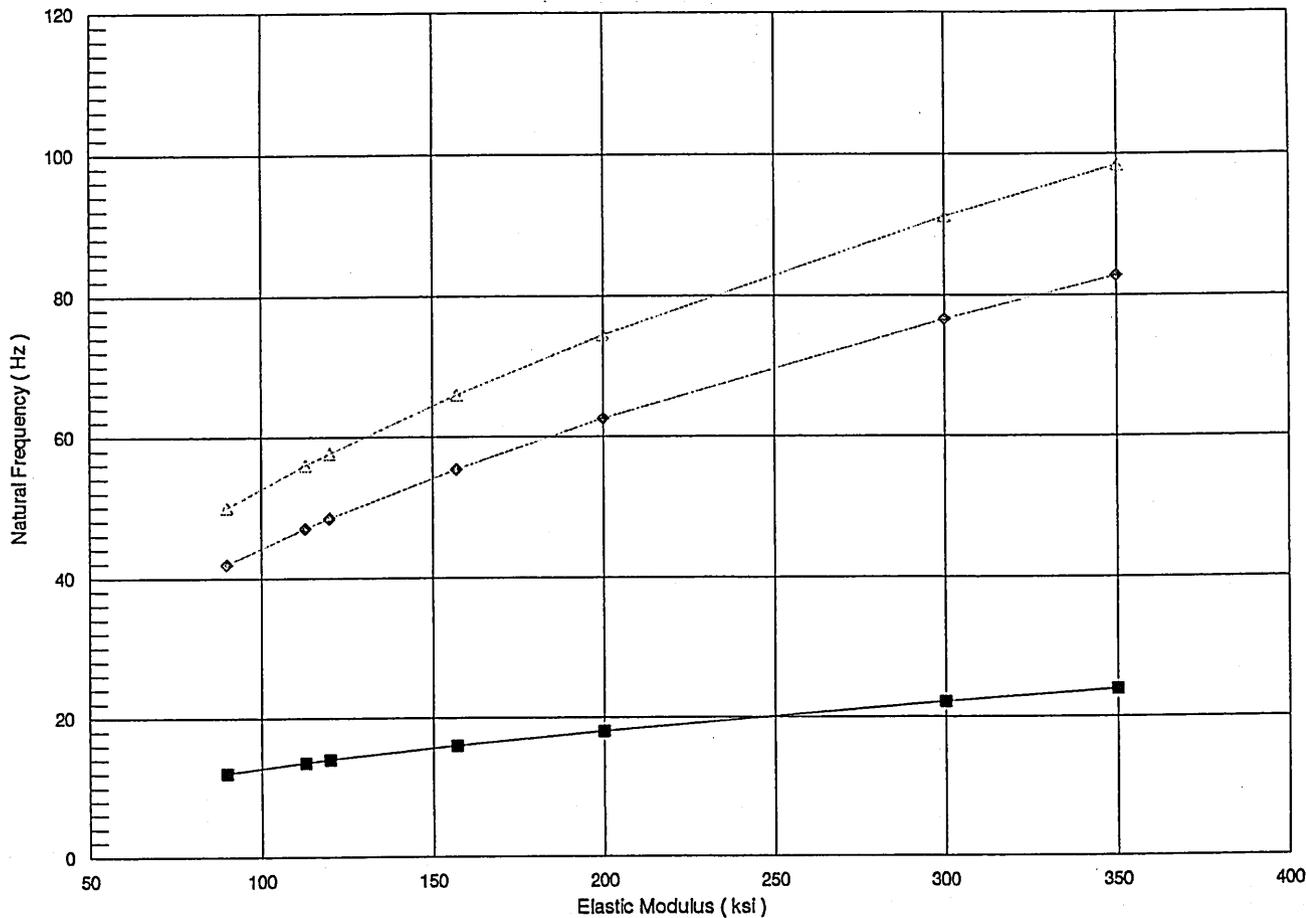
Uncracked Koyna Laboratory Study  
Sensitivity to Variation in Elastic Modulus  
Mesh#3

Material Properties

E = ( 90, 113, 120, 157, 200, 300, 350 ksi )  
Material Density = 138.2 pcf

Damping = 3.5% critical  
Rayleigh Damping Factors  
Alpha = 1.954769; Beta = .000248

**Natural Frequencies**  
Elastic Modulus Varied



Natural Frequencies (Hz)

Mode	90	113	120	157	200	300	350	LAB
1	12.1	13.6	14.0	16.0	18.0	22.2	23.9	18.0
2	23.2	26.0	26.8	30.6	34.6	42.4	45.7	24.0
3	41.9	47.0	48.4	55.4	62.5	76.6	82.7	30.0
4	49.9	55.9	57.6	65.9	74.4	91.1	98.4	
5	52.1	58.4	60.2	68.8	77.7	95.2	102.8	
6	53.8	60.2	62.1	71.0	80.1	98.1	106.0	
7	57.1	64.0	65.9	75.4	85.1	104.2	112.6	
8	57.8	64.8	66.8	76.4	86.2	105.6	114.0	
9	58.4	65.4	67.4	77.1	87.0	106.6	115.1	
10	59.5	66.7	68.7	78.6	88.7	108.7	117.4	

Figure g1

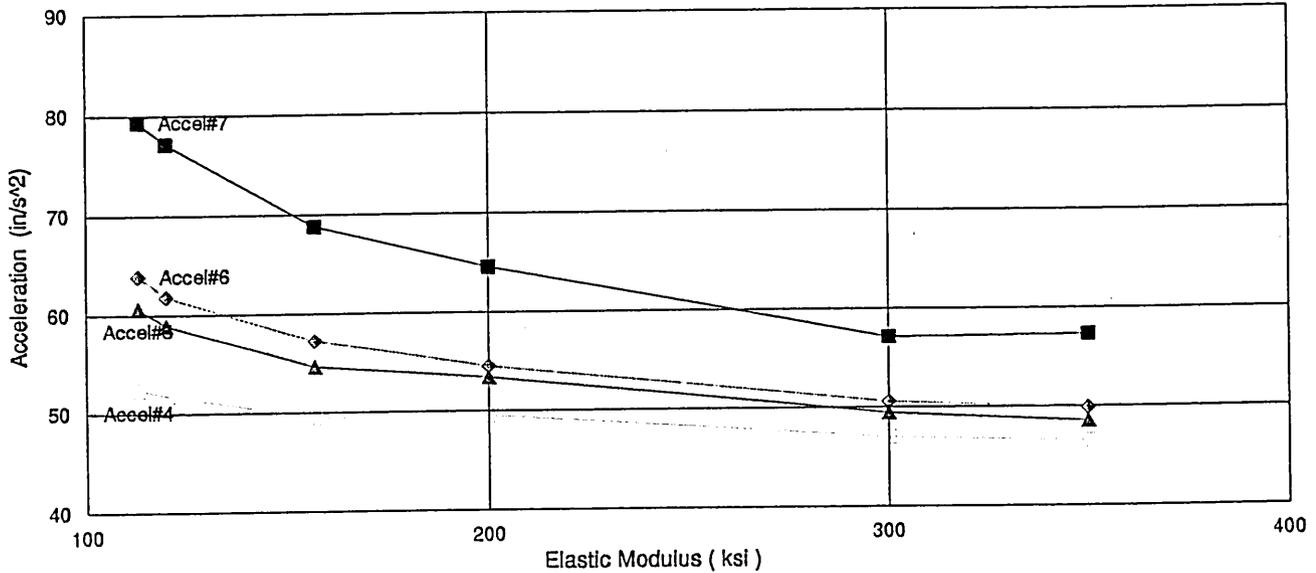
Uncracked Koyna Laboratory Study  
Sensitivity to Variation in Elastic Modulus  
Mesh#3

Material Properties

E = ( 113, 120, 157, 200, 300, 350 ksi )  
Material Density = 138.2 pcf

Damping = 3.5% critical  
Rayleigh Damping Factors  
Alpha = 1.954769; Beta = .000248

**Peak Accelerations**  
Elastic Modulus Varied



Peak Accelerations ( inch / sec ^ 2 )

	113	120	157	200	300	350	LAB
Accel#7	79.31	77.11	68.75	64.53	57.14	57.39	53.26
Accel#6	63.80	61.74	57.19	54.46	50.50	49.85	51.72
Accel#5	60.60	58.90	54.54	53.34	49.42	48.51	49.26
Accel#4	52.28	51.69	49.47	49.50	46.97	46.47	47.72

Figure g2

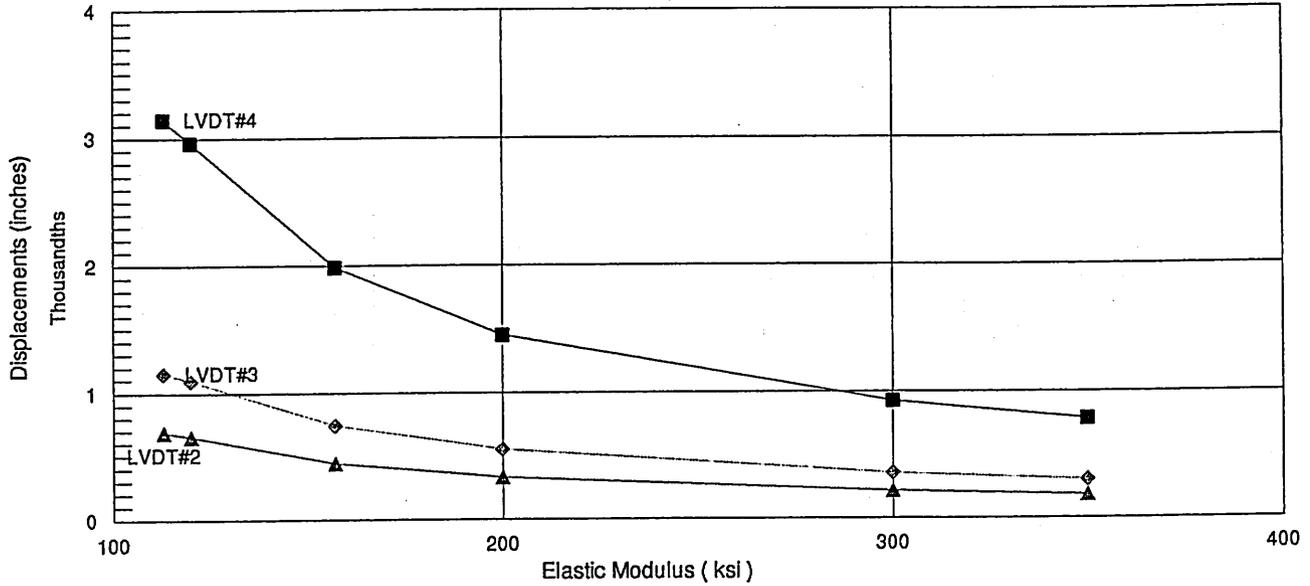
Uncracked Koyna Laboratory Study  
Sensitivity to Variation in Elastic Modulus  
Mesh#3

Material Properties

E = (113, 120, 157, 200, 300, 350 ksi)  
Material Density = 138.2 pcf

Damping = 3.5% critical  
Rayleigh Damping Factors  
Alpha = 1.954769; Beta = .000248

**Peak Displacements**  
Elastic Modulus Varied



Peak Displacements ( inches )

	113	120	157	200	300	350	LAB
LVDT#4	3.1E-03	3.0E-03	2.0E-03	1.5E-03	9.2E-04	7.8E-04	7.2E-04
LVDT#3	1.2E-03	1.1E-03	7.4E-04	5.5E-04	3.6E-04	3.0E-04	3.1E-04
LVDT#2	6.9E-04	6.5E-04	4.4E-04	3.3E-04	2.2E-04	1.8E-04	2.1E-04

Figure g3

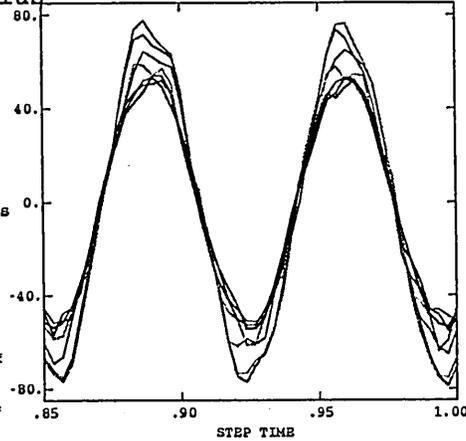
# ABAQUS

Elastic Modulus Varied

- E113\_176
- E120\_176
- E157\_176
- E200\_176
- E300\_176
- E350\_176
- LAB

Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model  
Acceleration  
at ACCEL#7

Modal Damping, 3.5%  
Material Density = 138 pcf  
Filename:SHAKEA  
Total Time : 279.75 to 280 sec



ABAQUS Modal Dynamic Analyses (E113 to E300) vs Laboratory Measurements (LAB)

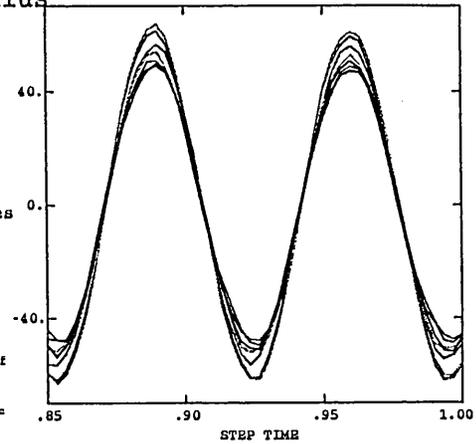
# ABAQUS

Elastic Modulus Varied

- E113\_204
- E120\_204
- E157\_204
- E200\_204
- E300\_204
- E350\_204
- LAB

Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model  
Acceleration  
at ACCEL#6

Modal Damping, 3.5%  
Material Density = 138 pcf  
Filename:SHAKEA  
Total Time : 279.75 to 280 sec



ABAQUS Modal Dynamic Analyses (E113 to E350) vs Laboratory Measurements (LAB)

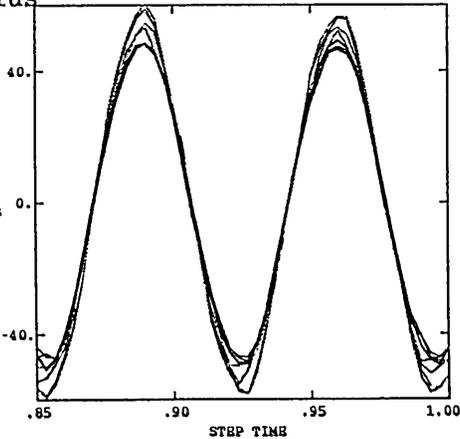
# ABAQUS

Elastic Modulus Varied

- E113\_491
- E120\_491
- E157\_491
- E200\_491
- E300\_491
- E350\_491
- LAB

Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model  
Acceleration  
at ACCEL#5

Modal Damping, 3.5%  
Material Density = 138 pcf  
Filename:SHAKEA  
Total Time : 279.75 to 280 sec



ABAQUS Modal Dynamic Analyses (E113 to E350) vs Laboratory Measurements (LAB)

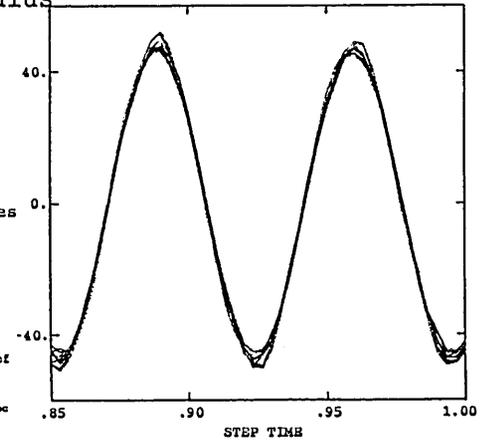
# ABAQUS

Elastic Modulus Varied

- E113\_519
- E120\_519
- E157\_519
- E200\_519
- E300\_519
- E350\_519
- LAB

Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model  
Acceleration  
at ACCEL#4

Modal Damping, 3.5%  
Material Density = 138 pcf  
Filename:SHAKEA  
Total Time : 279.75 to 280 sec



ABAQUS Modal Dynamic Analyses (E113 to E350) vs Laboratory Measurements (LAB)

# ABAQUS

Koyna Laboratory Model Study  
 Uncracked Model Study  
 Sensitivity Study  
 Variation of Elastic Modulus

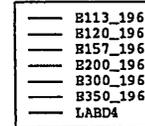
Comparison of Displacements  
 ABAQUS STANDARD  
 Modal Dynamic Analysis

Input Record SHAKEA  
 Modal Damping, 3.5%  
 Density = 138.2 pcf  
 Mesh # 3

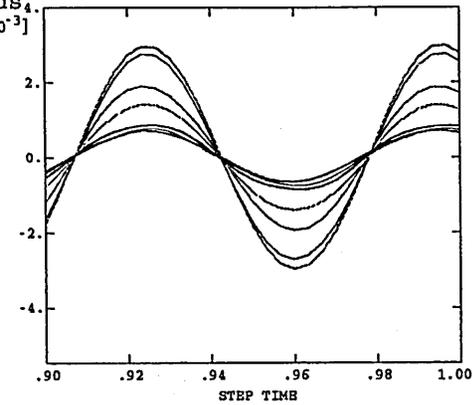


# ABAQUS

Elastic Modulus<sub>4</sub>  
 [ $\times 10^{-3}$ ]



Linear Elastic  
 Material Properties  
 STANDARD Analyses  
 Uncracked Model  
 Displacement  
 at LVDT#4

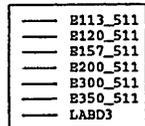


Total Time = 279.90 to 280 sec

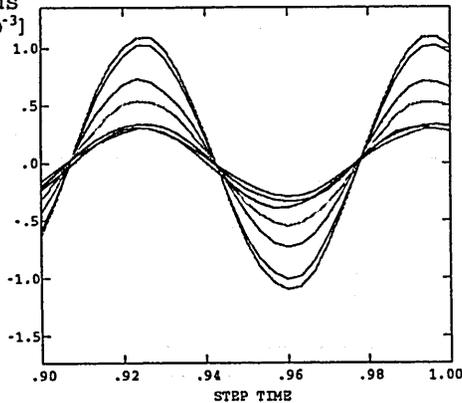
ABAQUS Modal Dynamic Analyses & Laboratory Measurements

# ABAQUS

Elastic Modulus  
 [ $\times 10^{-3}$ ]



Linear Elastic  
 Material Properties  
 STANDARD Analyses  
 Uncracked Model  
 Displacement  
 at LVDT#3

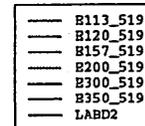


Total Time = 279.90 to 280 sec

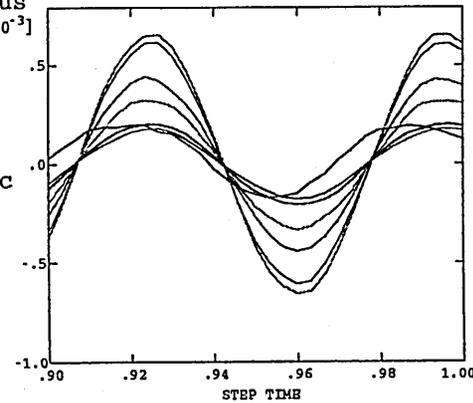
ABAQUS Modal Dynamic Analyses & Laboratory Measurements

# ABAQUS

Elastic Modulus  
 [ $\times 10^{-3}$ ]



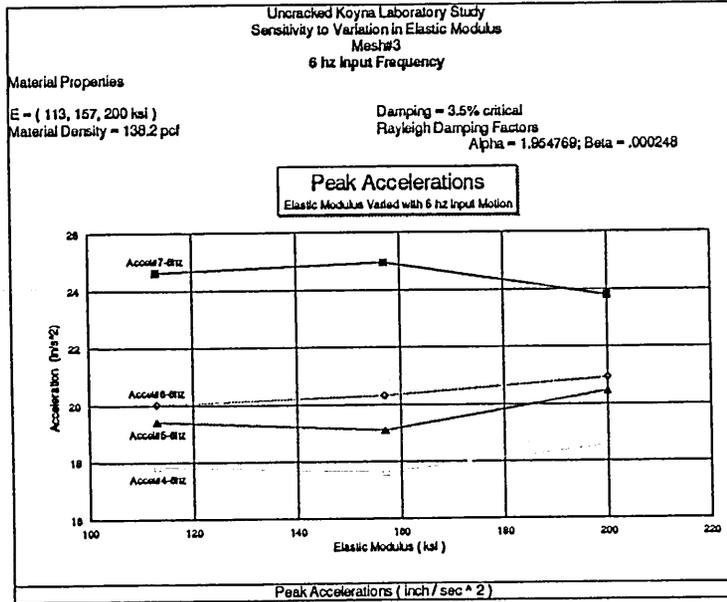
Linear Elastic  
 Material Properties  
 STANDARD Analyses  
 Uncracked Model  
 Acceleration  
 at LVDT#2



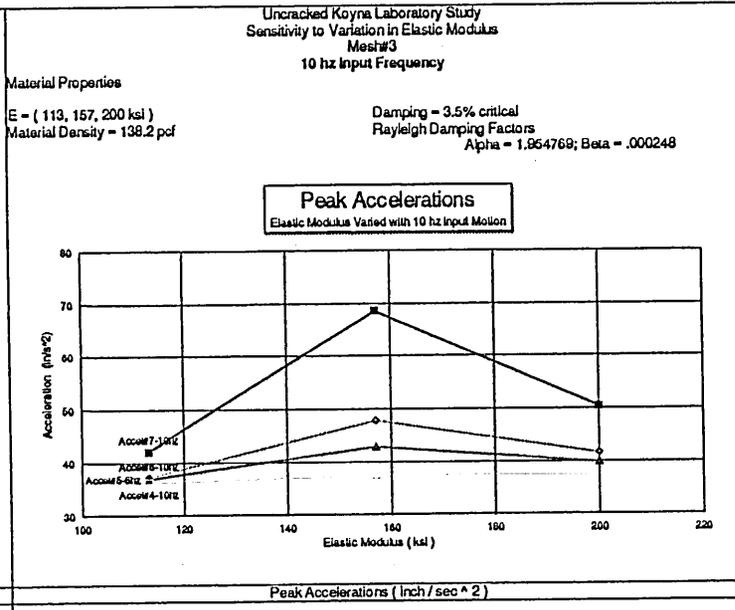
Total Time = 279.90 to 280 sec

ABAQUS Modal Dynamic Analyses & Laboratory Measurements

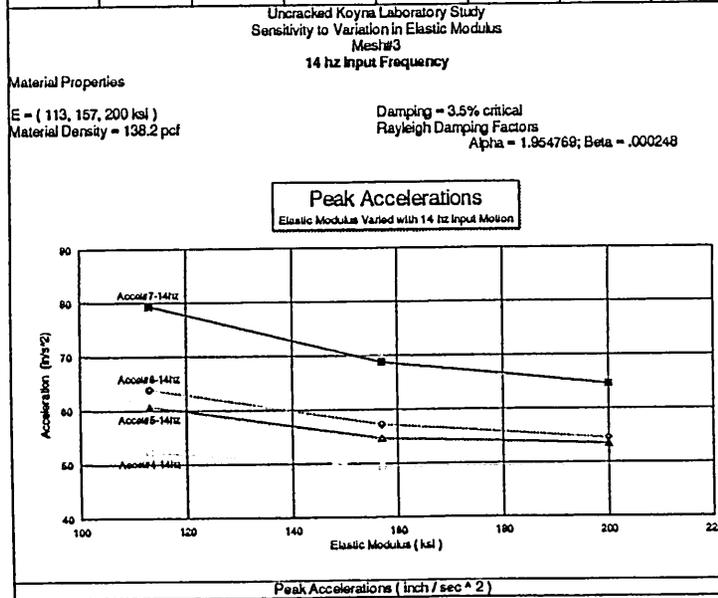
Figure 95



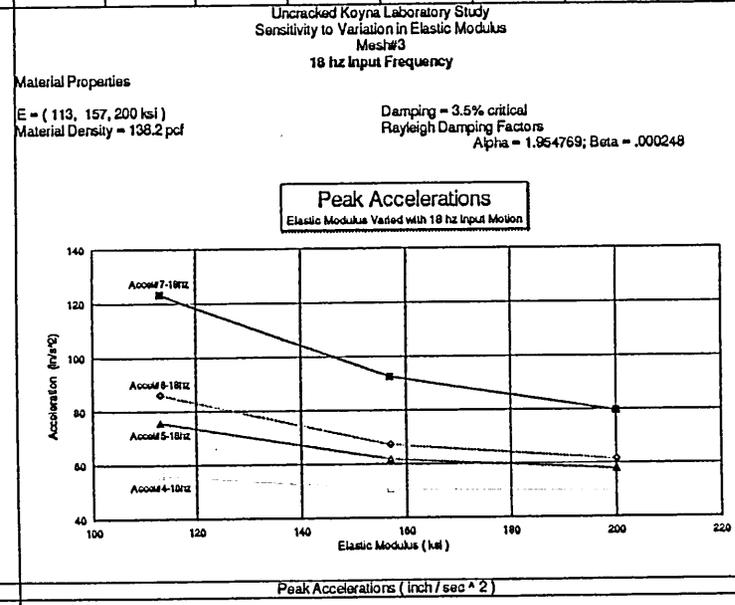
10 Hz Input Motion	113	157	200	Lab	10 Hz
Accel#7-6Hz	24.62	24.96	23.79	Accel#7-6Hz	17.55
Accel#6-6Hz	20.02	20.31	20.93	Accel#6-6Hz	17.86
Accel#5-6Hz	19.40	19.09	20.45	Accel#5-6Hz	16.93
Accel#4-6Hz	17.84	17.65	18.56	Accel#4-6Hz	17.24



10 Hz Input Motion	113	157	200	Lab	10 Hz
Accel#7-10Hz	42.15	68.45	60.39	Accel#7-10Hz	37.87
Accel#6-10Hz	37.18	47.84	41.61	Accel#6-10Hz	36.94
Accel#5-10Hz	36.79	42.87	39.70	Accel#5-10Hz	35.4
Accel#4-10Hz	36.27	37.47	37.50	Accel#4-10Hz	36.02

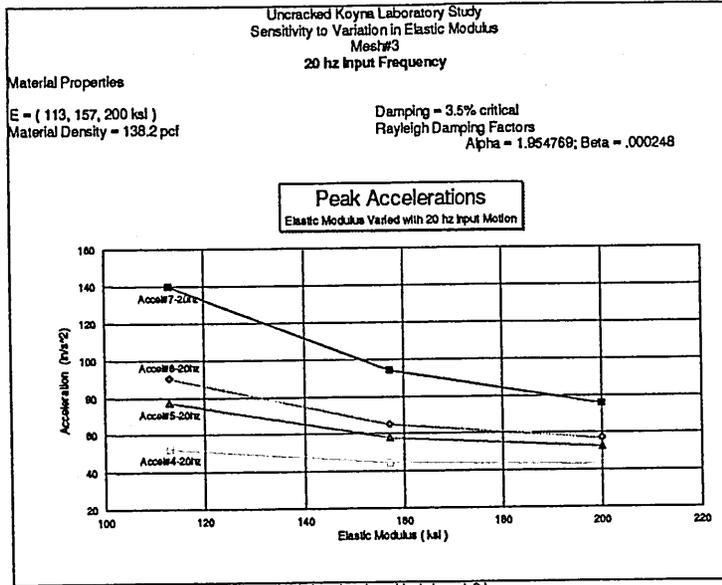


14 Hz Input Motion	113	157	200	Lab	14 Hz
Accel#7-14Hz	79.31	68.75	64.53	Accel#7-14Hz	53.26
Accel#6-14Hz	63.80	57.19	54.46	Accel#6-14Hz	50.72
Accel#5-14Hz	60.60	54.54	53.34	Accel#5-14Hz	49.26
Accel#4-14Hz	52.28	49.47	49.5	Accel#4-14Hz	47.72



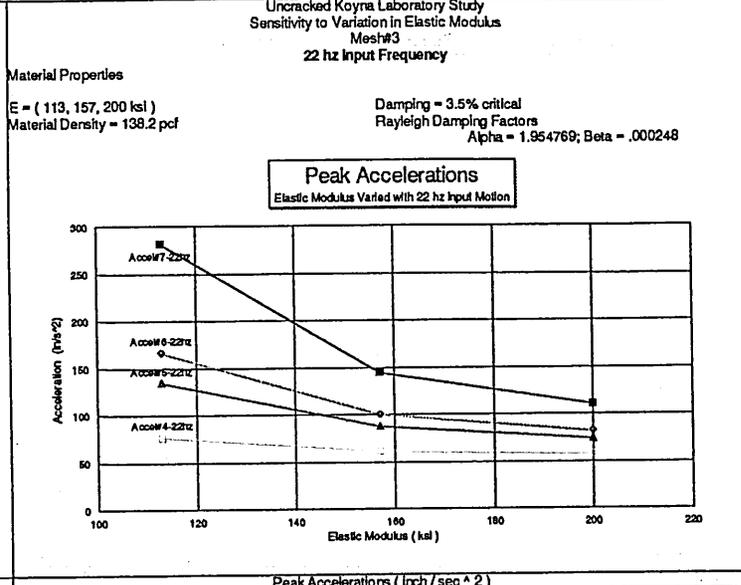
18 Hz Input Motion	113	157	200	Lab	18 Hz
Accel#7-18Hz	123.2	92.43	79.49	Accel#7-18Hz	28.94
Accel#6-18Hz	85.88	67.23	61.48	Accel#6-18Hz	32.62
Accel#5-18Hz	75.55	61.65	57.8	Accel#5-18Hz	35.71
Accel#4-18Hz	58.15	50.82	49.95	Accel#4-18Hz	40.02

Figure g6



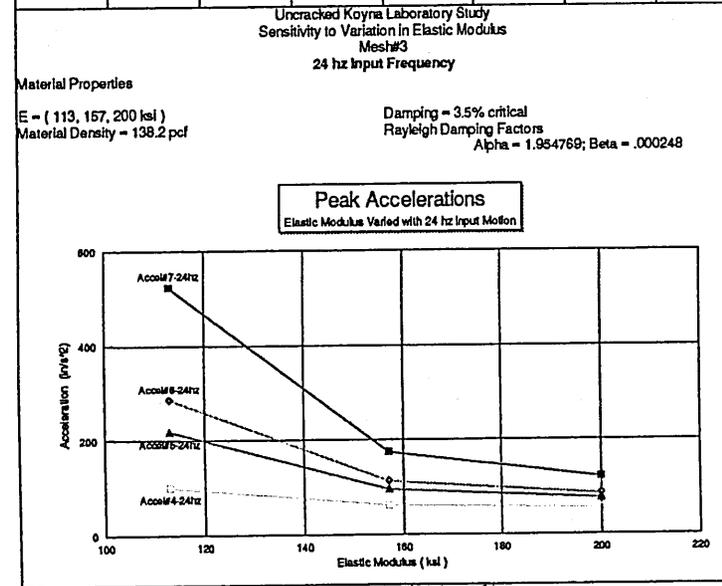
Peak Accelerations ( Inch / sec ^ 2 )

20 hz Input	Motion	113	157	200	Lab	20 hz
	Accel#7-20hz	139.80	94.03	75.55	Accel#7-20hz	65.26
	Accel#6-20hz	90.25	65.09	57.14	Accel#6-20hz	57.57
	Accel#5-20hz	77.07	57.65	52.66	Accel#5-20hz	51.1
	Accel#4-20hz	52.48	44.84	43.31	Accel#4-20hz	44.84



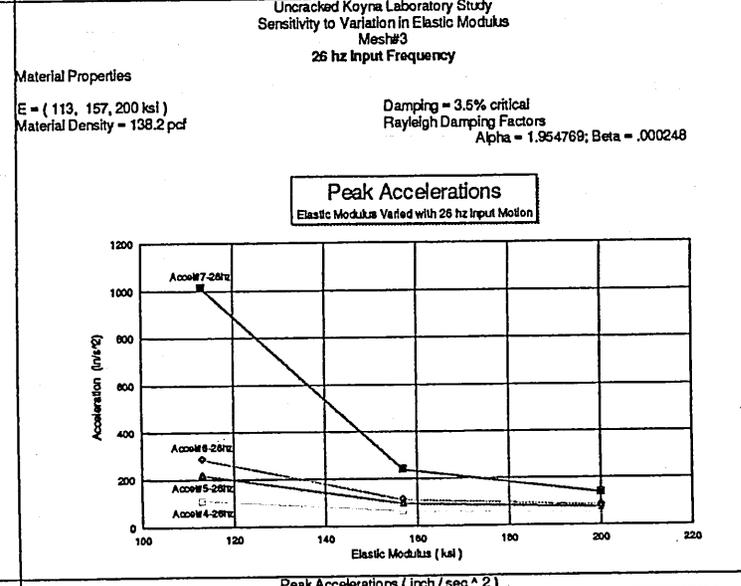
Peak Accelerations ( Inch / sec ^ 2 )

22 hz Input	Motion	113	157	200	Lab	22 hz
	Accel#7-22hz	281.60	144.20	110.20	Accel#7-22hz	65.57
	Accel#6-22hz	166.30	100.10	82.04	Accel#6-22hz	60.03
	Accel#5-22hz	134.40	87.09	73.59	Accel#5-22hz	55.72
	Accel#4-22hz	77.24	61.90	57.66	Accel#4-22hz	52.33



Peak Accelerations ( Inch / sec ^ 2 )

24 hz Input Motion	113	157	200	Lab	24 hz
Accel#7-24hz	523.00	174.50	121.4	Accel#7-24hz	97.59
Accel#6-24hz	285.30	112.60	85.59	Accel#6-24hz	79.42
Accel#5-24hz	217.90	95.42	75.81	Accel#5-24hz	68.96
Accel#4-24hz	100.50	82.95	56.31	Accel#4-24hz	57.88



Peak Accelerations ( Inch / sec ^ 2 )

26 hz	113	157	200	Lab	26 hz
Accel#7-26hz	1013	238.6	137.9	Accel#7-26hz	97.59
Accel#6-26hz	285.3	112.6	85.59	Accel#6-26hz	79.42
Accel#5-26hz	217.9	95.42	75.81	Accel#5-26hz	68.96
Accel#4-26hz	111.4	65.02	54.3	Accel#4-26hz	57.88

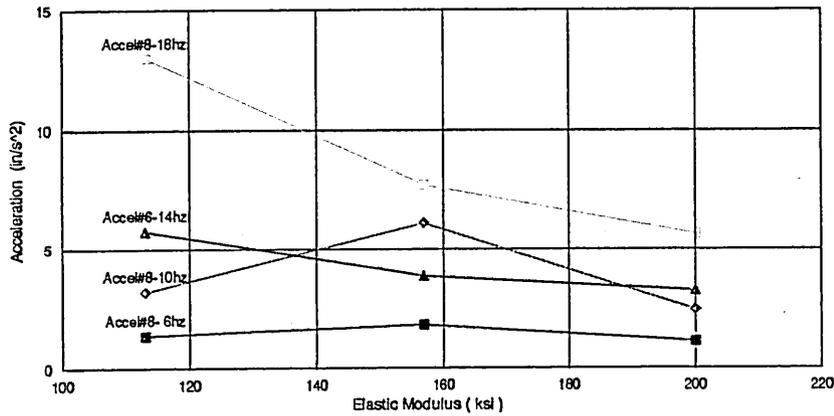
Figure 97

Uncracked Koyna Laboratory Study  
Sensitivity to Variation in Elastic Modulus  
Mesh#3  
6, 10, 14, 18 Hz Input Frequency  
Vertical Accelerations

Material Properties  
E = ( 113, 157, 200 ksi )  
Material Density = 138.2 pcf

Damping = 3.5% critical  
Rayleigh Damping Factors  
Alpha = 1.954769; Beta = .000248

**Peak Vertical Accelerations**  
6, 10, 14, 18 Hz Input Motions



Peak Accelerations ( Inch / sec ^ 2 )

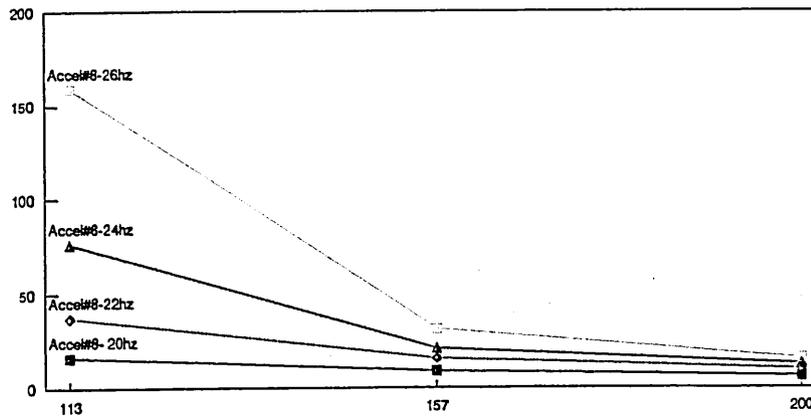
Motion	113	157	200	Lab	
Accel#8- 6hz	1.356	1.791	1.096	Accel#8-6hz	3.694
Accel#8- 10hz	3.18	6.07	2.45	Accel#8-10hz	6.773
Accel#6- 14hz	5.73	3.87	3.23	Accel#6-14hz	11.08
Accel#8- 18hz	12.97	7.66	5.62	Accel#8-18hz	76.96

Uncracked Koyna Laboratory Study  
Sensitivity to Variation in Elastic Modulus  
Mesh#3  
20, 22, 24, 26 Hz Input Frequency  
Vertical Accelerations

Material Properties  
E = ( 113, 157, 200 ksi )  
Material Density = 138.2 pcf

Damping = 3.5% critical  
Rayleigh Damping Factors  
Alpha = 1.954769; Beta = .000248

**Peak Vertical Accelerations**  
20, 22, 24, 26 Hz Input Motions



Peak Accelerations ( Inch / sec ^ 2 )

Motion	113	157	200	Lab	
Accel#8- 20hz	16.38	8.679	5.977	Accel#8-6hz	33.86
Accel#8- 22hz	37.06	15.66	10.00	Accel#8-10hz	18.47
Accel#6- 24hz	78.13	21.01	12.52	Accel#6-14hz	18.78
Accel#8- 26hz	158.70	31.27	15.63	Accel#8-18hz	10.78

Figure g8

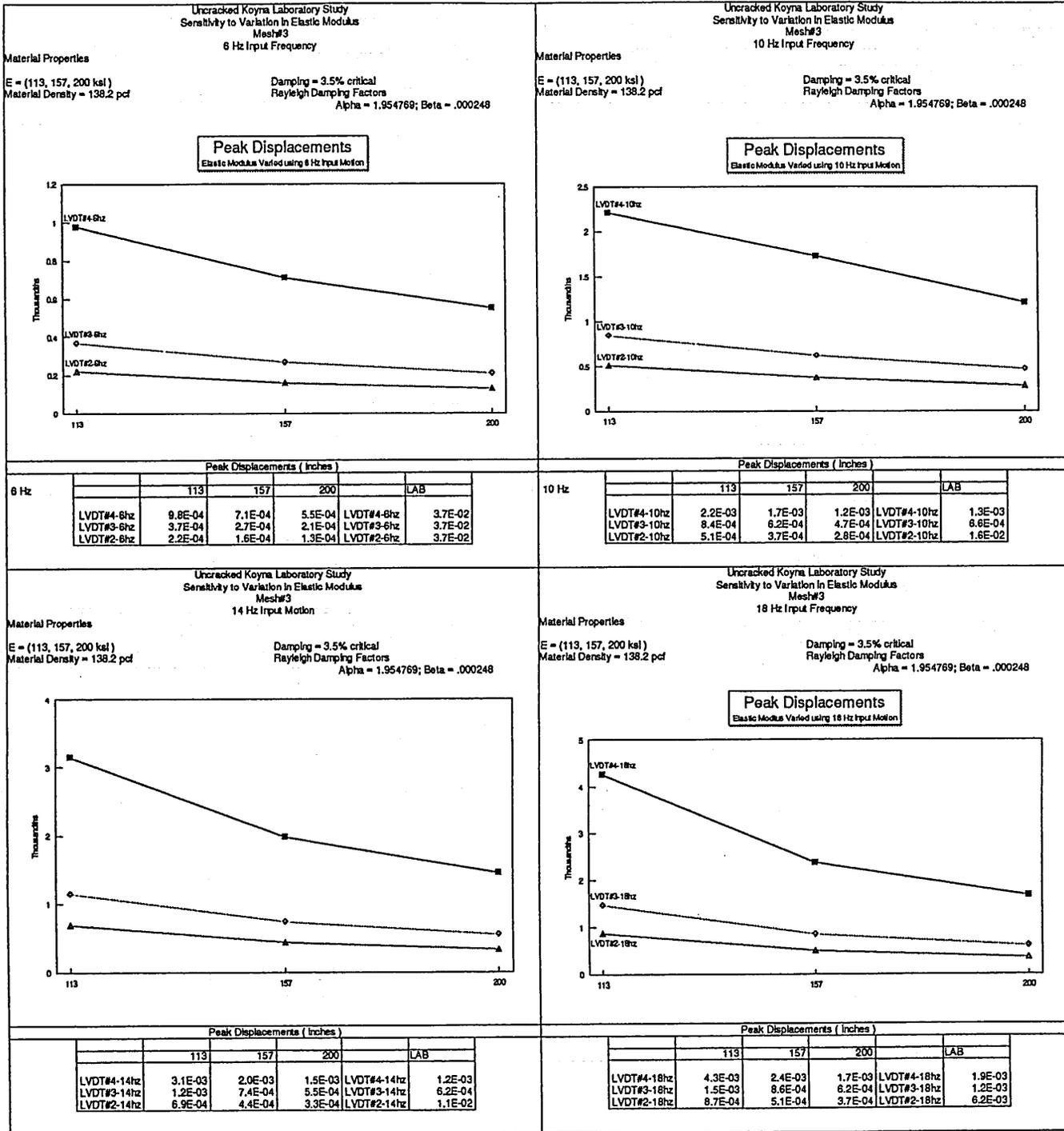
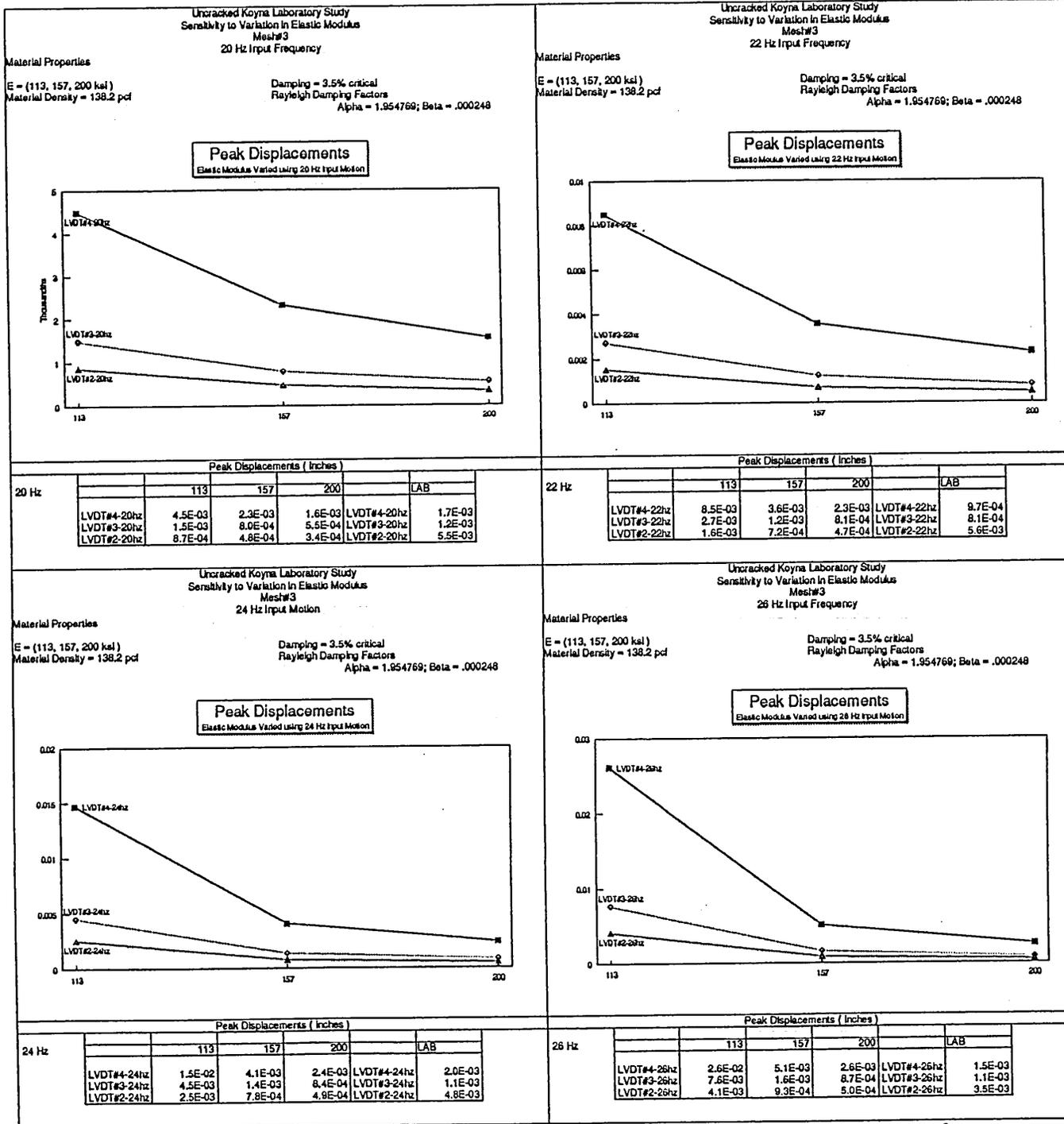
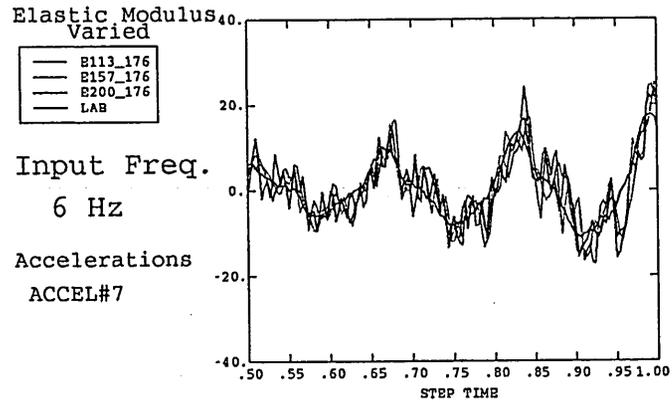


Figure 99

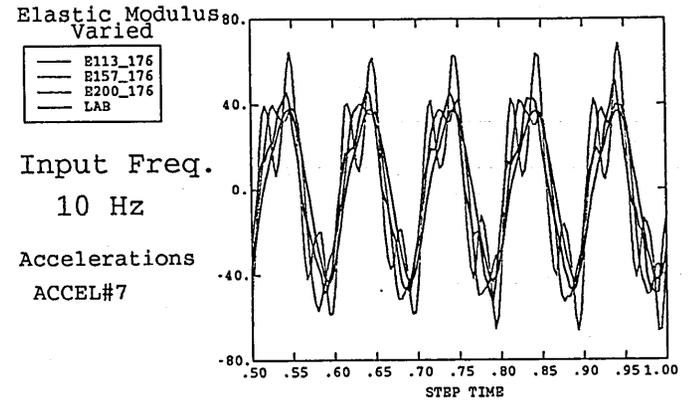
Figure g10



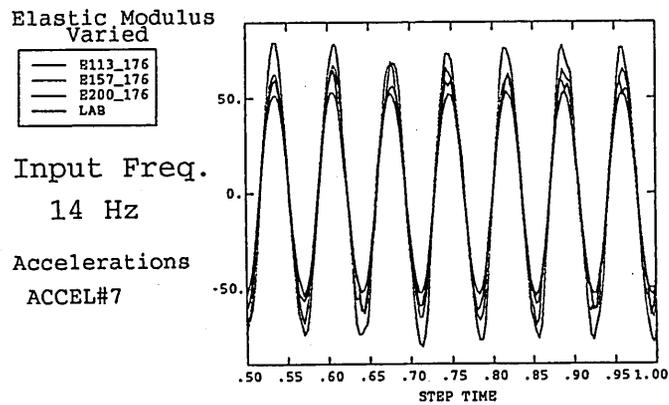
# ABAQUS



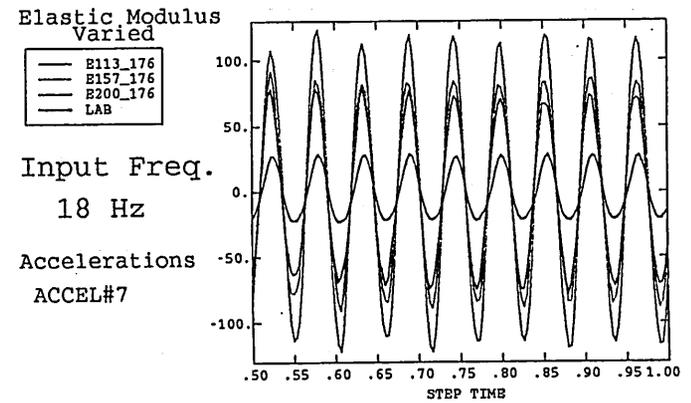
# ABAQUS



# ABAQUS

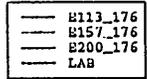


# ABAQUS

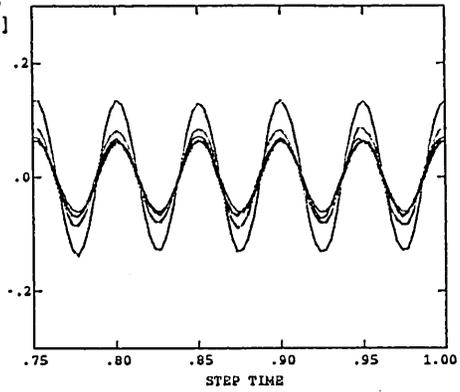


# ABAQUS

Elastic Modulus Varied [ $\times 10^3$ ]

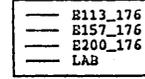


Input Freq.  
20 Hz  
Accelerations  
ACCEL#7

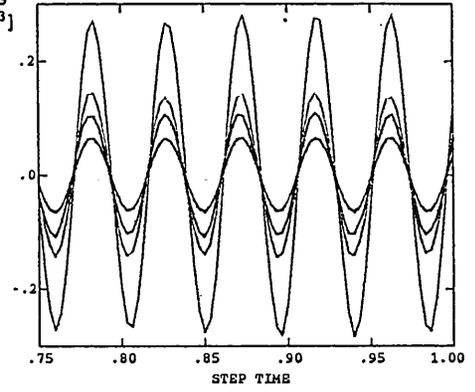


# ABAQUS

Elastic Modulus Varied [ $\times 10^3$ ]

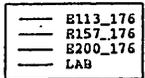


Input Freq.  
22 Hz  
Accelerations  
ACCEL#7

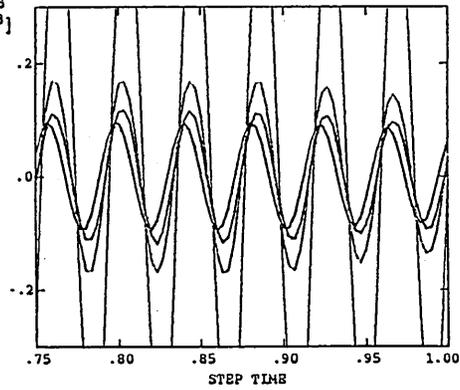


# ABAQUS

Elastic Modulus Varied [ $\times 10^3$ ]

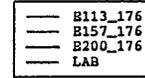


Input Freq.  
24 Hz  
Accelerations  
ACCEL#7

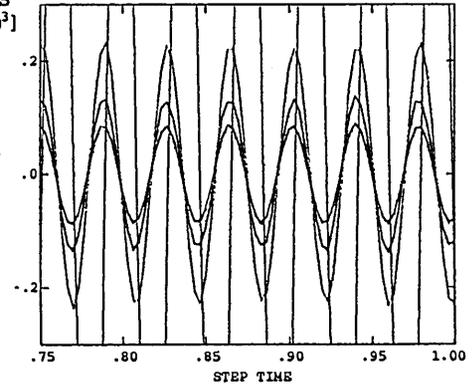


# ABAQUS

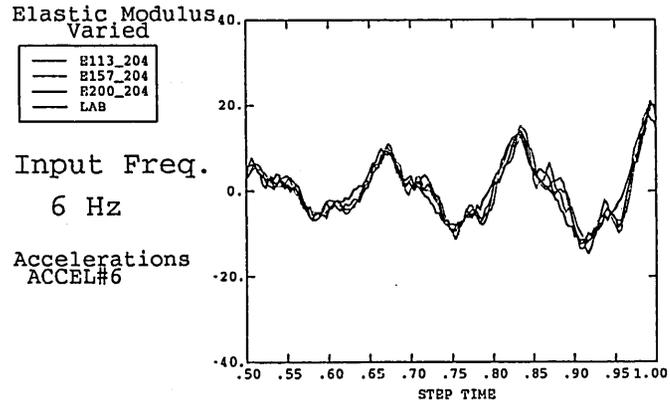
Elastic Modulus Varied [ $\times 10^3$ ]



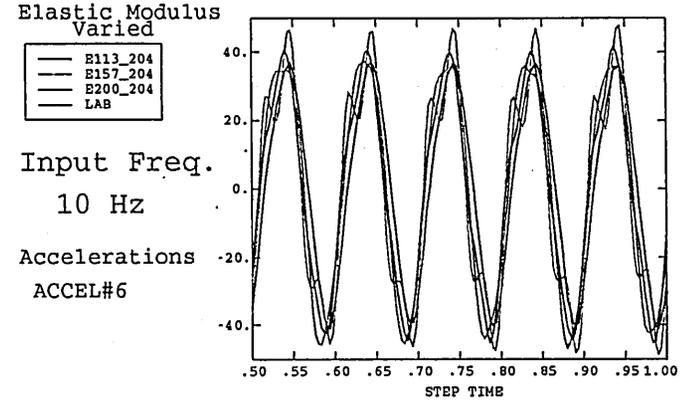
Input Freq.  
26 Hz  
Accelerations  
ACCEL#7



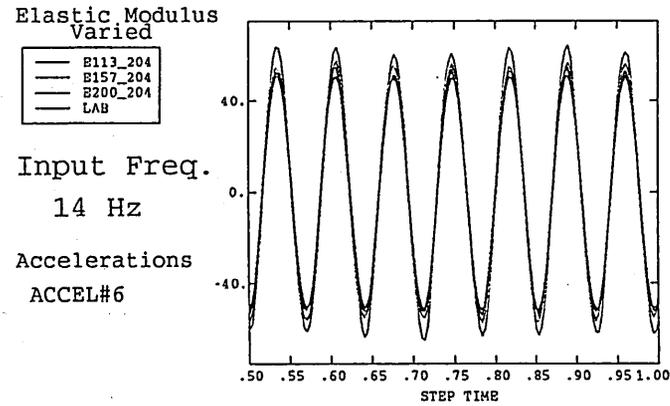
# ABAQUS



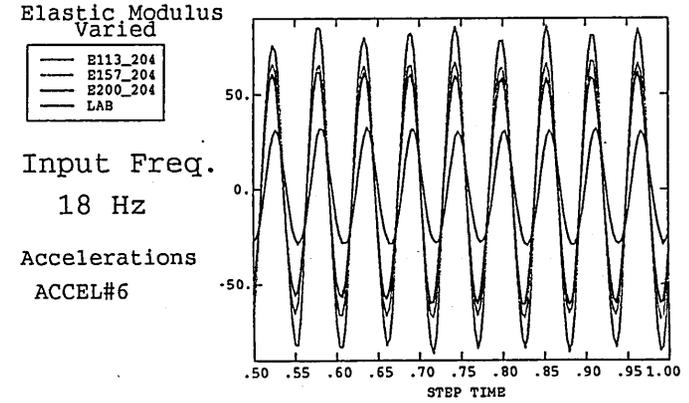
# ABAQUS



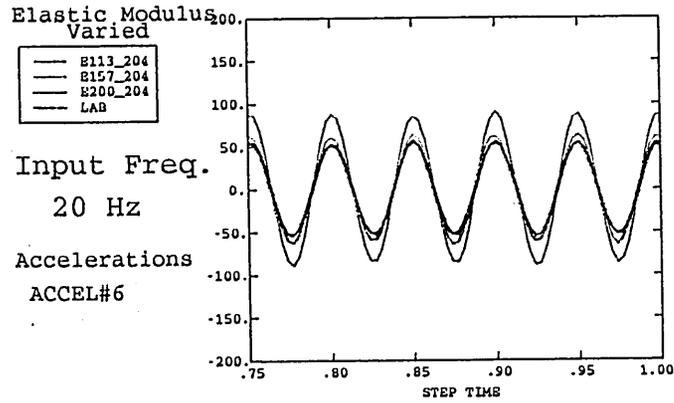
# ABAQUS



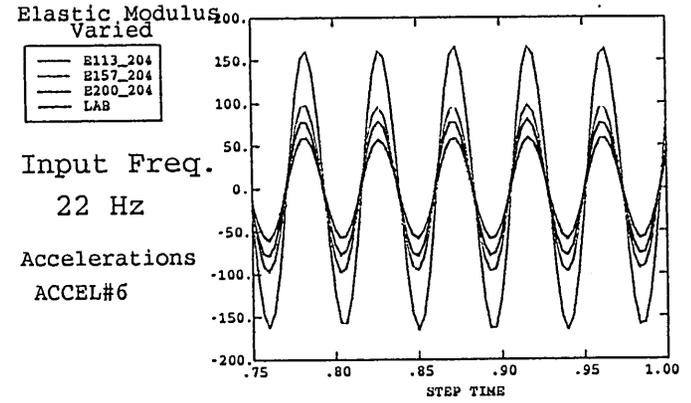
# ABAQUS



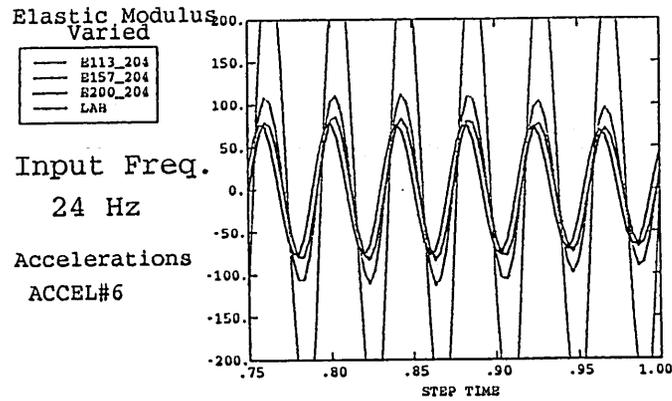
# ABAQUS



# ABAQUS



# ABAQUS



# ABAQUS

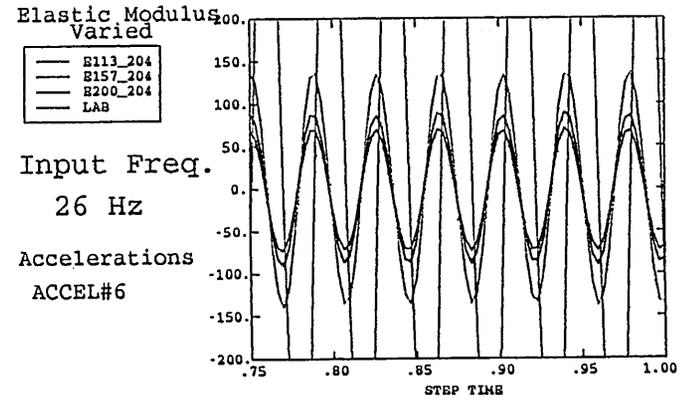
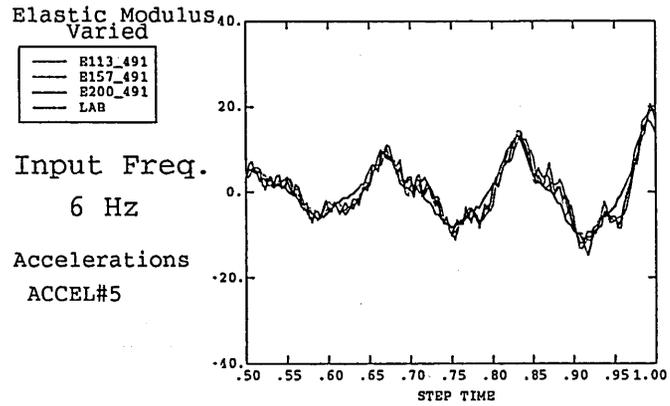
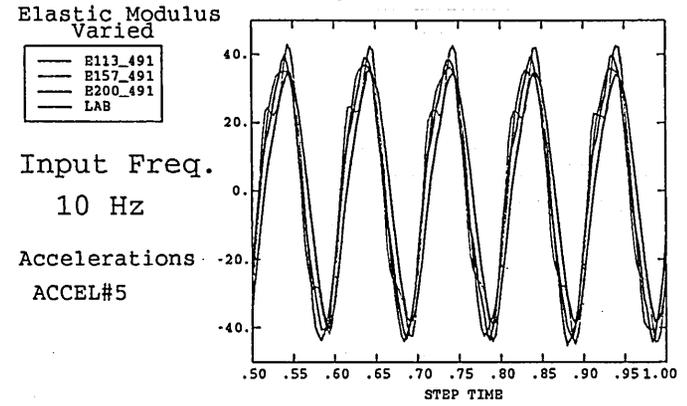


Figure g14

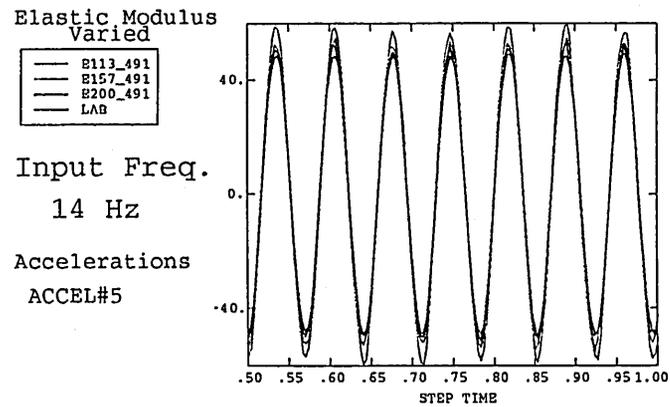
# ABAQUS



# ABAQUS



# ABAQUS



# ABAQUS

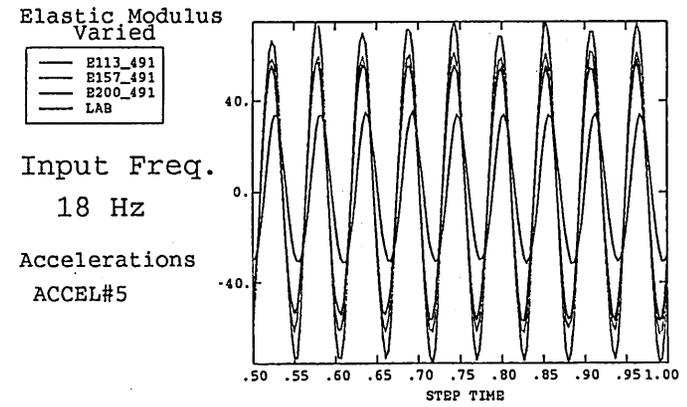
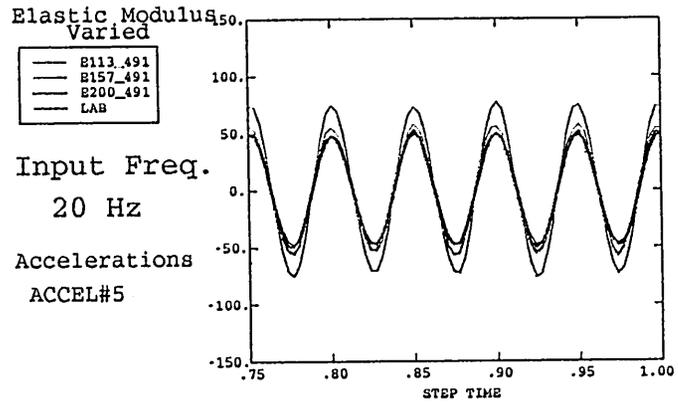
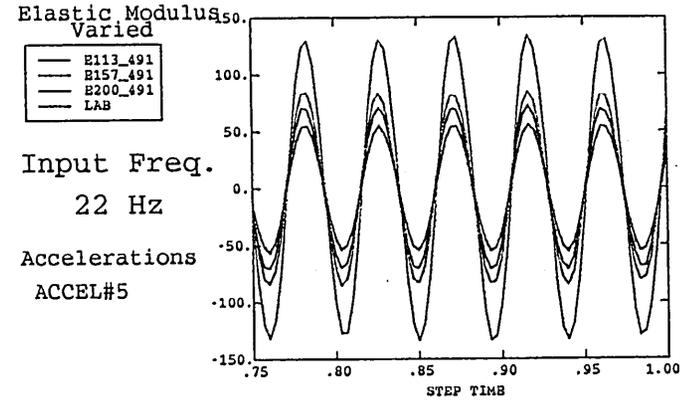


Figure g15

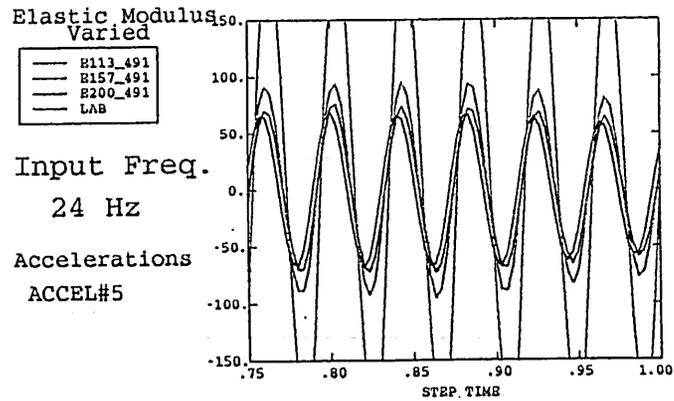
# ABAQUS



# ABAQUS



# ABAQUS



# ABAQUS

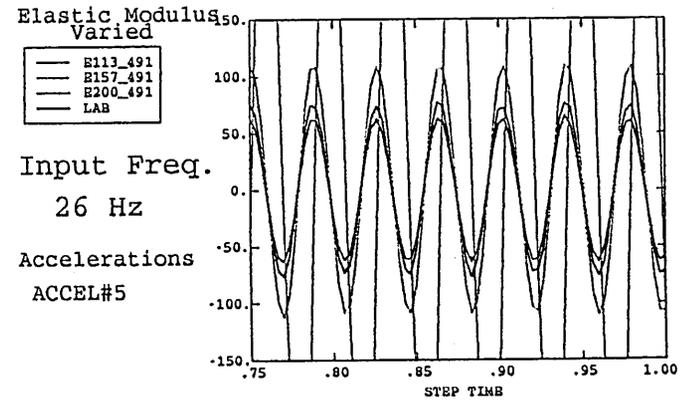
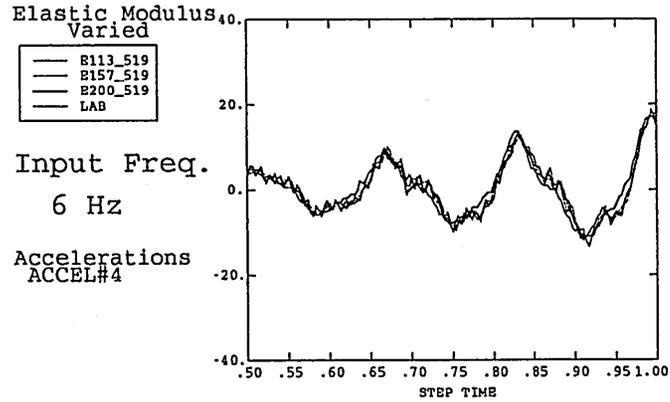
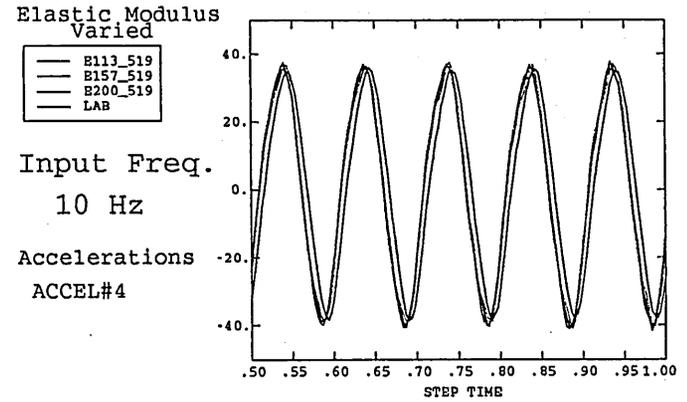


Figure g16

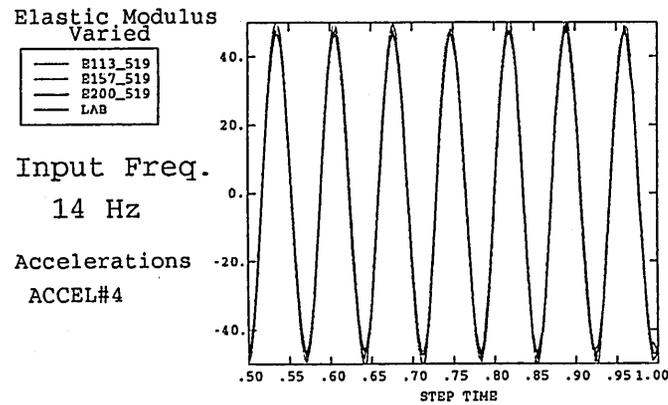
# ABAQUS



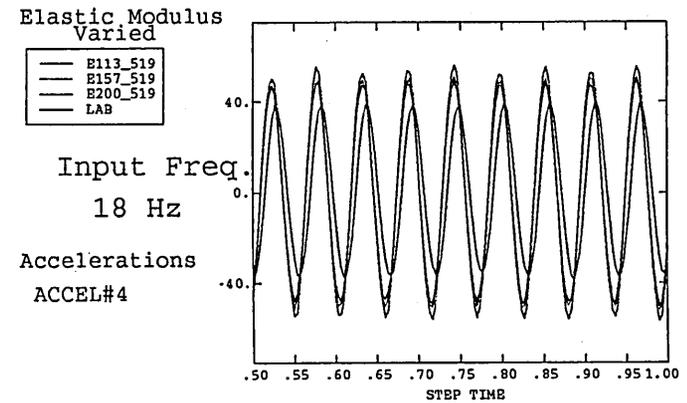
# ABAQUS



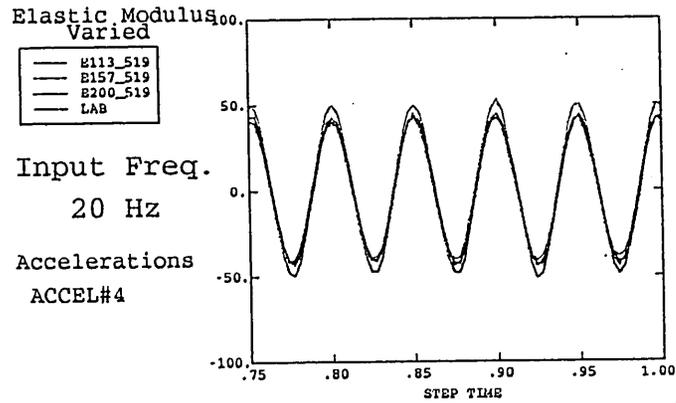
# ABAQUS



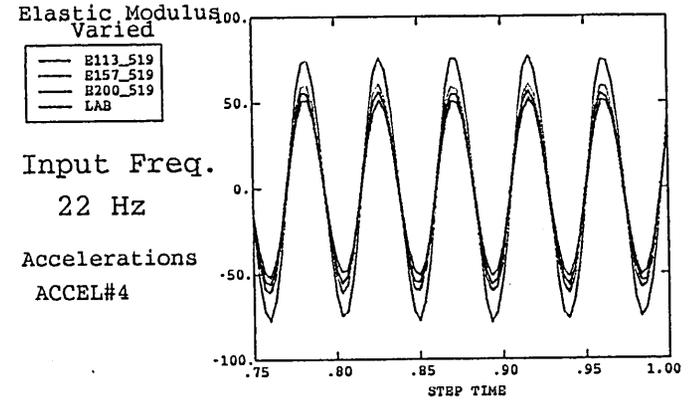
# ABAQUS



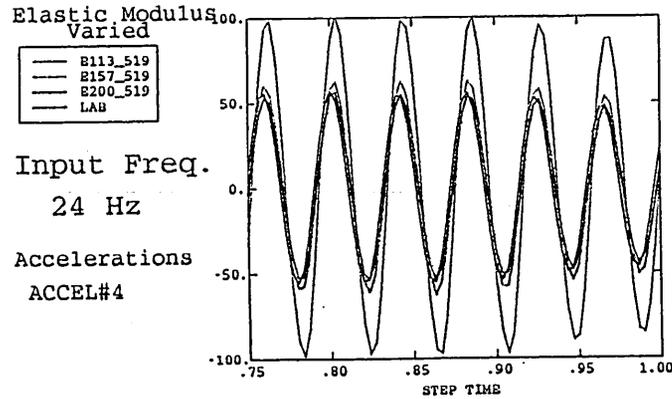
# ABAQUS



# ABAQUS



# ABAQUS



# ABAQUS

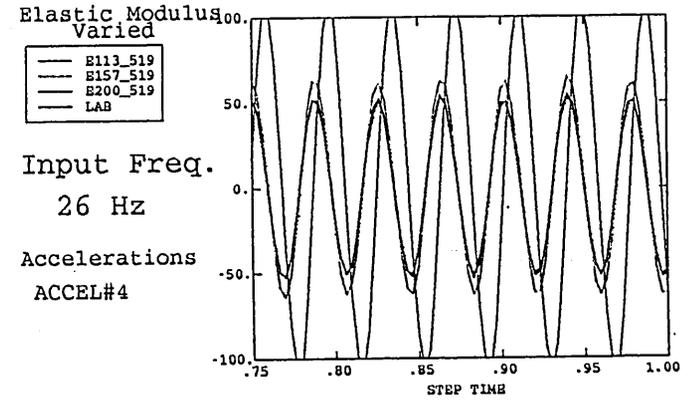
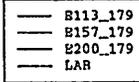


Figure g18

# ABAQUS

Elastic Modulus  
Varied

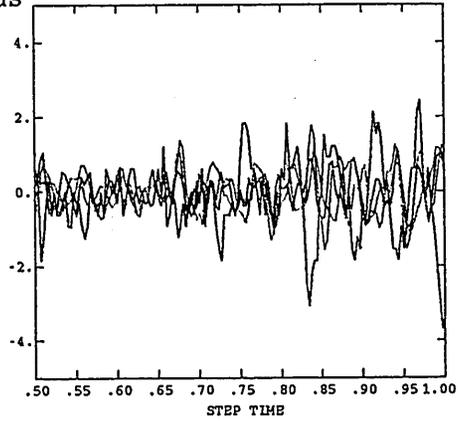


Input Freq.

6 Hz

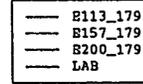
Accelerations

ACCEL#8



# ABAQUS

Elastic Modulus  
Varied

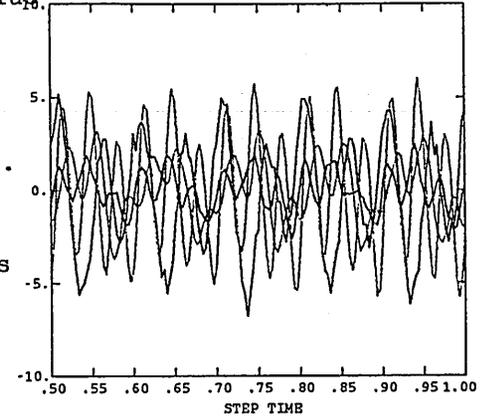


Input Freq.

10 Hz

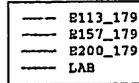
Accelerations

ACCEL#8



# ABAQUS

Elastic Modulus  
Varied

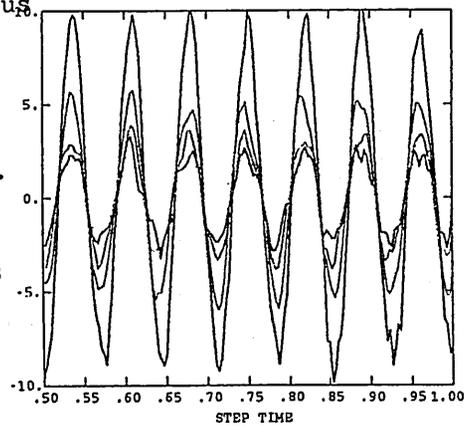


Input Freq.

14 Hz

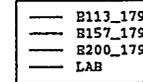
Accelerations

ACCEL#8



# ABAQUS

Elastic Modulus  
Varied



Input Freq.

18 Hz

Accelerations

ACCEL#8

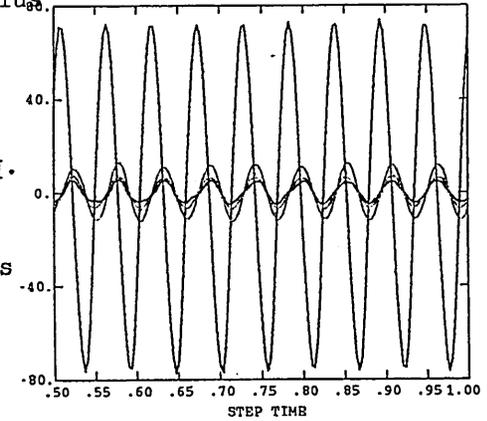
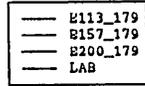


Figure g19

# ABAQUS

Elastic Modulus  
Varied

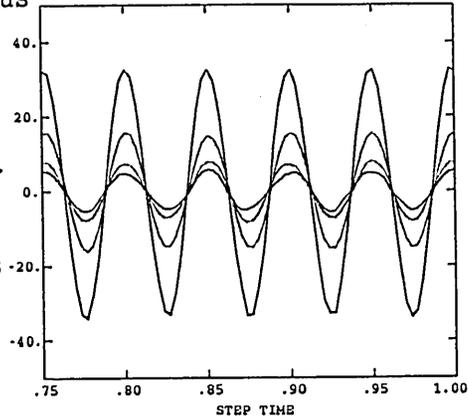


Input Freq.

20 Hz

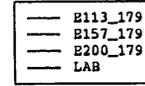
Accelerations

ACCEL#8



# ABAQUS

Elastic Modulus  
Varied

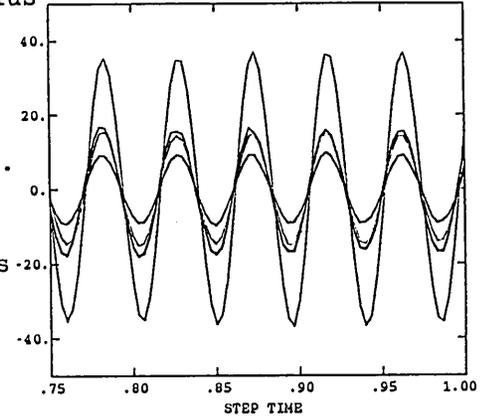


Input Freq.

22 Hz

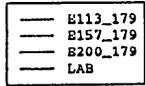
Accelerations

ACCEL#8



# ABAQUS

Elastic Modulus  
Varied

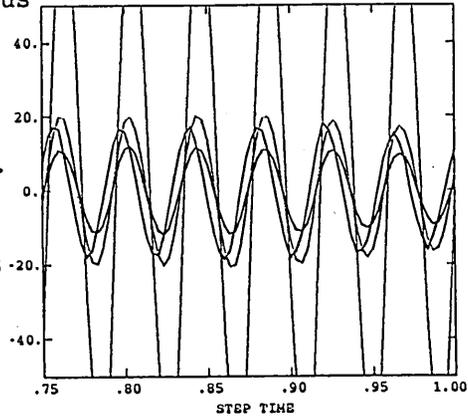


Input Freq.

24 Hz

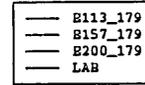
Accelerations

ACCEL#8



# ABAQUS

Elastic Modulus  
Varied

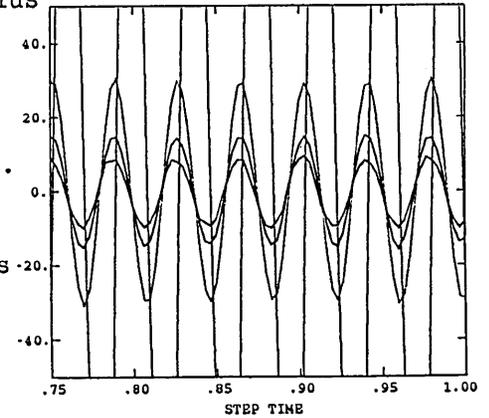


Input Freq.

26 Hz

Accelerations

ACCEL#8



# ABAQUS

Koyna Laboratory Model Study  
 Uncracked Model Study  
 Sensitivity Study  
 Variation of Elastic Modulus

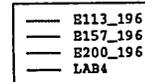
At Diff. Input Frequencies  
 Comparison of Displacements  
 Dynamic Analysis

Input Record SHAKEA  
 Mesh # 3



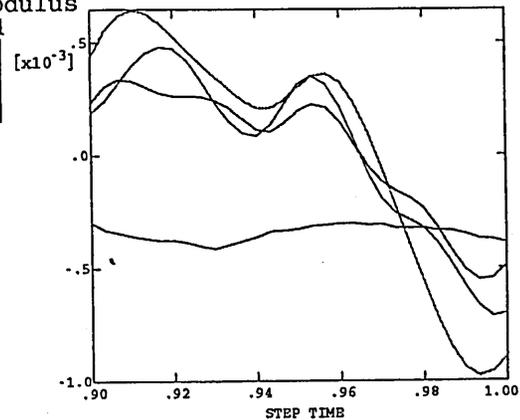
# ABAQUS

Elastic Modulus  
 Varied



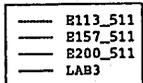
Input Freq.  
 6 hz

Displacement  
 at LVDT#4



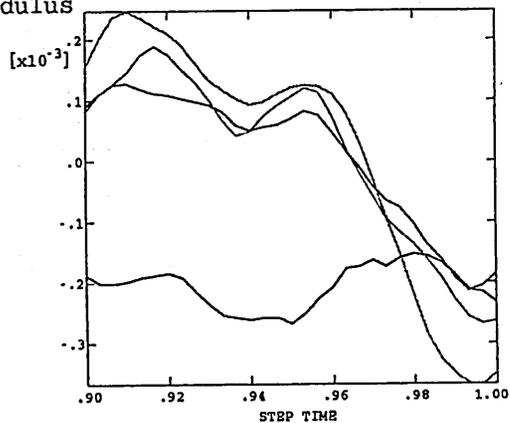
# ABAQUS

Elastic Modulus  
 Varied



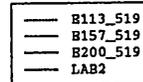
Input Freq.  
 6 hz

Displacement  
 at LVDT#3



# ABAQUS

Elastic Modulus  
 Varied



Input Freq.  
 6 hz

Displacement  
 at LVDT#2

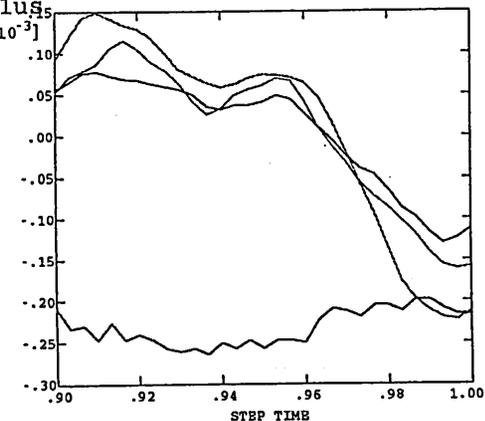


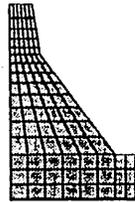
Figure g21

# ABAQUS

Koyna Laboratory Model Study  
Uncracked Model Study  
Sensitivity Study  
Variation of Elastic Modulus

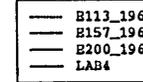
At Diff. Input Frequencies  
Comparison of Displacements  
Dynamic Analysis

Input Record SHAKEA  
Mesh # 3



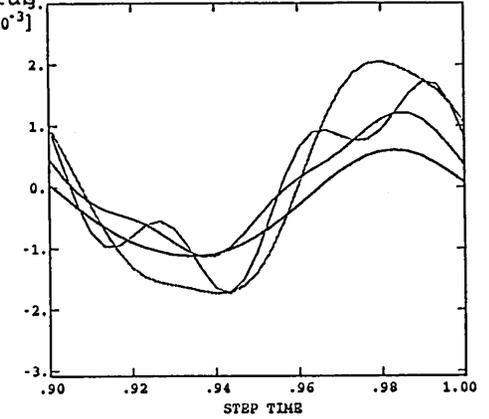
# ABAQUS

Elastic Modulus  
Varied [ $\times 10^{-3}$ ]



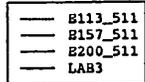
Input Freq.  
10 hz

Displacement  
at LVDT#4



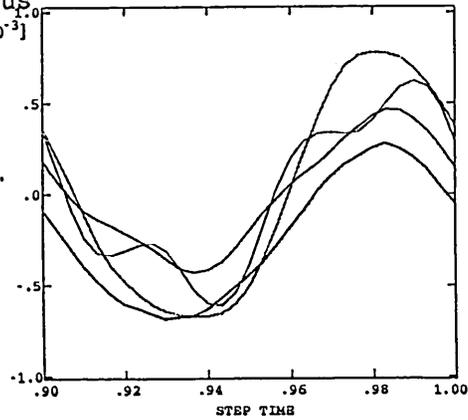
# ABAQUS

Elastic Modulus  
Varied [ $\times 10^{-3}$ ]



Input Freq.  
10 hz

Displacement  
at LVDT#3



# ABAQUS

Elastic Modulus  
Varied [ $\times 10^{-3}$ ]



Input Freq.  
10 hz

Displacement  
at LVDT#2

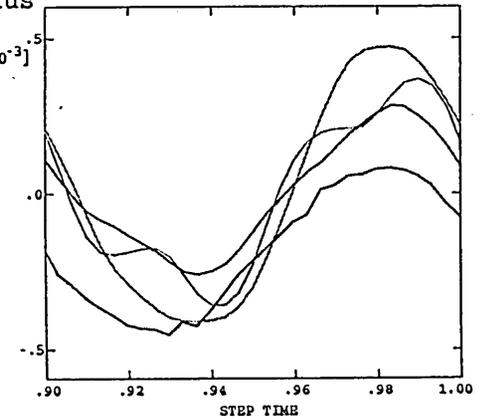


Figure g22

# ABAQUS

Koyna Laboratory Model Study  
Uncracked Model Study  
Sensitivity Study  
Variation of Elastic Modulus

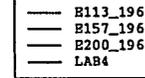
At Diff. Input Frequencies  
Comparison of Displacements  
Dynamic Analysis

Input Record SHAKEA  
Mesh # 3



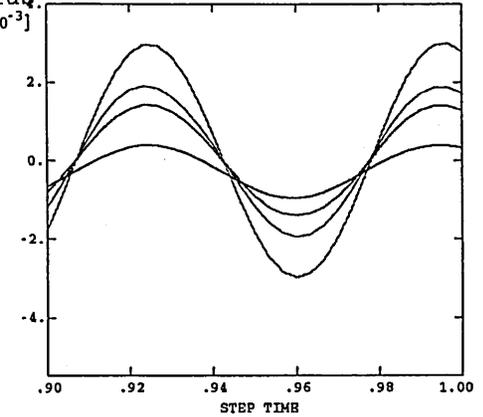
# ABAQUS

Elastic Modulus  
Varied [ $\times 10^{-3}$ ]



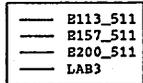
Input Freq.  
14 hz

Displacement  
at LVDT#4



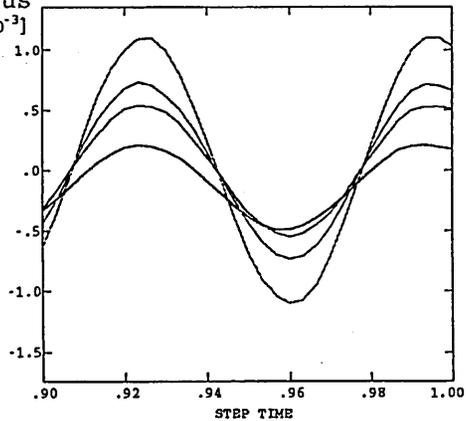
# ABAQUS

Elastic Modulus  
Varied [ $\times 10^{-3}$ ]



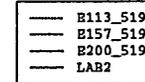
Input Freq.  
14 hz

Displacement  
at LVDT#3



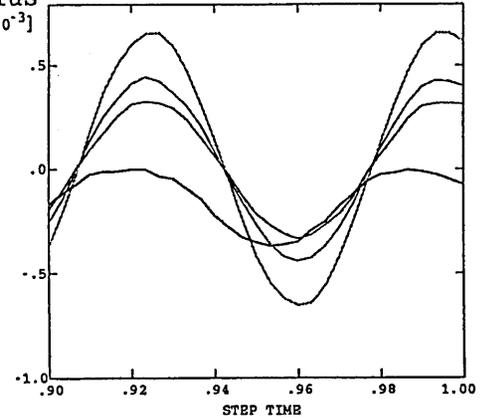
# ABAQUS

Elastic Modulus  
Varied [ $\times 10^{-3}$ ]



Input Freq.  
14 hz

Displacement  
at LVDT#2

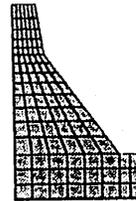


# ABAQUS

Koyna Laboratory Model Study  
 Uncracked Model Study  
 Sensitivity Study  
 Variation of Elastic Modulus

At Diff. Input Frequencies  
 Comparison of Displacements  
 Dynamic Analysis

Input Record SHAKEA  
 Mesh # 3



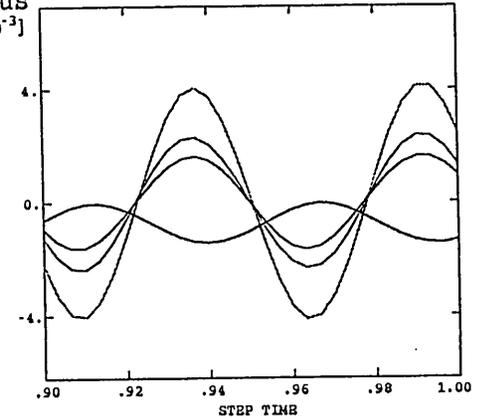
# ABAQUS

Elastic Modulus  
 Varied [ $\times 10^{-3}$ ]

- B113\_196
- B157\_196
- B200\_196
- LAB4

Input Freq.  
 18 hz

Displacement  
 at LVDT#4



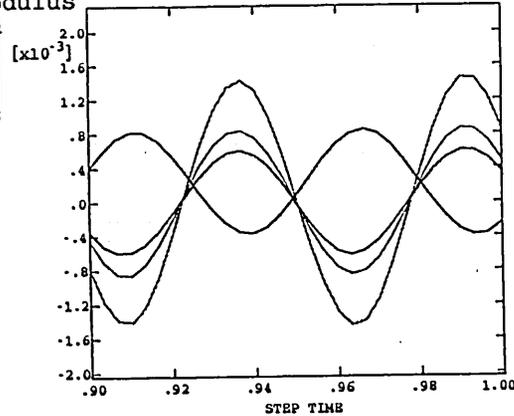
# ABAQUS

Elastic Modulus  
 Varied

- B113\_511 [ $\times 10^{-3}$ ]
- B157\_511
- B200\_511
- LAB3

Input Freq.  
 18 hz

Displacement  
 at LVDT#3



# ABAQUS

Elastic Modulus  
 Varied [ $\times 10^{-3}$ ]

- B113\_519
- B157\_519
- B200\_519
- LAB2

Input Freq.  
 18 hz

Displacement  
 at LVDT#2

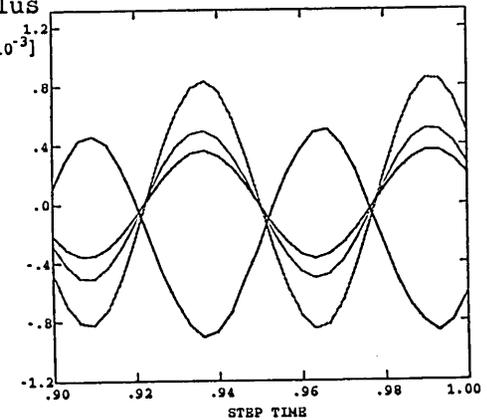


Figure g24

# ABAQUS

Koyna Laboratory Model Study  
 Uncracked Model Study  
 Sensitivity Study  
 Variation of Elastic Modulus

At Diff. Input Frequencies  
 Comparison of Displacements  
 Dynamic Analysis

Input Record SHAKEA  
 Mesh # 3



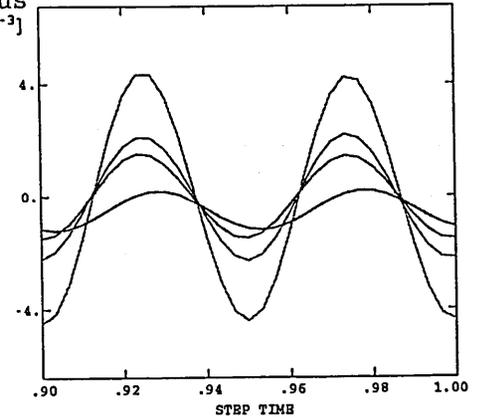
# ABAQUS

Elastic Modulus  
 Varied [ $\times 10^{-3}$ ]

- E113\_196
- E157\_196
- E200\_196
- LAB4

Input Freq.  
 20 hz

Displacement  
 at LVDT#4



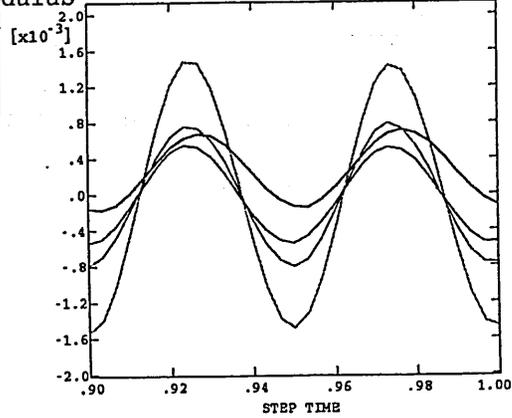
# ABAQUS

Elastic Modulus  
 Varied [ $\times 10^{-3}$ ]

- E113\_511
- E157\_511
- E200\_511
- LAB3

Input Freq.  
 20 hz

Displacement  
 at LVDT#3



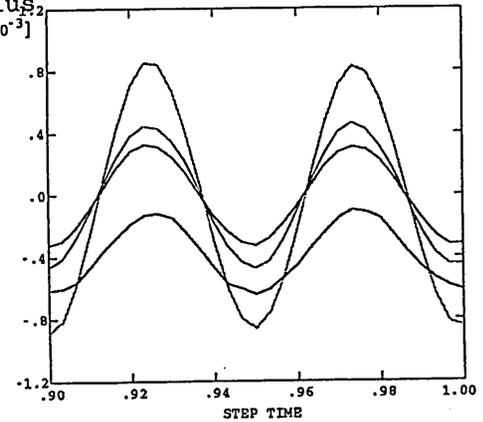
# ABAQUS

Elastic Modulus<sub>2</sub>  
 Varied [ $\times 10^{-3}$ ]

- E113\_519
- E157\_519
- E200\_519
- LAB2

Input Freq.  
 20 hz

Displacement  
 at LVDT#2



# ABAQUS

Koyna Laboratory Model Study  
 Uncracked Model Study  
 Sensitivity Study  
 Variation of Elastic Modulus

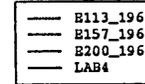
At Diff. Input Frequencies  
 Comparison of Displacements  
 Dynamic Analysis

Input Record SHAKEA  
 Mesh # 3



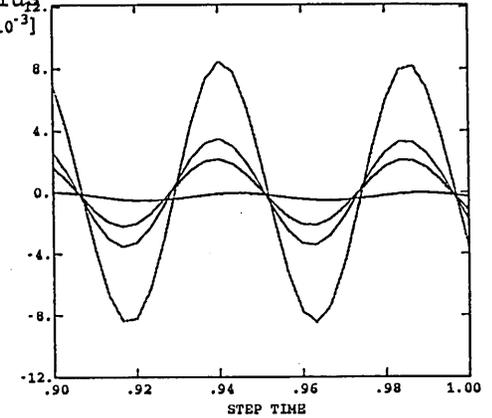
# ABAQUS

Elastic Modulus  
 Varied [ $\times 10^{-3}$ ]



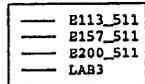
Input Freq.  
 22 hz

Displacement  
 at LVDT#4



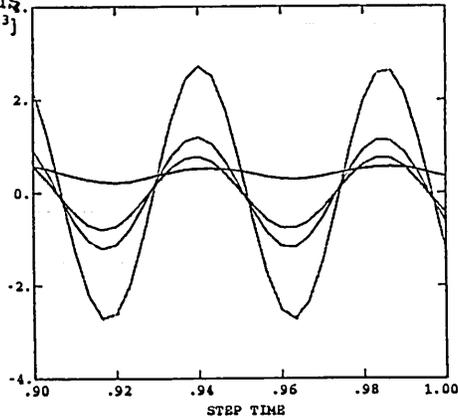
# ABAQUS

Elastic Modulus  
 Varied [ $\times 10^{-3}$ ]



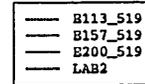
Input Freq.  
 22 hz

Displacement  
 at LVDT#3



# ABAQUS

Elastic Modulus  
 Varied [ $\times 10^{-3}$ ]



Input Freq.  
 22 hz

Displacement  
 at LVDT#2

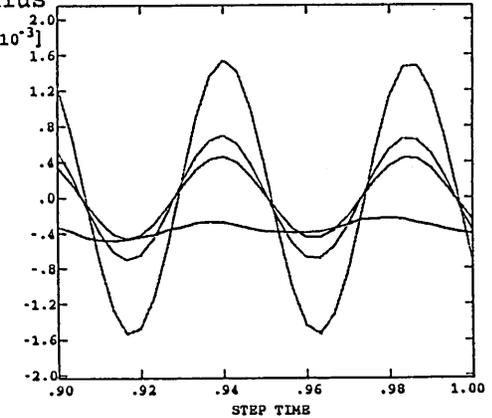


Figure g26

# ABAQUS

Koyna Laboratory Model Study  
 Uncracked Model Study  
 Sensitivity Study  
 Variation of Elastic Modulus

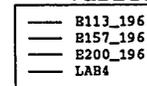
At Diff. Input Frequencies  
 Comparison of Displacements  
 Dynamic Analysis

Input Record SHAKEA  
 Mesh # 3



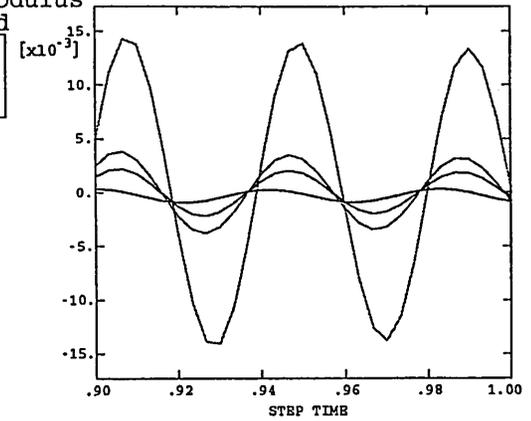
# ABAQUS

Elastic Modulus  
 Varied



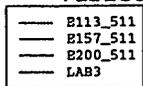
Input Freq.  
 24 hz

Displacement  
 at LVDT#4



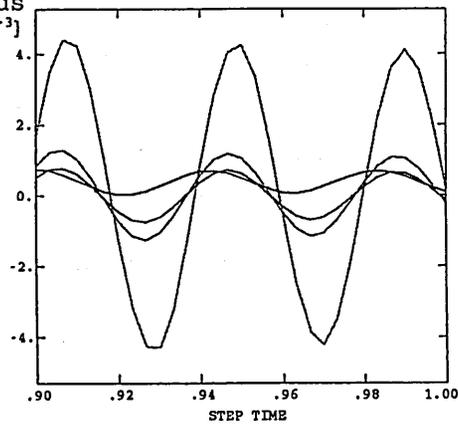
# ABAQUS

Elastic Modulus  
 Varied [ $\times 10^{-3}$ ]



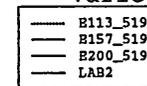
Input Freq.  
 24 hz

Displacement  
 at LVDT#3



# ABAQUS

Elastic Modulus  
 Varied [ $\times 10^{-3}$ ]



Input Freq.  
 24 hz

Displacement  
 at LVDT#2

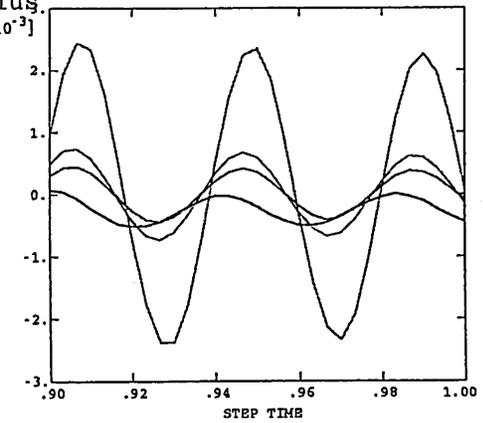


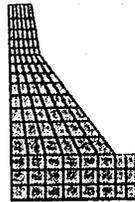
Figure g27

# ABAQUS

Koyna Laboratory Model Study  
 Uncracked Model Study  
 Sensitivity Study  
 Variation of Elastic Modulus

At Diff. Input Frequencies  
 Comparison of Displacements  
 Dynamic Analysis

Input Record SHAKEA  
 Mesh # 3



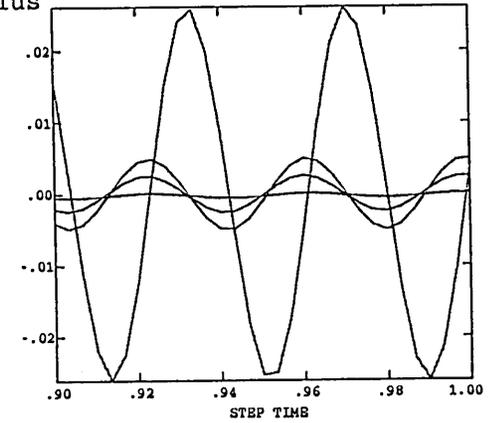
# ABAQUS

Elastic Modulus  
 Varied

- E113\_196
- E157\_196
- E200\_196
- LAB4

Input Freq.  
 26 hz

Displacement  
 at LVDT#4



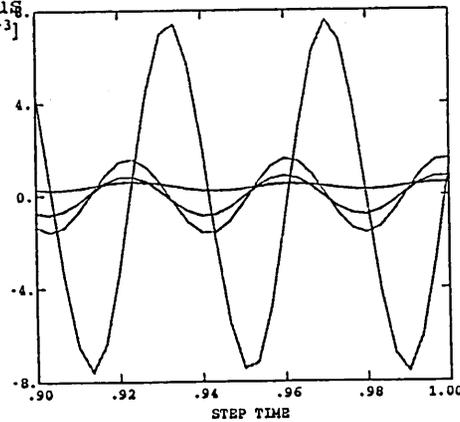
# ABAQUS

Elastic Modulus  
 Varied [ $\times 10^{-3}$ ]

- E113\_511
- E157\_511
- E200\_511
- LAB3

Input Freq.  
 26 hz

Displacement  
 at LVDT#3



# ABAQUS

Elastic Modulus  
 Varied [ $\times 10^{-3}$ ]

- E113\_519
- E157\_519
- E200\_519
- LAB2

Input Freq.  
 26 hz

Displacement  
 at LVDT#2

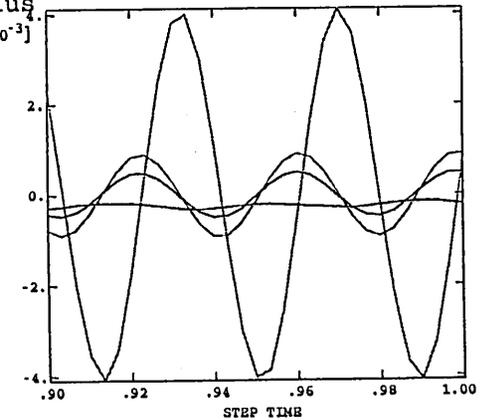


Figure g28

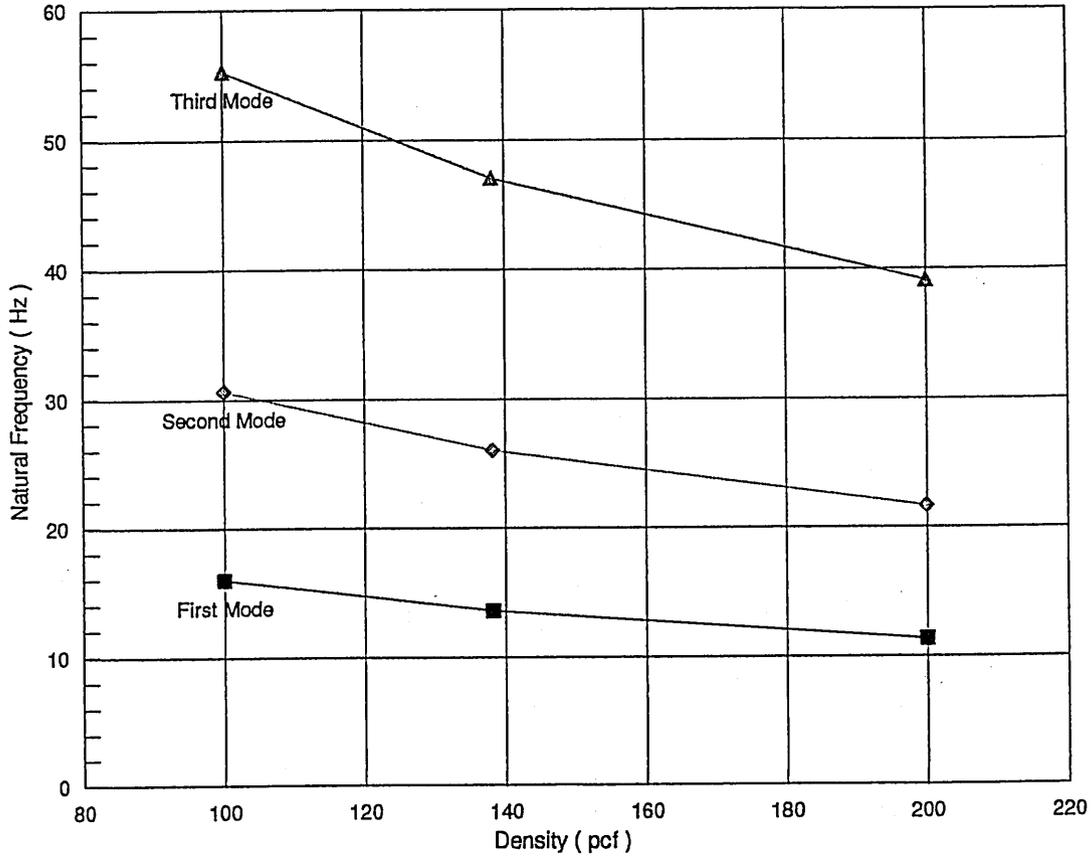
Uncracked Koyna Laboratory Study  
Sensitivity to Variation in Material Density  
Mesh#3

Material Properties

Elastic Modulus = 113 ksi  
Material Density = (100, 138, 200 pcf)

Damping = 3.5% critical  
Rayleigh Damping Factors  
Alpha = 1.954769; Beta = .000248

**Natural Frequency**  
Material Density Varied



**E = 113 ksi**

Natural Frequencies (Hz)

Mode	100	138.2	200	LAB
1	16.0	13.6	11.3	18.0
2	30.6	26.0	21.6	24.0
3	55.3	47.0	39.1	30.0
4	65.8	55.9	46.5	
5	68.7	58.4	48.5	
6	70.8	60.2	50.1	
7	75.2	64.0	53.2	
8	76.2	64.8	53.9	
9	76.9	65.4	54.4	
10	78.4	66.7	55.4	

Figure g29

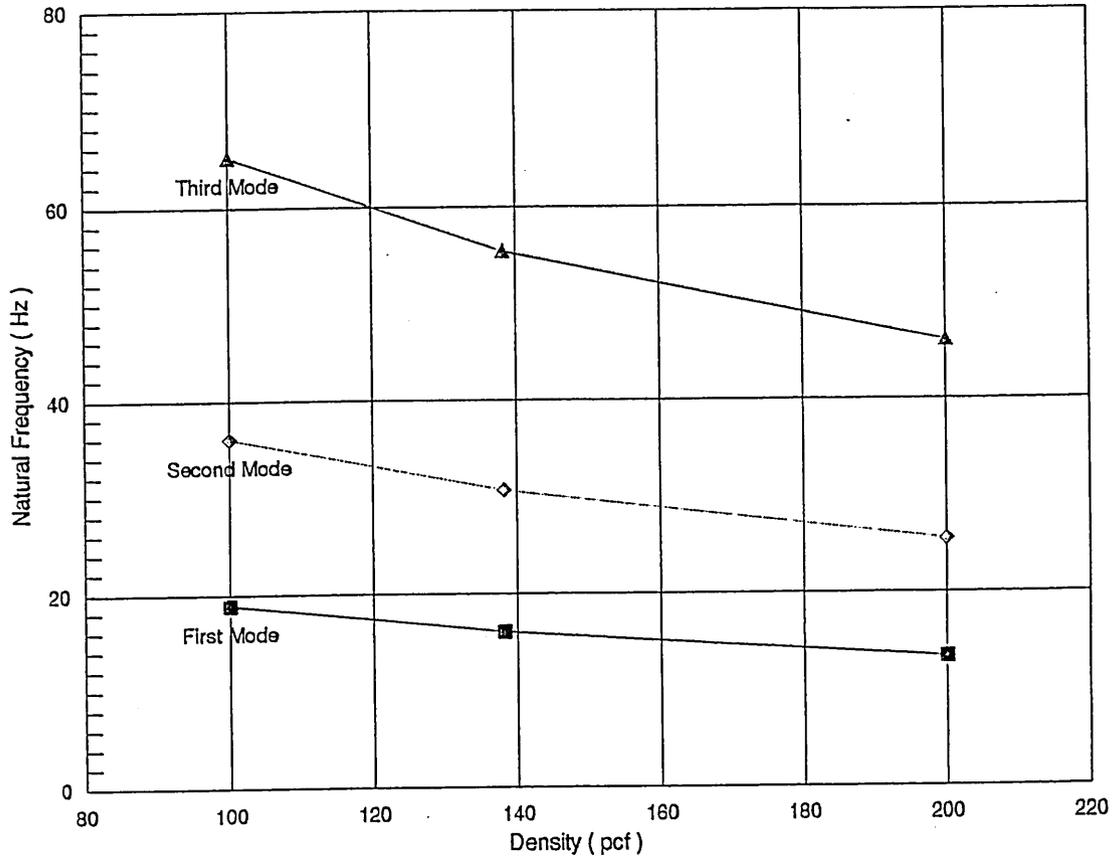
Uncracked Koyna Laboratory Study  
Sensitivity to Variation in Material Density  
Mesh#3

Material Properties

Elastic Modulus = 157 ksi  
Material Density = (100, 138, 200 pcf)

Damping = 3.5% critical  
Rayleigh Damping Factors

Natural Frequencies  
Material Density Varied



E = 157 ksi

Natural Frequencies (Hz)

Mode	100	138.2	200	LAB
1	18.8	16.0	13.3	18.0
2	36.0	30.6	25.5	22.0
3	65.1	55.4	46.1	30.0
4	77.5	65.9	54.8	
5	80.9	68.8	57.2	
6	83.5	71.0	59.0	
7	88.7	75.4	62.7	
8	89.8	76.4	63.5	
9	90.6	77.1	64.1	
10	92.4	78.6	65.3	

Figure g30

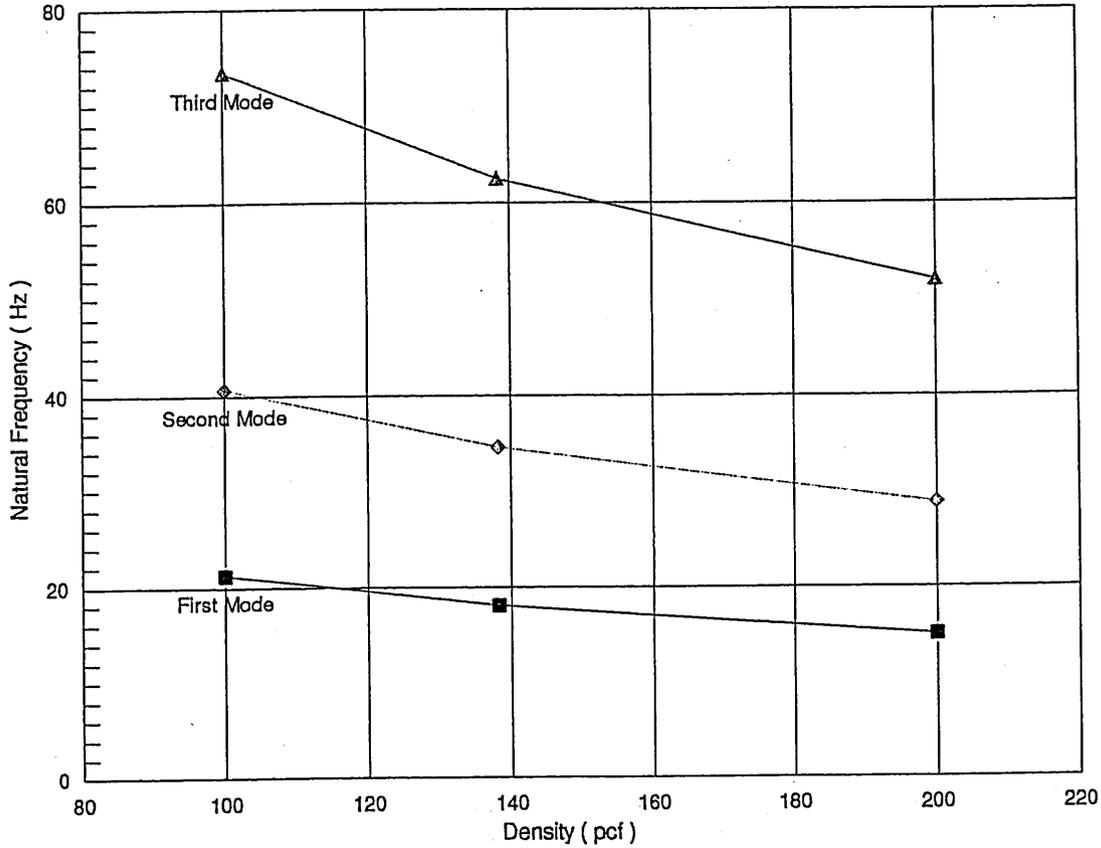
Uncracked Koyna Laboratory Study  
Sensitivity to Variation in Material Density  
Mesh#3

Material Properties

Elastic Modulus = 200 ksi  
Material Density = (100, 138, 200 pcf)

Damping = 3.5% critical  
Rayleigh Damping Factors  
Alpha = 1.954769; Beta = .000248

**Natural Frequencies**  
Material Density Varied



E = 200 ksi

Natural Frequencies (Hz)				
Mode	100	138.2	200	LAB
1	21.3	18.1	15.0	18.0
2	40.7	34.6	28.7	24.0
3	73.5	62.5	52.0	30.0
4	87.5	74.4	61.9	
5	91.3	77.7	64.6	
6	94.2	80.1	66.6	
7	100.1	85.1	70.8	
8	101.3	86.2	71.6	
9	102.3	87.0	72.3	
10	104.3	88.7	73.7	

Figure g31

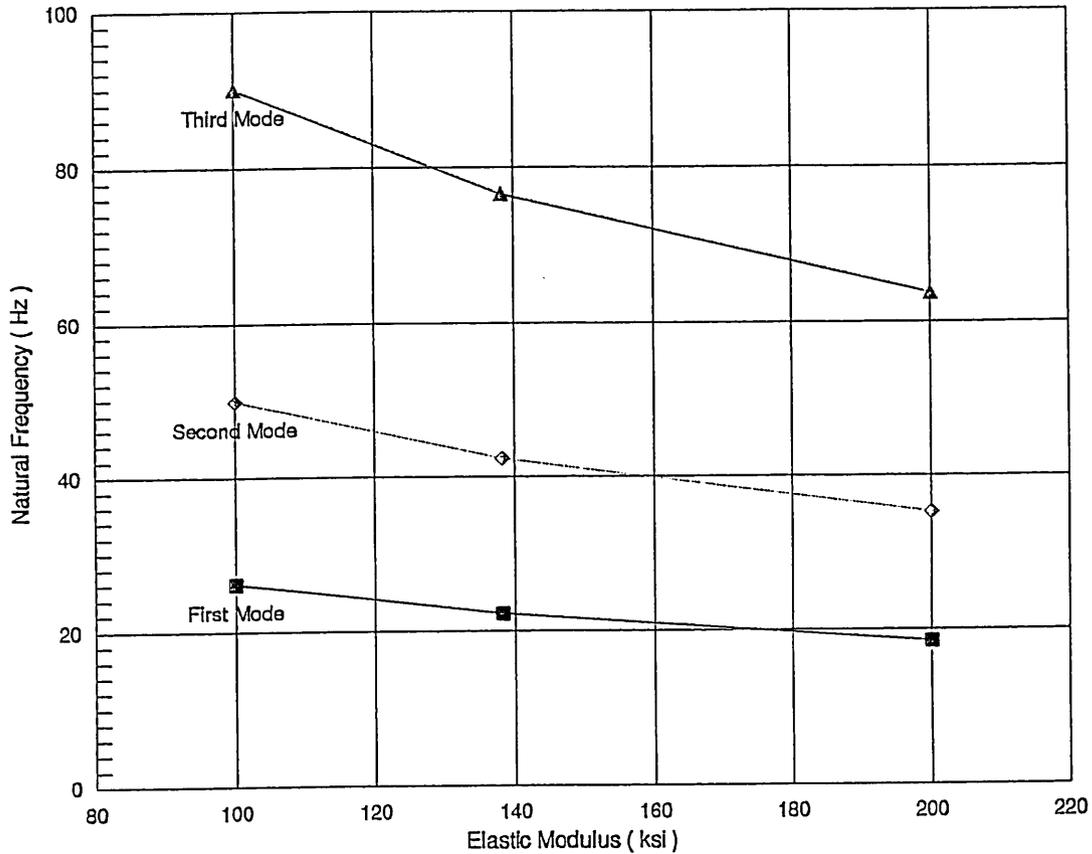
Uncracked Koyna Laboratory Study  
Sensitivity to Variation in Material Density  
Mesh#3

Material Properties

Elastic Modulus = 300 ksi  
Material Density = (100, 138, 200 pcf)

Damping = 3.5% critical  
Rayleigh Damping Factors  
Alpha = 1.954769; Beta = .000248

**Natural Frequency**  
Material Density Varied



E = 300 ksi

Natural Frequencies (Hz)

Mode	100	138.2	200	LAB
1	26.0	22.2	18.4	18.0
2	49.8	42.4	35.2	24.0
3	90.0	76.6	63.7	30.0
4	107.2	91.1	75.8	
5	111.9	95.2	79.1	
6	115.4	98.1	81.6	
7	122.5	104.2	86.7	
8	124.1	105.6	87.7	
9	125.3	106.6	88.6	
10	127.7	108.7	90.3	

Figure g32

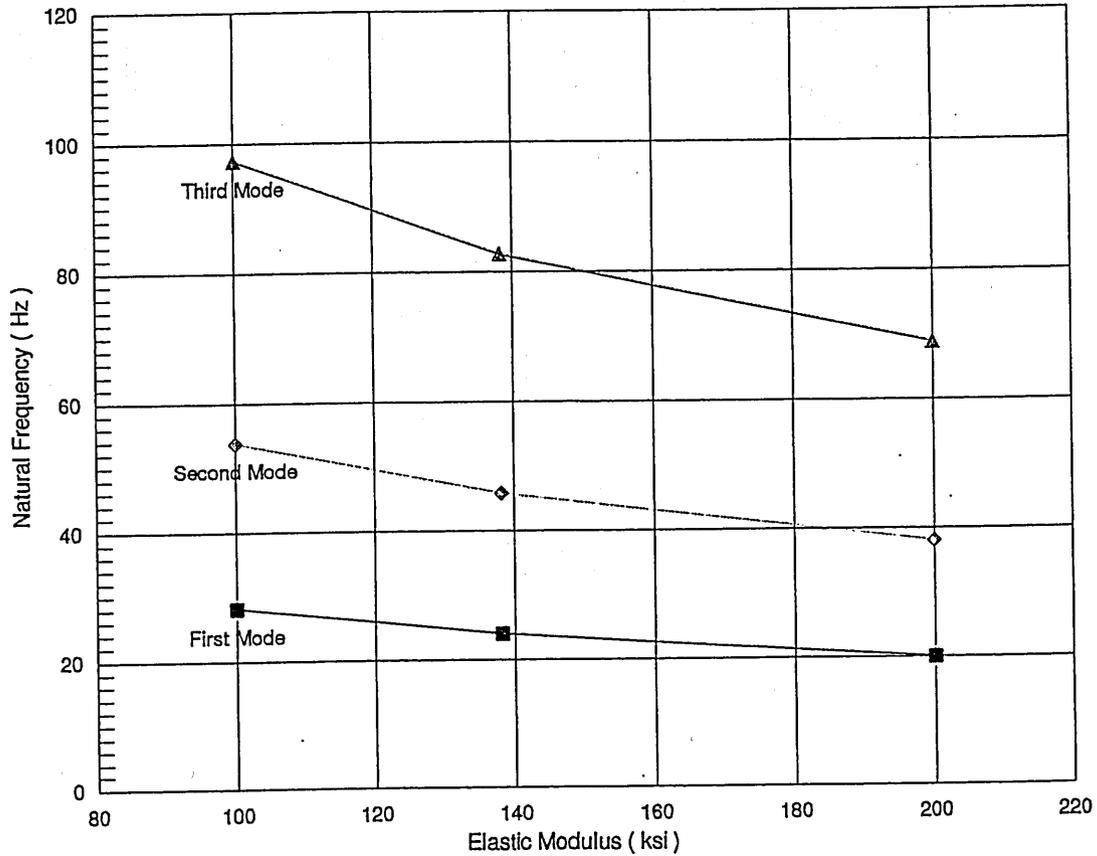
Uncracked Koyna Laboratory Study  
Sensitivity to Variation in Material Density  
Mesh#3

Material Properties

Elastic Modulus = 350 ksi  
Material Density = (100, 138, 200 pcf)

Damping = 3.5% critical  
Rayleigh Damping Factors  
Alpha = 1.954769; Beta = .000248

Natural Frequency  
Material Density Varied



E = 350 ksi

Natural Frequencies (Hz)

Mode	100	138.2	200	LAB
1	28.1	24.0	19.9	18.0
2	53.8	45.7	38.0	24.0
3	97.2	82.7	68.8	30.0
4	115.7	98.4	81.8	
5	120.8	102.8	85.4	
6	124.6	106.0	88.1	
7	132.4	112.6	93.6	
8	134.0	114.0	94.8	
9	135.3	115.1	95.7	
10	138.0	117.4	97.6	

Figure g33

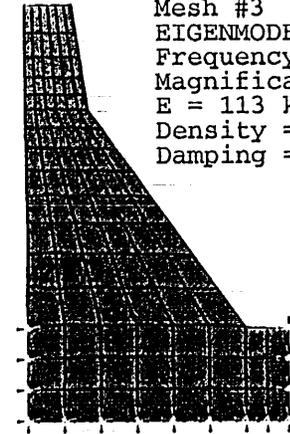
# ABAQUS

Mesh #3  
EIGENMODE 1  
Frequency = 13.6  
Magnification = 20  
E = 113 ksi  
Density = 138.2  
Damping = 3.5%



# ABAQUS

Mesh #3  
EIGENMODE 1  
Frequency = 13.6  
Magnification = 20  
E = 113 ksi  
Density = 138.2 pcf  
Damping = 3.5%



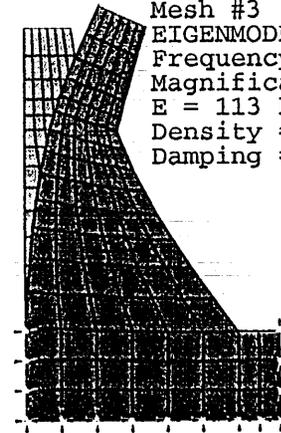
# ABAQUS

Mesh #3  
EIGENMODE 2  
Frequency = 26  
Magnification = 20  
E = 113 ksi  
Density = 138.2 pcf  
Damping = 3.5%



# ABAQUS

Mesh #3  
EIGENMODE 2  
Frequency = 26  
Magnification = 20  
E = 113 ksi  
Density = 138.2 pcf  
Damping = 3.5%



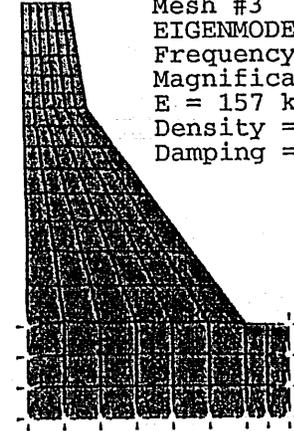
# ABAQUS

Mesh #3  
EIGENMODE 1  
Frequency = 16.0  
Magnification =  
E = 157 ksi  
Density = 138.2  
Damping = 3.5%



# ABAQUS

Mesh #3  
EIGENMODE 1  
Frequency = 16.0  
Magnification = 20  
E = 157 ksi  
Density = 138.2 pcf  
Damping = 3.5%



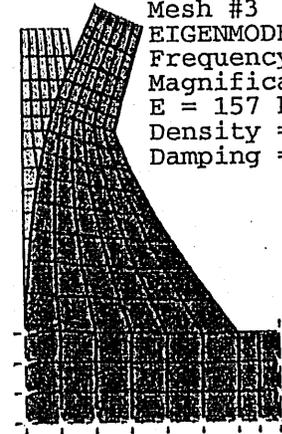
# ABAQUS

Mesh #3  
EIGENMODE 2  
Frequency = 30.6  
Magnification = 20  
E = 157 ksi  
Density = 138.2 pcf  
Damping = 3.5%



# ABAQUS

Mesh #3  
EIGENMODE 2  
Frequency = 30.6  
Magnification = 20  
E = 157 ksi  
Density = 138.2 pcf  
Damping = 3.5%



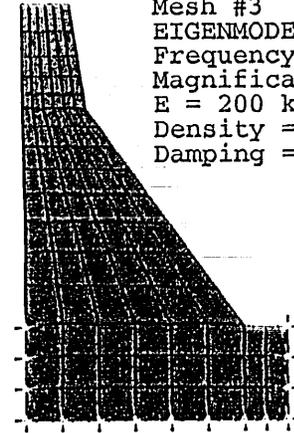
# ABAQUS

Mesh #3  
EIGENMODE 1  
Frequency = 18.1  
Magnification = 20  
E = 200 ksi  
Density = 138.2  
Damping = 3.5%



# ABAQUS

Mesh #3  
EIGENMODE 1  
Frequency = 18.1  
Magnification = 20  
E = 200 ksi  
Density = 138.2 pcf  
Damping = 3.5%



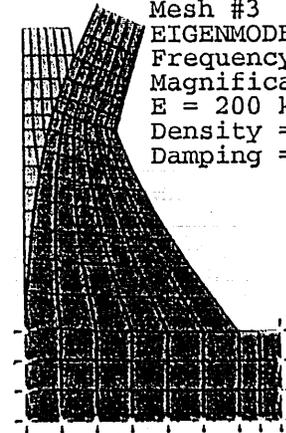
# ABAQUS

Mesh #3  
EIGENMODE 2  
Frequency = 34.6  
Magnification = 20  
E = 200 ksi  
Density = 138.2 pcf  
Damping = 3.5%



# ABAQUS

Mesh #3  
EIGENMODE 2  
Frequency = 34.6  
Magnification = 20  
E = 200 ksi  
Density = 138.2 pcf  
Damping = 3.5%



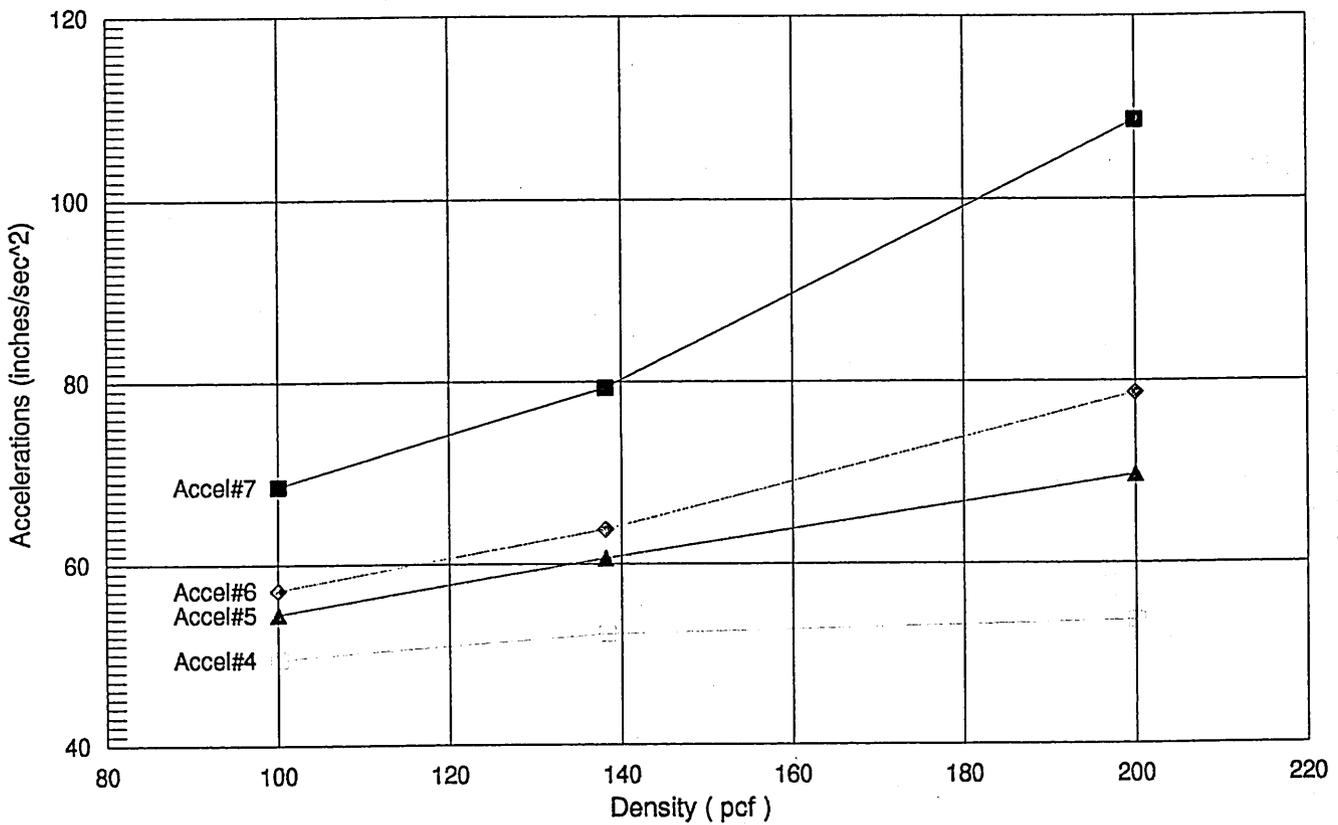
Uncracked Koyna Laboratory Study  
Sensitivity to Variation in Material Density  
Mesh#3

Material Properties

E = 113,000 psi  
Material Density = (100, 138, 200 pcf)

Damping = 3.5% critical  
Rayleigh Damping Factors  
Alpha = 1.954769; Beta = .000248

**Peak Accelerations**  
Material Density Varied



E = 113 ksi

Peak Accelerations ( inch / sec ^ 2 )

	100	138.2	200	LAB
Accel#7	68.51	79.31	108.60	53.26
Accel#6	57.18	63.80	78.68	51.72
Accel#5	54.49	60.60	69.67	49.26
Accel#4	49.40	52.28	53.65	47.72

Figure g37

Uncracked Koyna Laboratory Study  
Sensitivity to Variation in Material Density  
Mesh#3

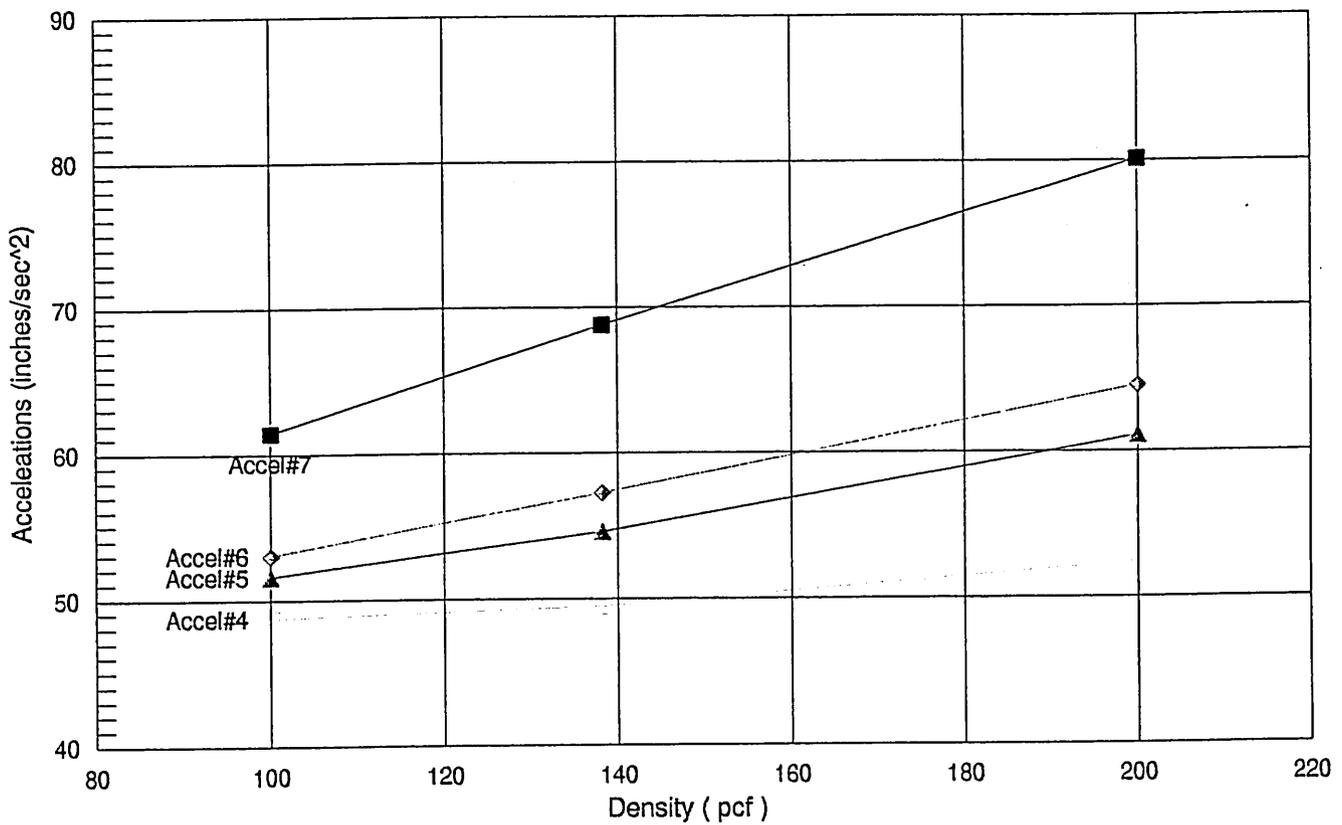
Material Properties

E = 157,000 psi  
Material Density = (100, 138, 200 pcf)

Damping = 3.5% critical

Rayleigh Damping Factors  
Alpha = 1.954769; Beta = .000248

**Peak Accelerations**  
Material Density Varied



E = 157 ksi

Peak Accelerations ( inch / sec ^ 2 )

	100	138.2	200	LAB
Accel#7	61.39	68.75	80.10	53.26
Accel#6	52.99	57.19	64.49	51.72
Accel#5	51.54	54.54	61.04	49.26
Accel#4	48.70	49.47	52.36	47.72

Figure g38

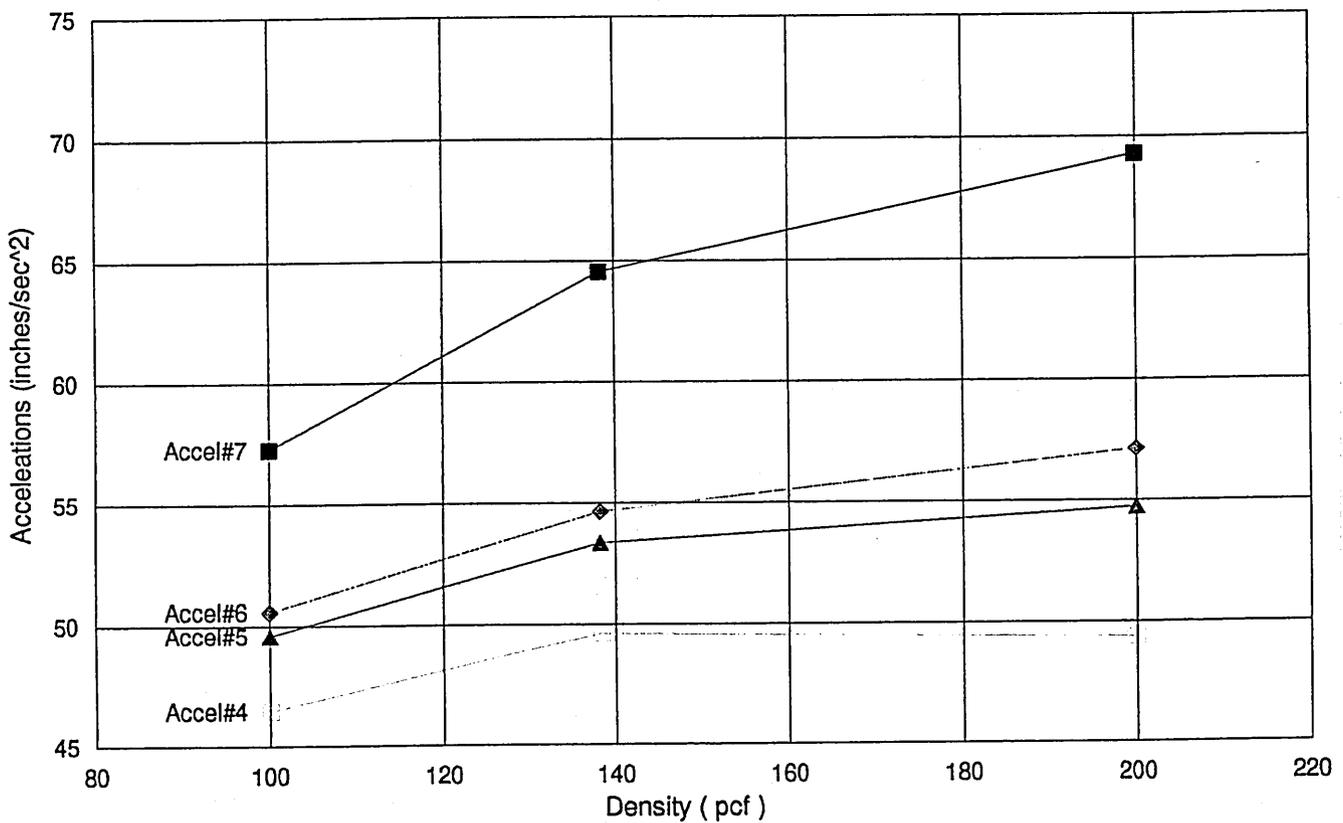
Uncracked Koyna Laboratory Study  
Sensitivity to Variation in Material Density  
Mesh#3

Material Properties

E = 200,000 psi  
Material Density = (100, 138, 200 pcf)

Damping = 3.5% critical  
Rayleigh Damping Factors  
Alpha = 1.954769; Beta = .000248

**Peak Accelerations**  
Material Density Varied



E = 200 ksi

Peak Accelerations ( inch / sec ^ 2 )

	100	138.2	200	LAB
Accel#7	57.25	64.53	69.27	53.26
Accel#6	50.56	54.64	57.12	51.72
Accel#5	49.57	53.34	54.73	49.26
Accel#4	46.42	49.60	49.36	47.72

Figure g39

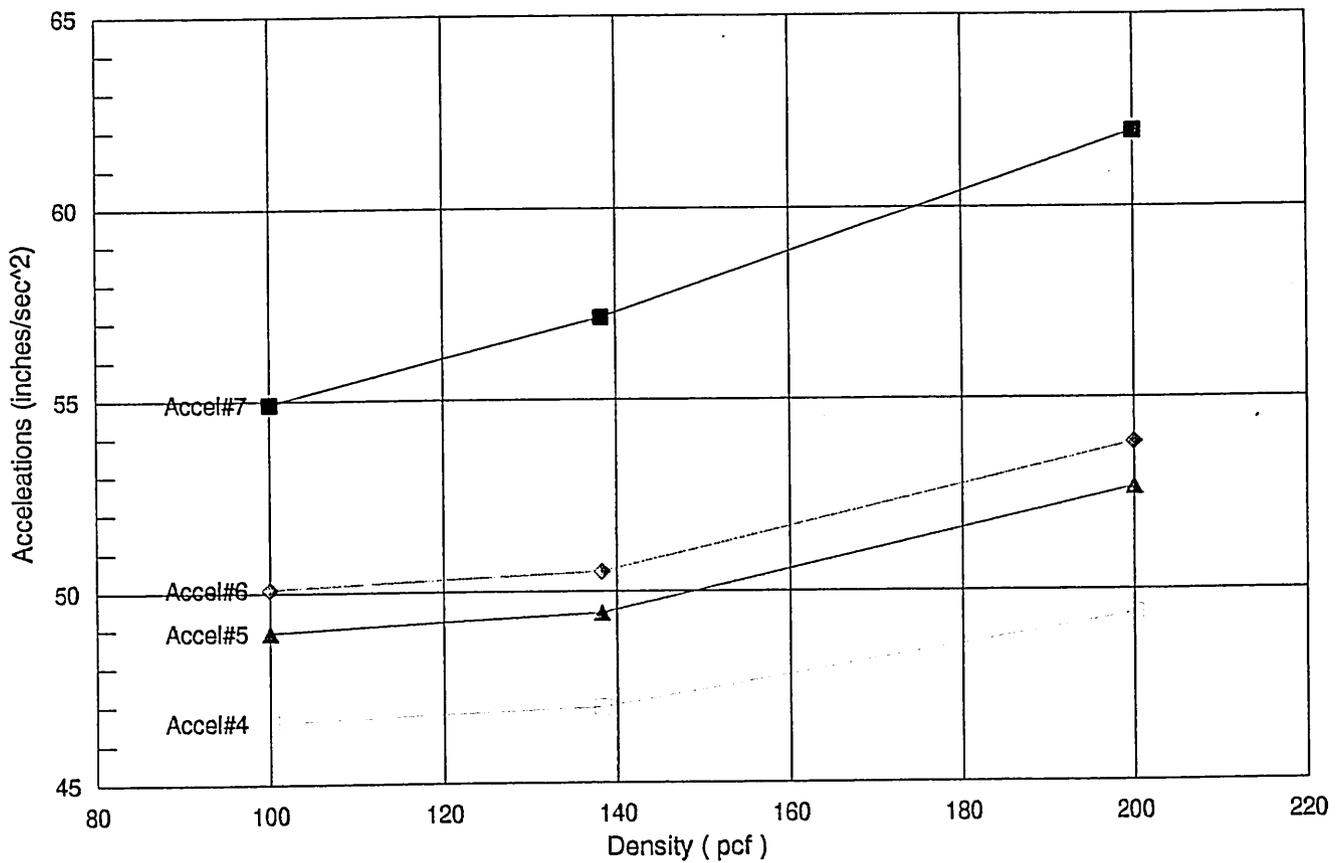
Uncracked Koyna Laboratory Study  
Sensitivity to Variation in Material Density  
Mesh#3

Material Properties

E = 300,000 psi  
Material Density = (100, 138, 200 pcf)

Damping = 3.5% critical  
Rayleigh Damping Factors  
Alpha = 1.954769; Beta = .000248

**Peak Accelerations**  
Material Density Varied



E = 300 ksi

Peak Accelerations ( inch / sec ^ 2 )

	100	138.2	200	LAB
Accel#7	54.90	57.14	61.96	53.26
Accel#6	50.07	50.50	53.82	51.72
Accel#5	48.93	49.42	52.65	49.26
Accel#4	46.59	46.97	49.36	47.72

Figure g40

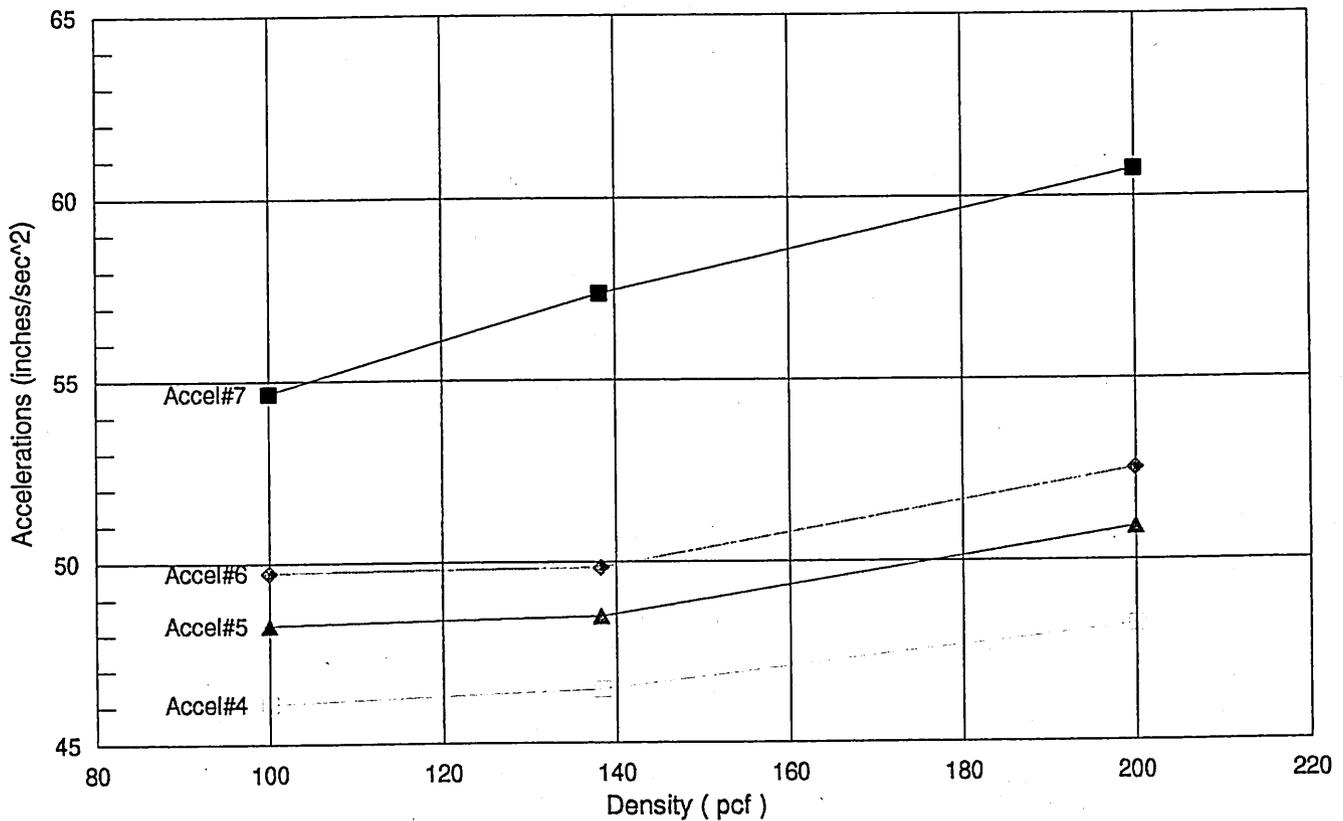
Uncracked Koyna Laboratory Study  
Sensitivity to Variation in Material Density  
Mesh#3

Material Properties

E = 350,000 psi  
Material Density = (100, 138, 200 pcf)

Damping = 3.5% critical  
Rayleigh Damping Factors  
Alpha = 1.954769; Beta = .000248

**Peak Accelerations**  
Material Density Varied



E = 350 ksi

Peak Accelerations ( inch / sec ^ 2 )

	100	138.2	200	LAB
Accel#7	54.66	57.39	60.74	53.26
Accel#6	49.73	49.85	52.52	51.72
Accel#5	48.29	48.51	50.91	49.26
Accel#4	46.09	46.47	48.24	47.72

Figure g41

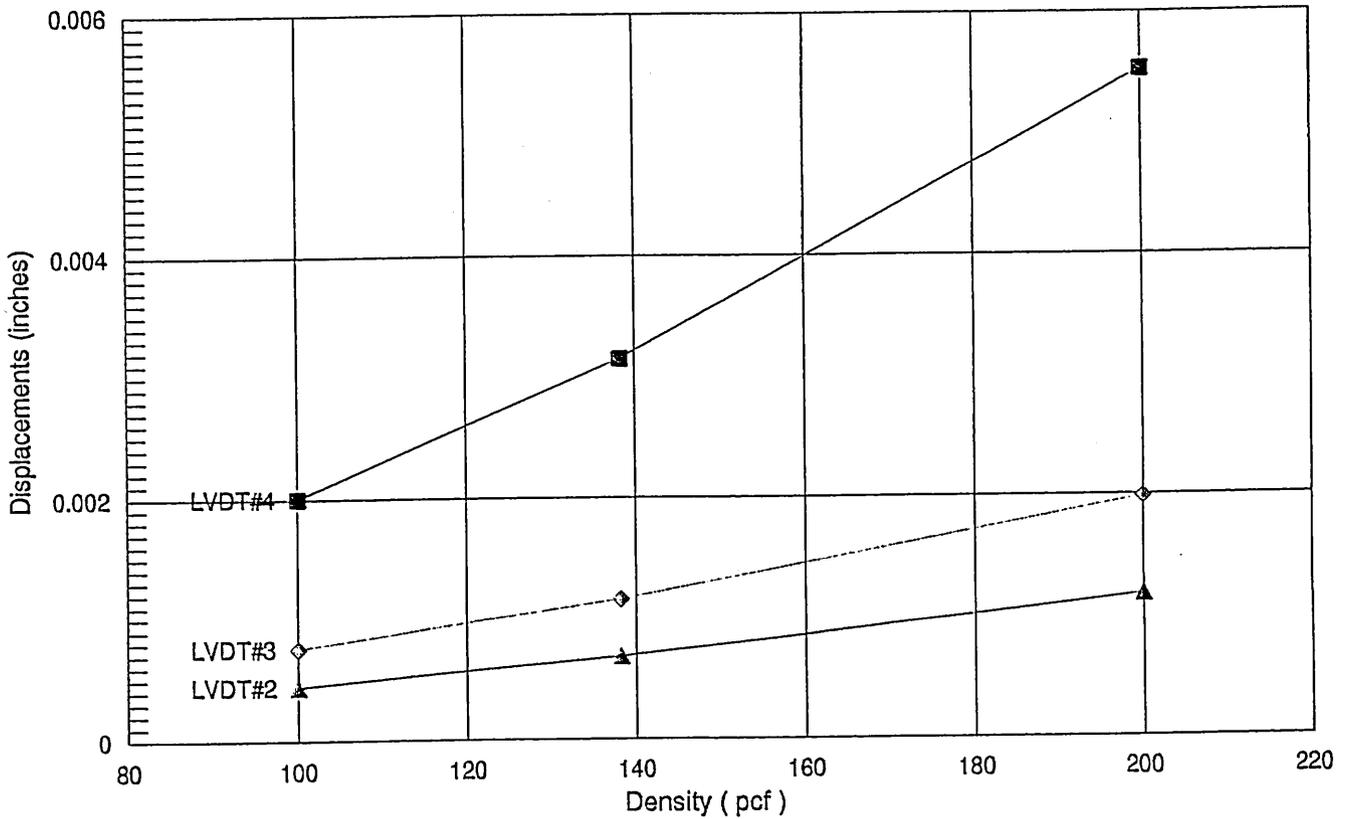
Uncracked Koyna Laboratory Study  
Sensitivity to Variation in Material Density  
Mesh#3

Material Properties

E = 113,000 psi  
Material Density = (100, 138, 200 pcf)

Damping = 3.5% critical  
Rayleigh Damping Factors  
Alpha = 1.954769; Beta = .000248

**Peak Displacements**  
Material Density Varied



E = 113 ksi

Peak Displacements ( inches )

	100	138.2	200	LAB
LVDT#4	2.0E-03	3.1E-03	5.5E-03	7.2E-04
LVDT#3	7.6E-04	1.2E-03	2.0E-03	3.1E-04
LVDT#2	4.5E-04	6.9E-04	1.2E-03	2.1E-04

Figure g42

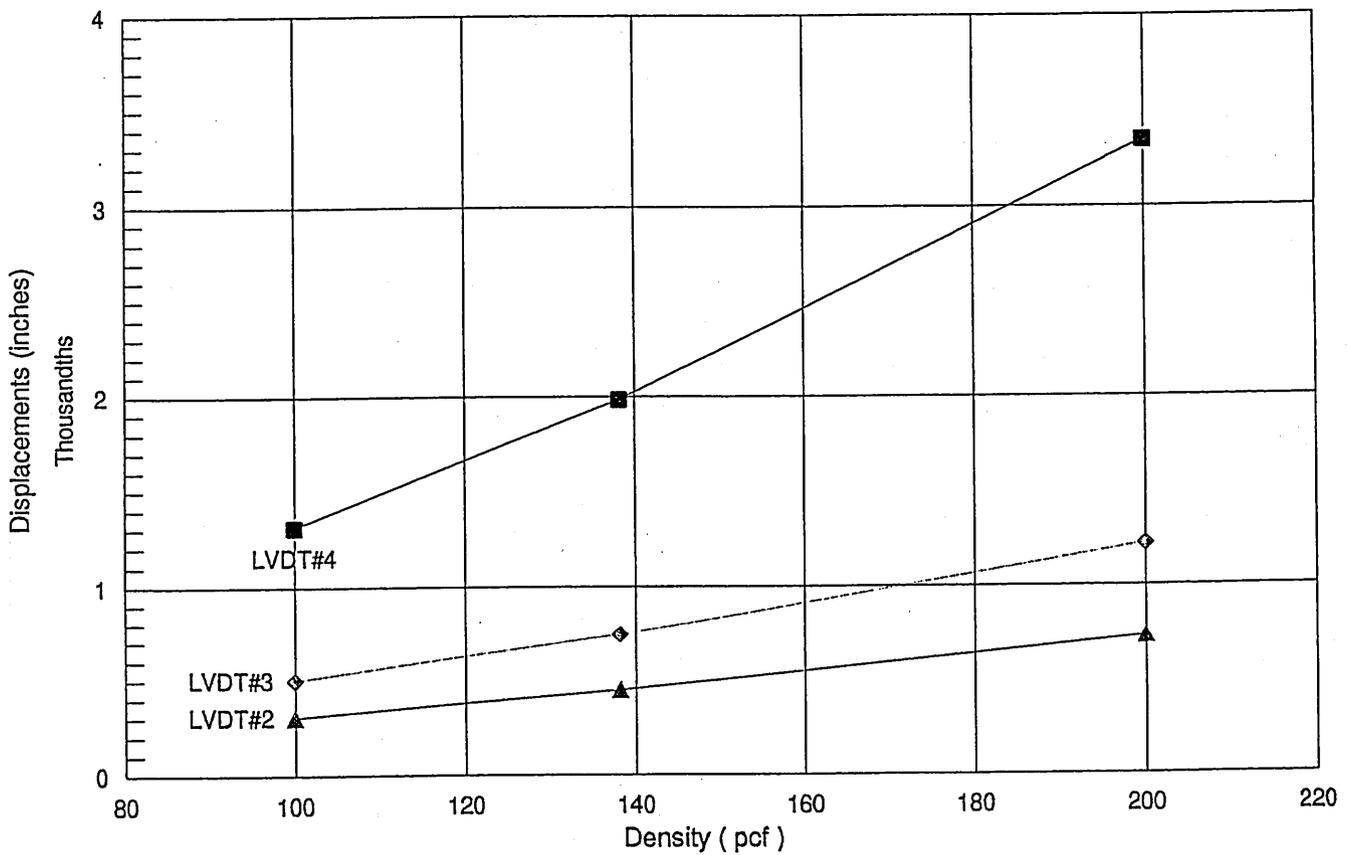
Uncracked Koyna Laboratory Study  
Sensitivity to Variation in Material Density  
Mesh#3

Material Properties

E = 157,000 psi  
Material Density = (100, 138, 200 pcf)

Damping = 3.5% critical  
Rayleigh Damping Factors  
Alpha = 1.954769; Beta = .000248

**Peak Displacements**  
Material Density Varied



E = 157 ksi

Peak Displacements ( inches )

	100	138.2	200	LAB
LVDT#4	1.3E-03	2.0E-03	3.3E-03	7.2E-04
LVDT#3	5.0E-04	7.4E-04	1.2E-03	3.1E-04
LVDT#2	3.0E-04	4.4E-04	7.2E-04	2.1E-04

Figure g43

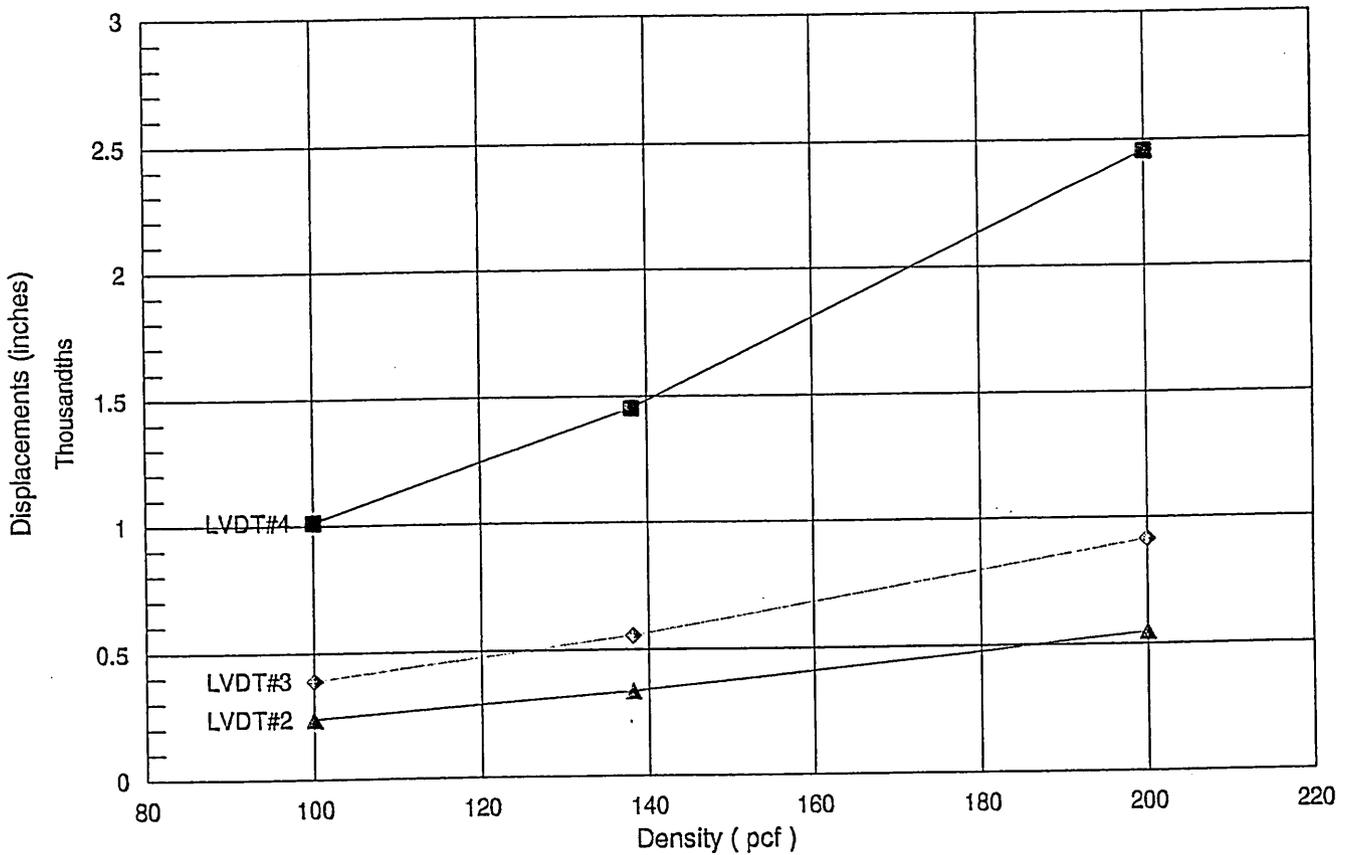
Uncracked Koyna Laboratory Study  
Sensitivity to Variation in Material Density  
Mesh#3

Material Properties

E = 200,000 psi  
Material Density = (100, 138, 200 pcf)

Damping = 3.5% critical  
Rayleigh Damping Factors  
Alpha = 1.954769; Beta = .000248

**Peak Displacements**  
Material Density Varied



E = 200 ksi

Peak Displacements ( inches )

	100	138.2	200	LAB
LVDT#4	1.0E-03	1.5E-03	2.5E-03	7.2E-04
LVDT#3	3.9E-04	5.5E-04	9.1E-04	3.1E-04
LVDT#2	2.4E-04	3.3E-04	5.5E-04	2.1E-04

Figure g44

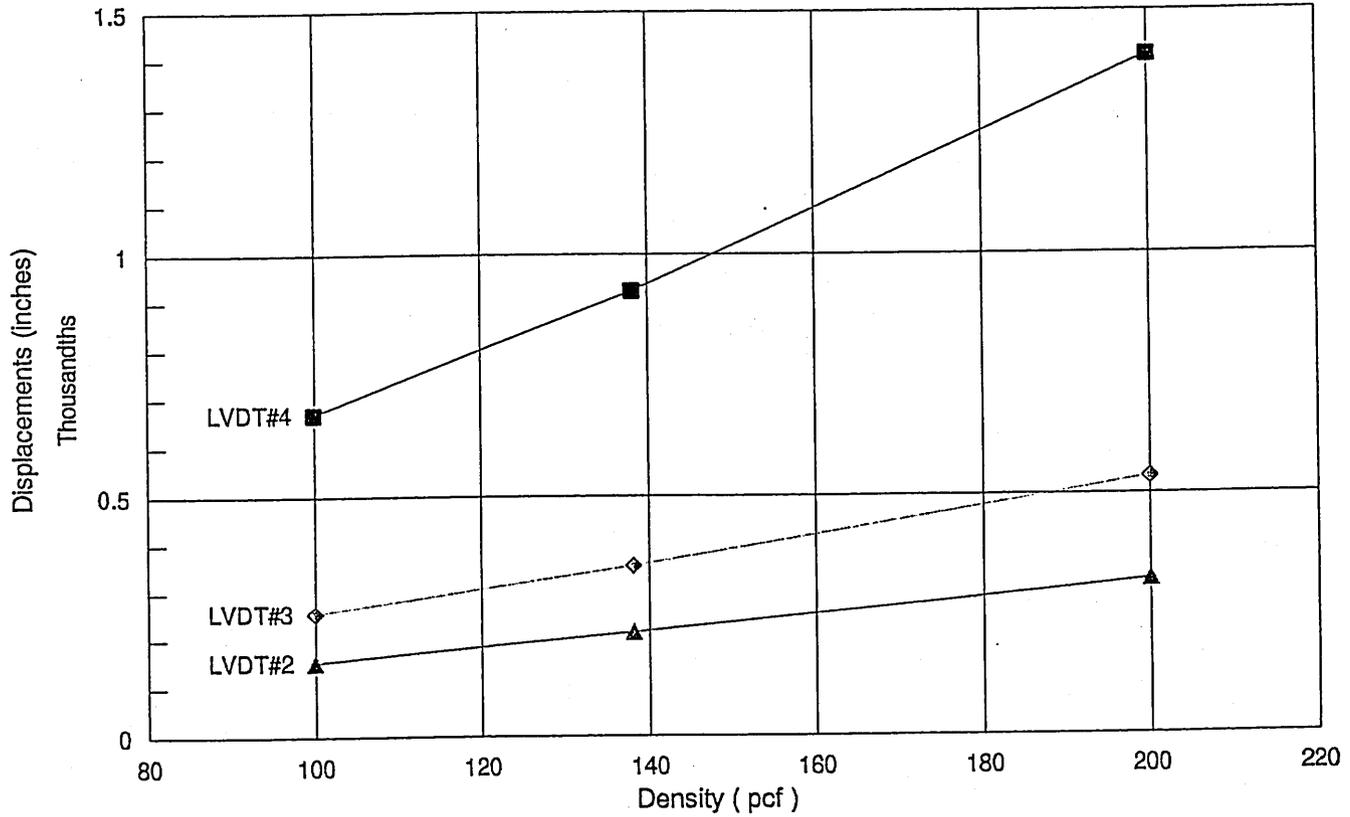
Uncracked Koyna Laboratory Study  
Sensitivity to Variation in Material Density  
Mesh#3

Material Properties

E = 300,000 psi  
Material Density = (100, 138, 200 pcf)

Damping = 3.5% critical  
Rayleigh Damping Factors  
Alpha = 1.954769; Beta = .000248

**Peak Displacements**  
Material Density Varied



E = 300 ksi

Peak Displacements ( inches )

	100	138.2	200	LAB
LVDT#4	6.7E-04	9.2E-04	1.4E-03	7.2E-04
LVDT#3	2.6E-04	3.6E-04	5.3E-04	3.1E-04
LVDT#2	1.5E-04	2.2E-04	3.2E-04	2.1E-04

Figure g45

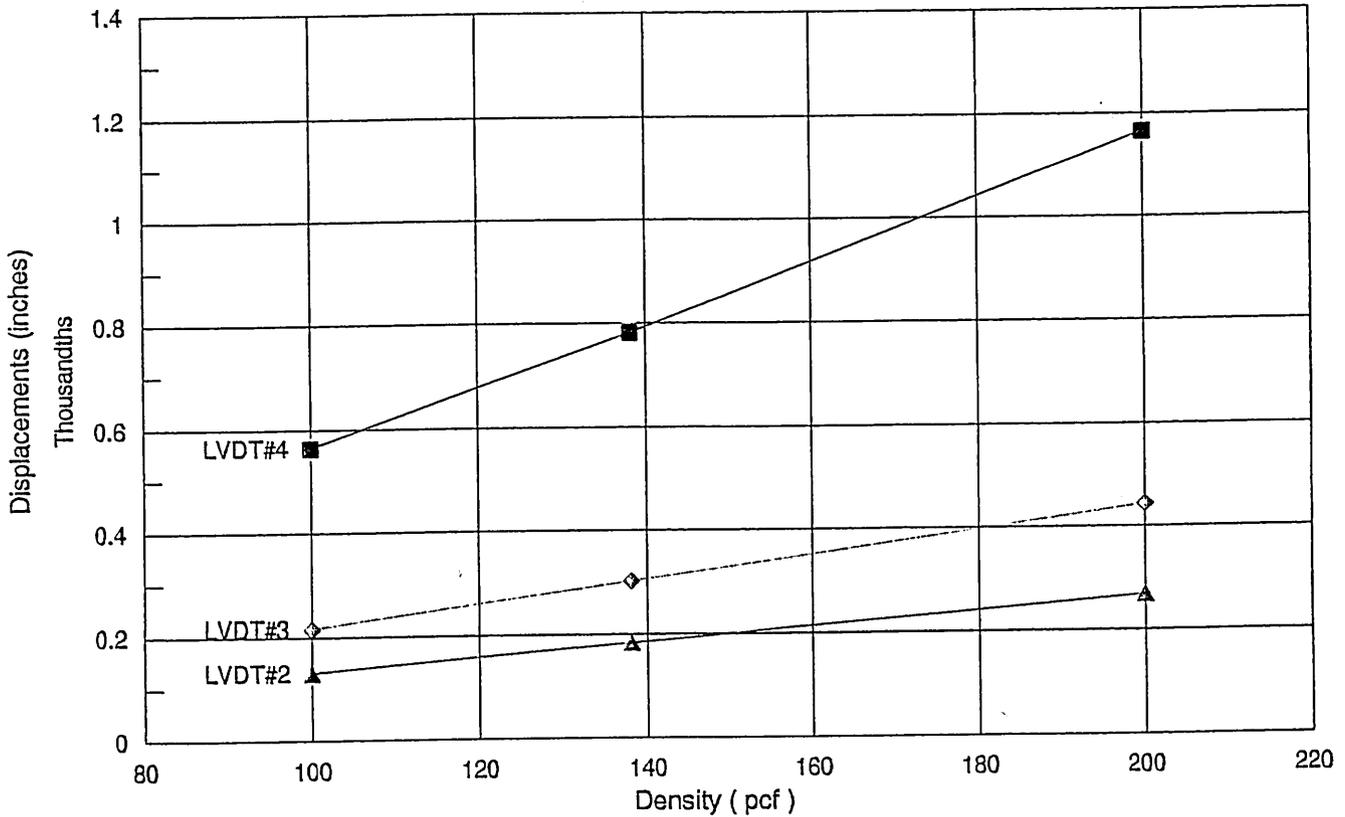
Uncracked Koyna Laboratory Study  
Sensitivity to Variation in Material Density  
Mesh#3

Material Properties

E = 350,000 psi  
Material Density = (100, 138, 200 pcf)

Damping = 3.5% critical  
Rayleigh Damping Factors  
Alpha = 1.954769; Beta = .000248

**Peak Displacements**  
Material Density Varied



E = 350 ksi

Peak Displacements ( inches )

	100	138.2	200	LAB
LVDT#4	5.6E-04	7.8E-04	1.2E-03	7.2E-04
LVDT#3	2.2E-04	3.0E-04	4.4E-04	3.1E-04
LVDT#2	1.3E-04	1.8E-04	2.7E-04	2.1E-04

Figure g46

# ABAQUS

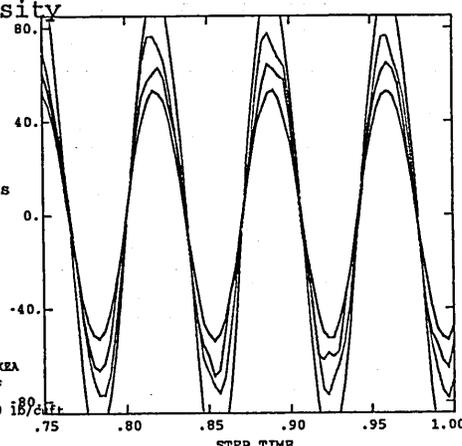
Material Density Varied

- DEN100\_176
- DEN138\_176
- DEN200\_176
- LAB7

Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model  
Acceleration  
at ACCEL#7  
E = 113 ksi

3.5% Critical Damping  
Input Freq=14 Hz File:SHAKEA  
Total Time : 279.75 to 280 sec

Densities 100, 138, & 200 lb/cu ft



ABAQUS Modal Dynamic Analyses vs Laboratory Measurements (LAB)

# ABAQUS

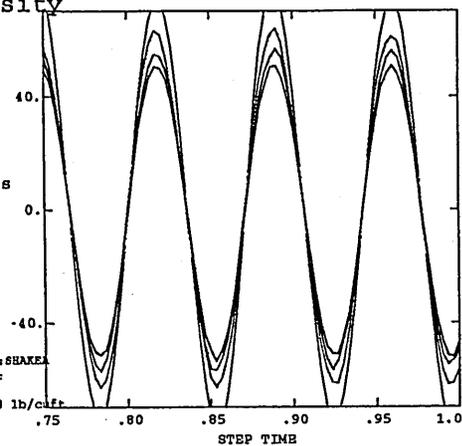
Material Density Varied

- DEN100\_204
- DEN138\_204
- DEN200\_204
- LAB6

Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model  
Acceleration  
at ACCEL#6  
E = 113 ksi

3.5% Critical Damping  
Input Freq=14 Hz File:SHAKEA  
Total Time : 279.75 to 280 sec

Densities 100, 138, & 200 lb/cu ft



ABAQUS Modal Dynamic Analyses vs Laboratory Measurements (LAB)

# ABAQUS

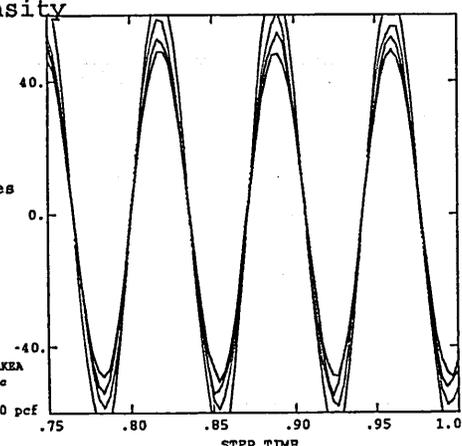
Material Density Varied

- DEN100\_491
- DEN138\_491
- DEN200\_491
- LAB5

Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model  
Acceleration  
at ACCEL#5  
E = 113 ksi

3.5% Critical Damping  
Input Freq=14 Hz File:SHAKEA  
Total Time : 279.75 to 280 sec

Densities 100, 138, & 200 pcf



ABAQUS Modal Dynamic Analyses vs Laboratory Measurements (LAB)

# ABAQUS

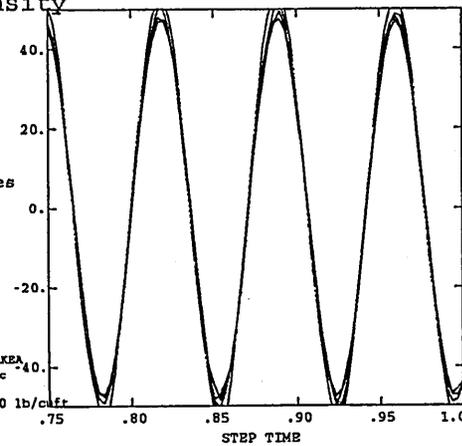
Material Density Varied

- DEN100\_519
- DEN138\_519
- DEN200\_519
- LAB4

Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model  
Acceleration  
at ACCEL#4  
E = 113 ksi

3.5% Critical Damping  
Input Freq=14 Hz File:SHAKEA  
Total Time : 279.75 to 280 sec

Densities 100, 138, & 200 lb/cu ft

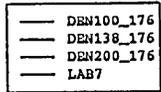


ABAQUS Modal Dynamic Analyses vs Laboratory Measurements (LAB)

Figure 947

# ABAQUS

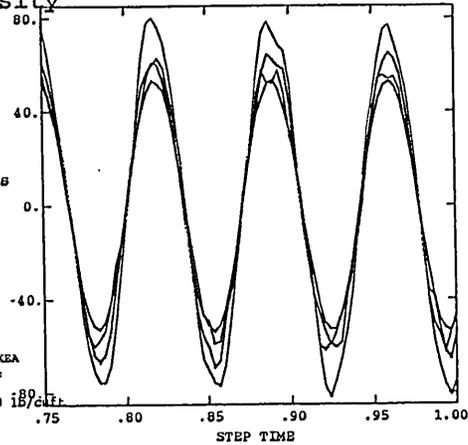
Material Density Varied



Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model  
Acceleration  
at ACCEL#7  
E = 157 ksi

3.5% Critical Damping  
Input Freq=14 Hz File:SHAKEA  
Total Time : 279.75 to 280 sec

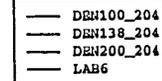
Densitys 100, 138, & 200 lb/cuft



ABAQUS Modal Dynamic Analyses vs Laboratory Measurements (LAB)

# ABAQUS

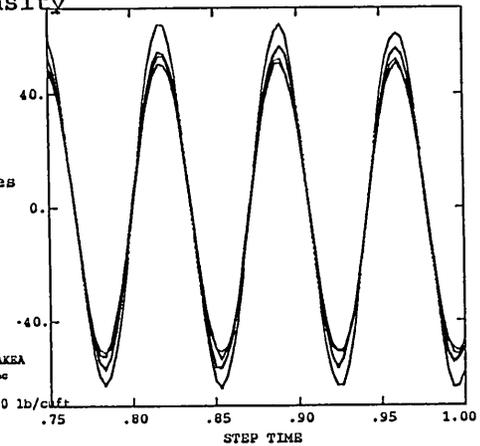
Material Density Varied



Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model  
Acceleration  
at ACCEL#6  
E = 157 ksi

3.5% Critical Damping  
Input Freq=14 Hz File:SHAKEA  
Total Time : 279.75 to 280 sec

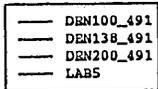
Densitys 100, 138, & 200 lb/cuft



ABAQUS Modal Dynamic Analyses vs Laboratory Measurements (LAB)

# ABAQUS

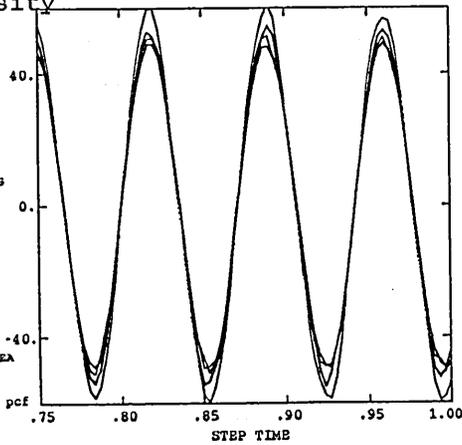
Material Density Varied



Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model  
Acceleration  
at ACCEL#5  
E = 157 psi

3.5% Critical Damping  
Input Freq=14 Hz File:SHAKEA  
Total Time : 279.75 to 280 sec

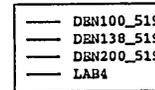
Densitys 100, 138, & 200 pcf



ABAQUS Modal Dynamic Analyses vs Laboratory Measurements (LAB)

# ABAQUS

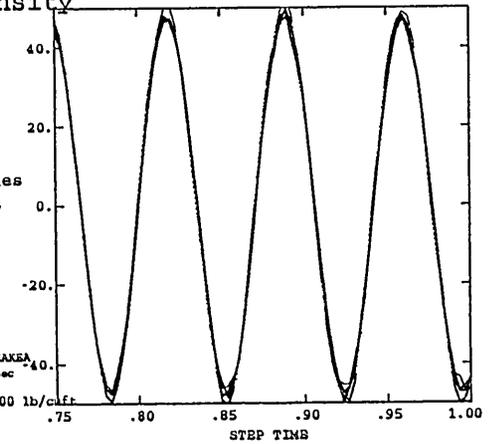
Material Density Varied



Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model  
Acceleration  
at ACCEL#4  
E = 157 ksi

3.5% Critical Damping  
Input Freq=14 Hz File:SHAKEA  
Total Time : 279.75 to 280 sec

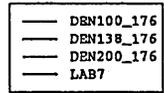
Densitys 100, 138, & 200 lb/cuft



ABAQUS Modal Dynamic Analyses vs Laboratory Measurements (LAB)

# ABAQUS

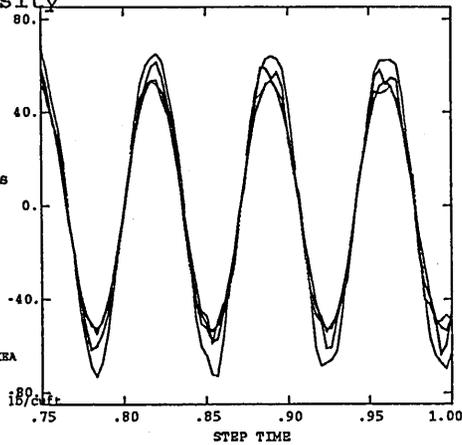
Material Density Varied



Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model  
Acceleration  
at ACCEL#7  
E = 200 ksi

3.5% Critical Damping  
Input Freq=14 Hz File:SHAKEA  
Total Time : 279.75 to 280 sec

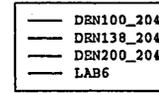
Densitys 100, 138, & 200 lb/cu ft



ABAQUS Modal Dynamic Analyses vs Laboratory Measurements (LAB)

# ABAQUS

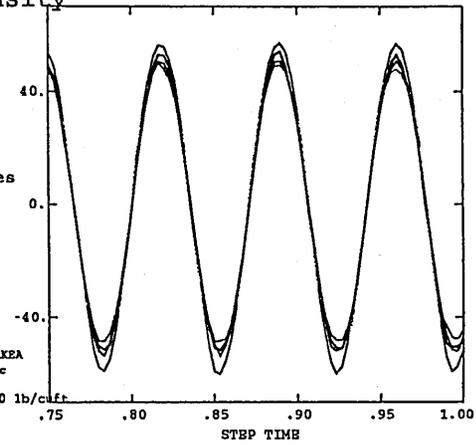
Material Density Varied



Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model  
Acceleration  
at ACCEL#6  
E = 200 ksi

3.5% Critical Damping  
Input Freq=14 Hz File:SHAKEA  
Total Time : 279.75 to 280 sec

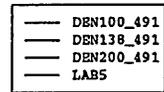
Densitys 100, 138, & 200 lb/cu ft



ABAQUS Modal Dynamic Analyses vs Laboratory Measurements (LAB)

# ABAQUS

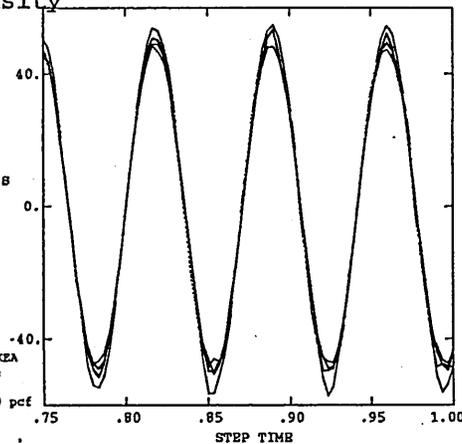
Material Density Varied



Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model  
Acceleration  
at ACCEL#5  
E = 200 ksi

3.5% Critical Damping  
Input Freq=14 Hz File:SHAKEA  
Total Time : 279.75 to 280 sec

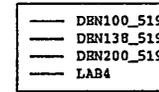
Densitys 100, 138, & 200 pcf



ABAQUS Modal Dynamic Analyses vs Laboratory Measurements (LAB)

# ABAQUS

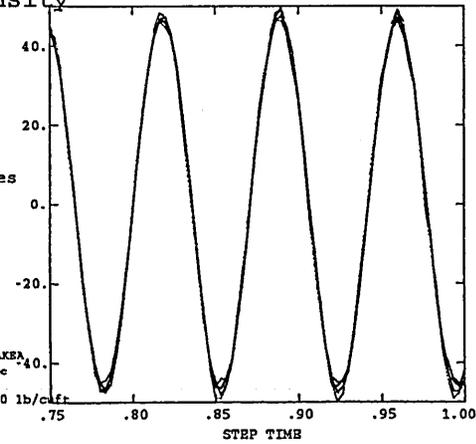
Material Density Varied



Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model  
Acceleration  
at ACCEL#4  
E = 200 ksi

3.5% Critical Damping  
Input Freq=14 Hz File:SHAKEA  
Total Time : 279.75 to 280 sec

Densitys 100, 138, & 200 lb/cu ft

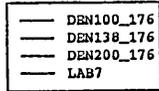


ABAQUS Modal Dynamic Analyses vs Laboratory Measurements (LAB)

Figure g49

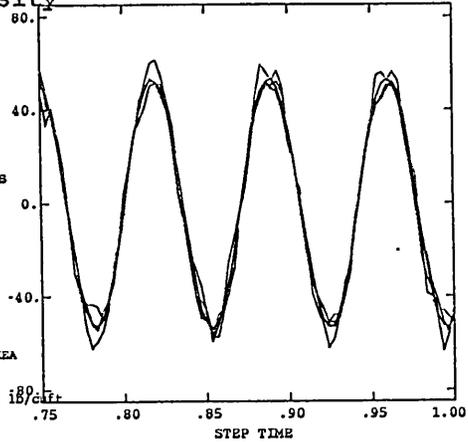
# ABAQUS

Material Density Varied



Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model  
Acceleration  
at ACCEL#7  
E = 300 ksi

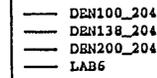
3.5% Critical Damping  
Input Freq=14 Hz File:SHAKEA  
Total Time : 279.75 to 280 sec  
Densitys 100, 138, & 200 lb/cu ft



ABAQUS Modal Dynamic Analyses vs Laboratory Measurements (LAB)

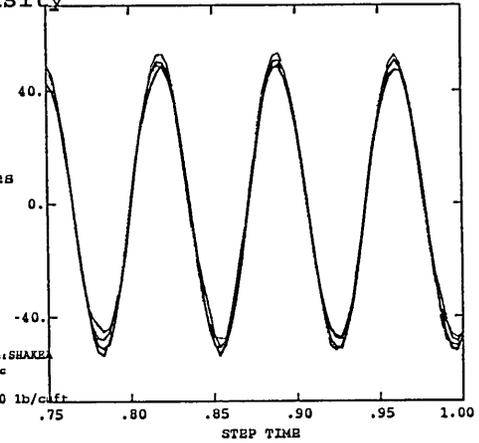
# ABAQUS

Material Density Varied



Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model  
Acceleration  
at ACCEL#6  
E = 300 ksi

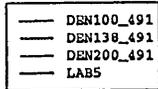
3.5% Critical Damping  
Input Freq=14 Hz Filename:SHAKEA  
Total Time : 279.75 to 280 sec  
Densitys 100, 138, & 200 lb/cu ft



ABAQUS Modal Dynamic Analyses vs Laboratory Measurements (LAB)

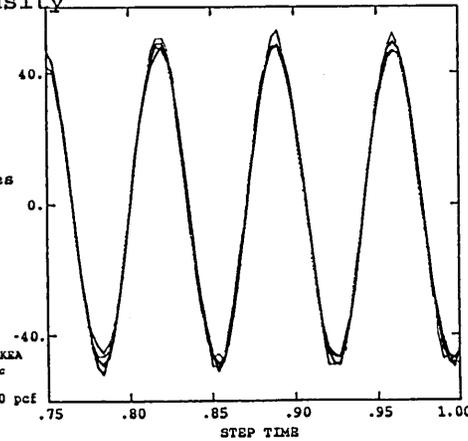
# ABAQUS

Material Density Varied



Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model  
Acceleration  
at ACCEL#5  
E = 300 ksi

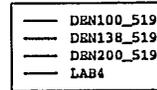
3.5% Critical Damping  
Input Freq=14 Hz File:SHAKEA  
Total Time : 279.75 to 280 sec  
Densitys 100, 138, & 200 pcf



ABAQUS Modal Dynamic Analyses vs Laboratory Measurements (LAB)

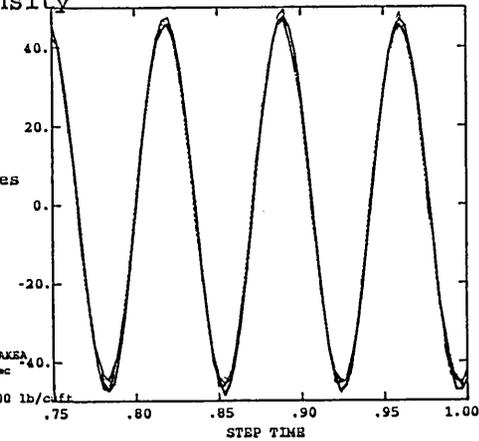
# ABAQUS

Material Density Varied



Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model  
Acceleration  
at ACCEL#4  
E = 300 ksi

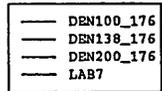
3.5% Critical Damping  
Input Freq=14 Hz File:SHAKEA  
Total Time : 279.75 to 280 sec  
Densitys 100, 138, & 200 lb/cu ft



ABAQUS Modal Dynamic Analyses vs Laboratory Measurements (LAB)

# ABAQUS

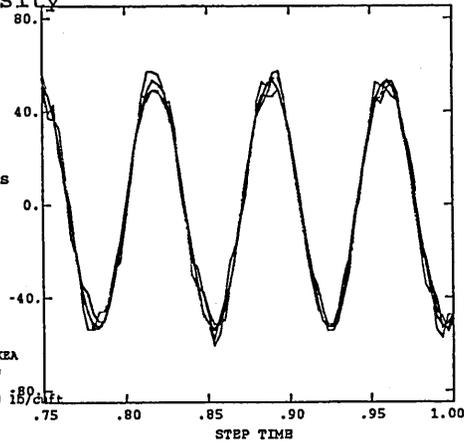
Material Density Varied



Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model  
Acceleration  
at ACCEL#7  
E = 350 ksi

3.5% Critical Damping  
Input Freq=14 Hz File:SHAKEA  
Total Time : 279.75 to 280 sec

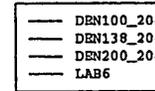
Densitys 100, 138, & 200 lb/cuft



ABAQUS Modal Dynamic Analyses vs Laboratory Measurements (LAB)

# ABAQUS

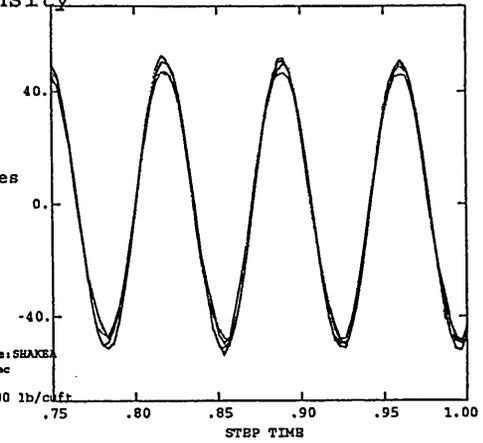
Material Density Varied



Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model  
Acceleration  
at ACCEL#6  
E = 350 ksi

3.5% Critical Damping  
Input Freq=14 Hz Filename:SHAKEA  
Total Time : 279.75 to 280 sec

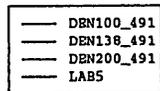
Densitys 100, 138, & 200 lb/cuft



ABAQUS Modal Dynamic Analyses vs Laboratory Measurements (LAB)

# ABAQUS

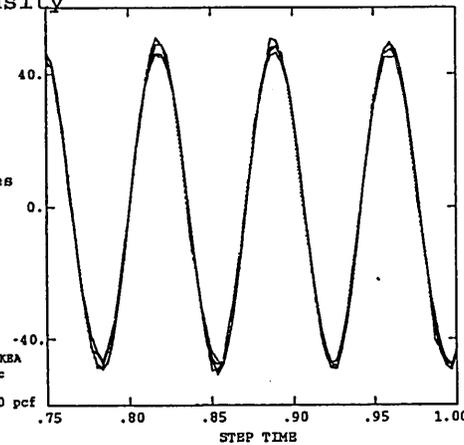
Material Density Varied



Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model  
Acceleration  
at ACCEL#5  
E = 350 ksi

3.5% Critical Damping  
Input Freq=14 Hz File:SHAKEA  
Total Time : 279.75 to 280 sec

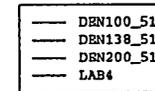
Densitys 100, 138, & 200 pcf



ABAQUS Modal Dynamic Analyses vs Laboratory Measurements (LAB)

# ABAQUS

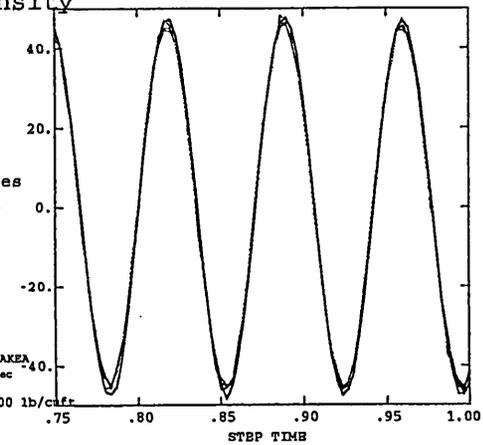
Material Density Varied



Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model  
Acceleration  
at ACCEL#4  
E = 350 ksi

3.5% Critical Damping  
Input Freq=14 Hz File:SHAKEA  
Total Time : 279.75 to 280 sec

Densitys 100, 138, & 200 lb/cuft



ABAQUS Modal Dynamic Analyses vs Laboratory Measurements (LAB)

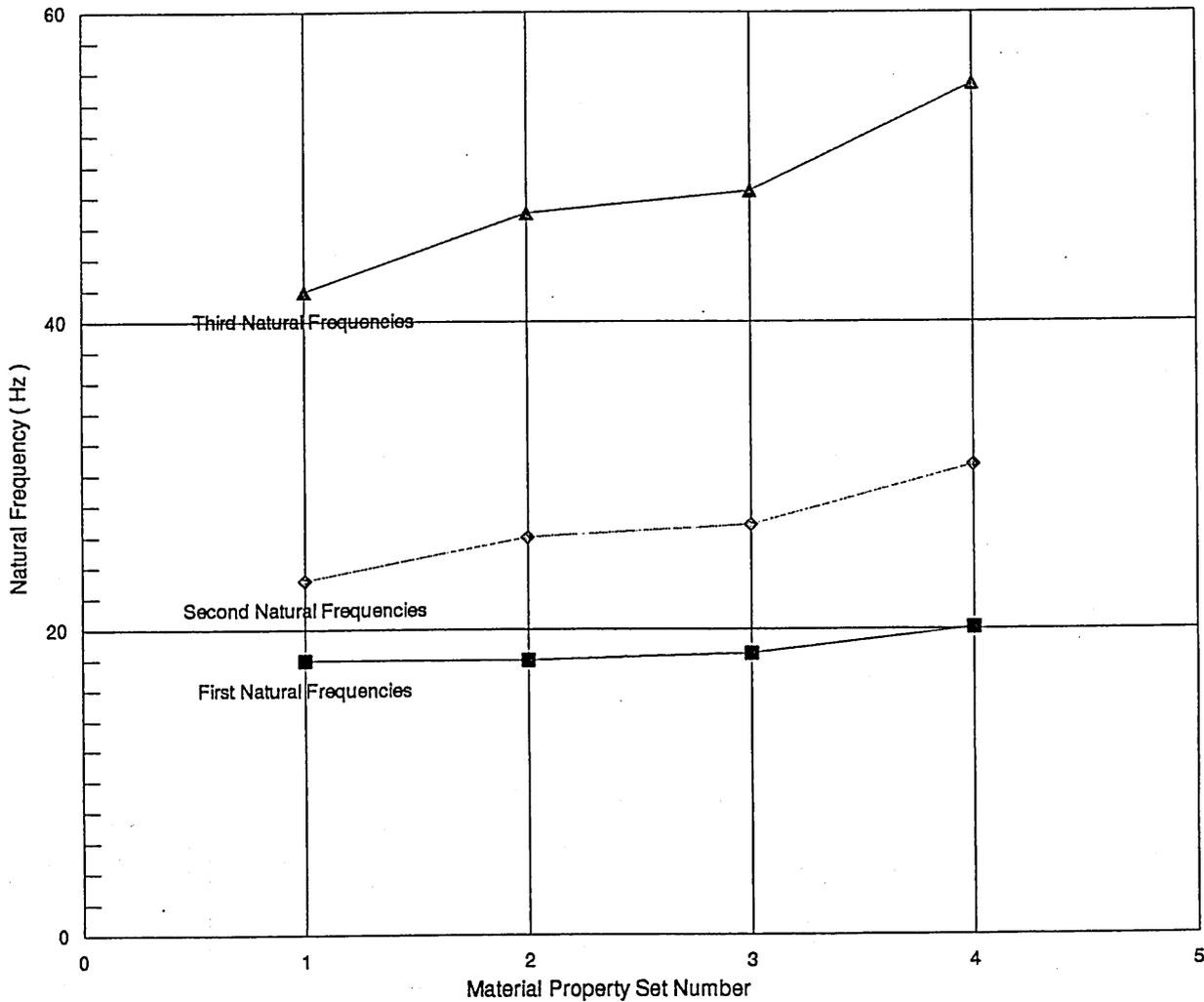
**Appendix H : Sensitivity to the  
Amount and Method of Applying  
Damping in the ABAQUS Analyses**

Uncracked Koyna Laboratory Study  
Sensitivity to Variation in Percent Critical Damping  
Mesh#3

Material Property Sets

Linear Elastic Material Property Set #1 : Elastic Modulus = 190 ksi; Material Density = 133 pcf  
 Linear Elastic Material Property Set #2 : Elastic Modulus = 200 ksi; Material Density = 140 pcf  
 Linear Elastic Material Property Set #3 : Elastic Modulus = 210 ksi; Material Density = 140 pcf  
 Linear Elastic Material Property Set #4 : Elastic Modulus = 250 ksi; Material Density = 140 pcf

**Natural Frequencies**  
For Material Property Sets #1-#4



Natural Frequencies (Hz)					
Material Property Set #	1	2	3	4	LAB
Mode 1	18.0	18.0	18.4	20.1	18.0
Mode 2	23.2	26.0	26.8	30.6	24.0
Mode 3	41.9	47.0	48.4	55.4	30.0

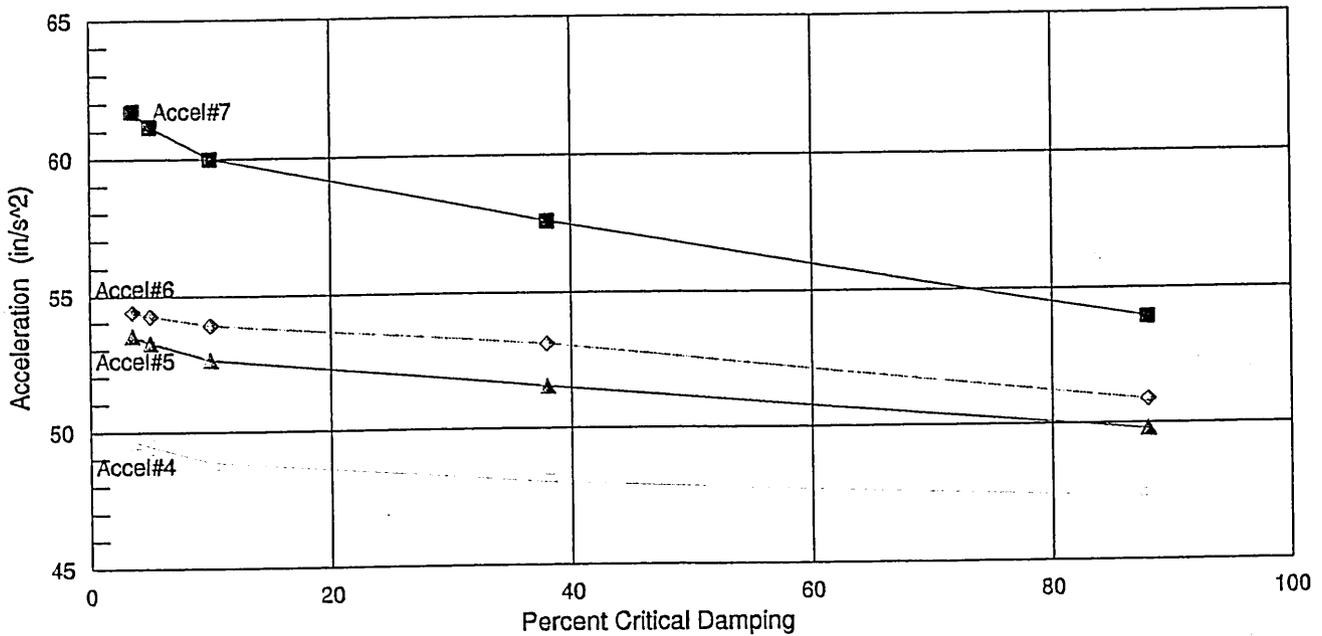
Figure h1

Uncracked Koyna Laboratory Study  
Sensitivity to Variation in Percent Critical Damping  
Mesh#3

Modal Damping = ( 3.5%, 5%, 10%, 38% & 88% ) critical

Linear Elastic Material Property Set #1 : Elastic Modulus = 190 ksi; Material Density = 133 pcf

**Peak Accelerations**  
Percent Critical Damping Varied



Peak Accelerations ( inch / sec ^ 2 )

Percent Damping	3.5	5	10	38	88	LAB
Accel#7	61.73	61.17	59.99	57.60	53.90	53.26
Accel#6	54.39	54.23	53.88	53.07	50.87	51.72
Accel#5	53.52	53.25	52.61	51.53	49.80	49.26
Accel#4	49.66	49.44	48.87	48.04	47.32	47.72
CPU seconds	278.83	278.65	278.89	268.59	267.18	

Figure h2

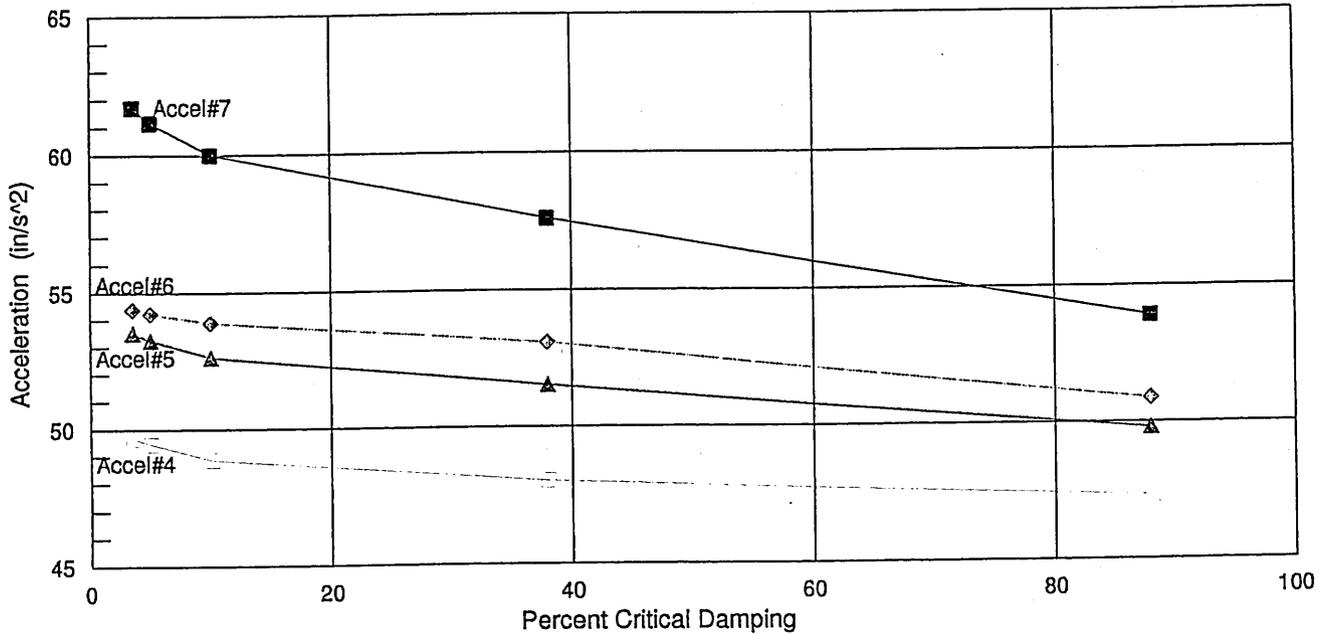
Uncracked Koyna Laboratory Study  
Sensitivity to Variation in Percent Critical Damping

Mesh#3

Modal Damping = ( 3.5%, 5%, 10%, 38%, & 88% ) critical

Linear Elastic Material Property Set #2 : Elastic Modulus = 200 ksi; Material Density = 140 pcf

**Peak Accelerations**  
Percent Critical Damping Varied



Peak Accelerations ( inch / sec ^ 2 )

Percent Damping	3.5	5	10	38	88	LAB
Accel#7	61.73	61.17	59.99	57.60	53.90	53.26
Accel#6	54.39	54.23	53.88	53.07	50.87	51.72
Accel#5	53.52	53.25	52.61	51.53	49.80	49.26
Accel#4	49.66	49.44	48.87	48.04	47.34	47.72

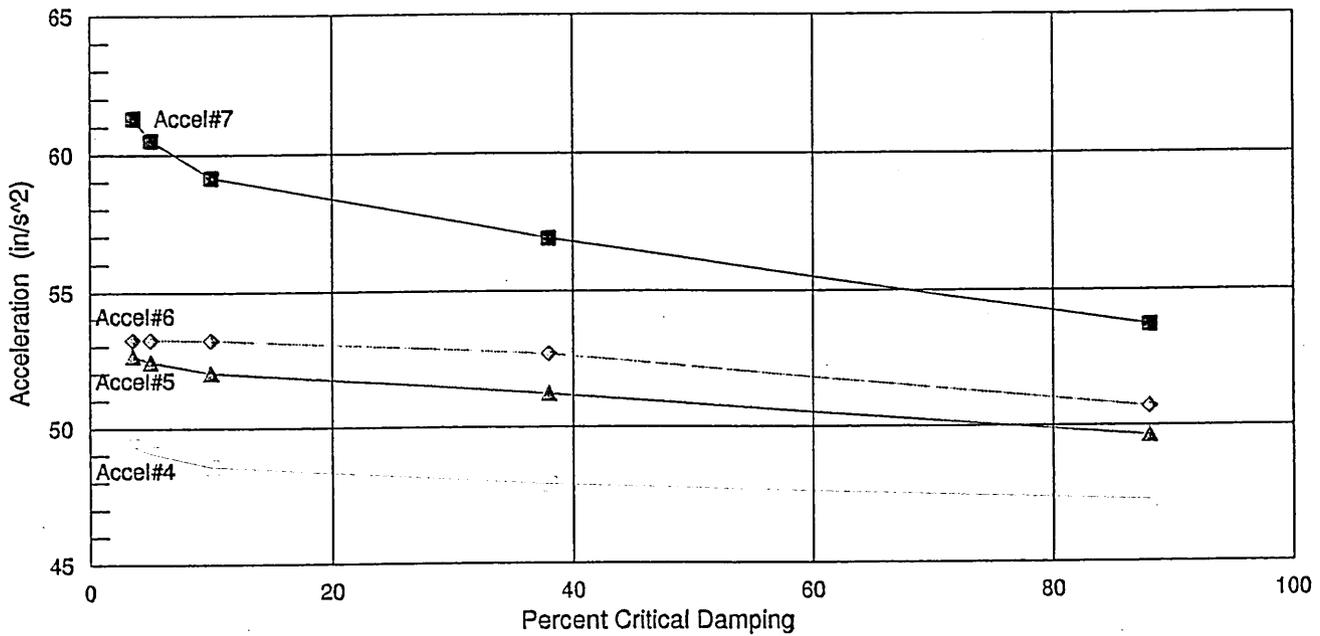
Figure h3

Uncracked Koyna Laboratory Study  
Sensitivity to Variation in Percent Critical Damping  
Mesh#3

Modal Damping = (3.5%,5%,10%,38%,&88%) critical

Linear Elastic Material Property Set #3 : Elastic Modulus = 210 ksi; Material Density = 140 pcf

**Peak Accelerations**  
Percent Critical Damping Varied



Peak Accelerations ( inch / sec ^ 2 )

Percent Damping	3.5	5	10	38	88	LAB
Accel#7	61.31	60.51	59.15	56.91	53.68	53.26
Accel#6	53.22	53.23	53.21	52.67	50.70	51.72
Accel#5	52.65	52.43	52.02	51.21	49.65	49.26
Accel#4	49.36	49.06	48.57	47.90	47.27	47.72

Figure h4

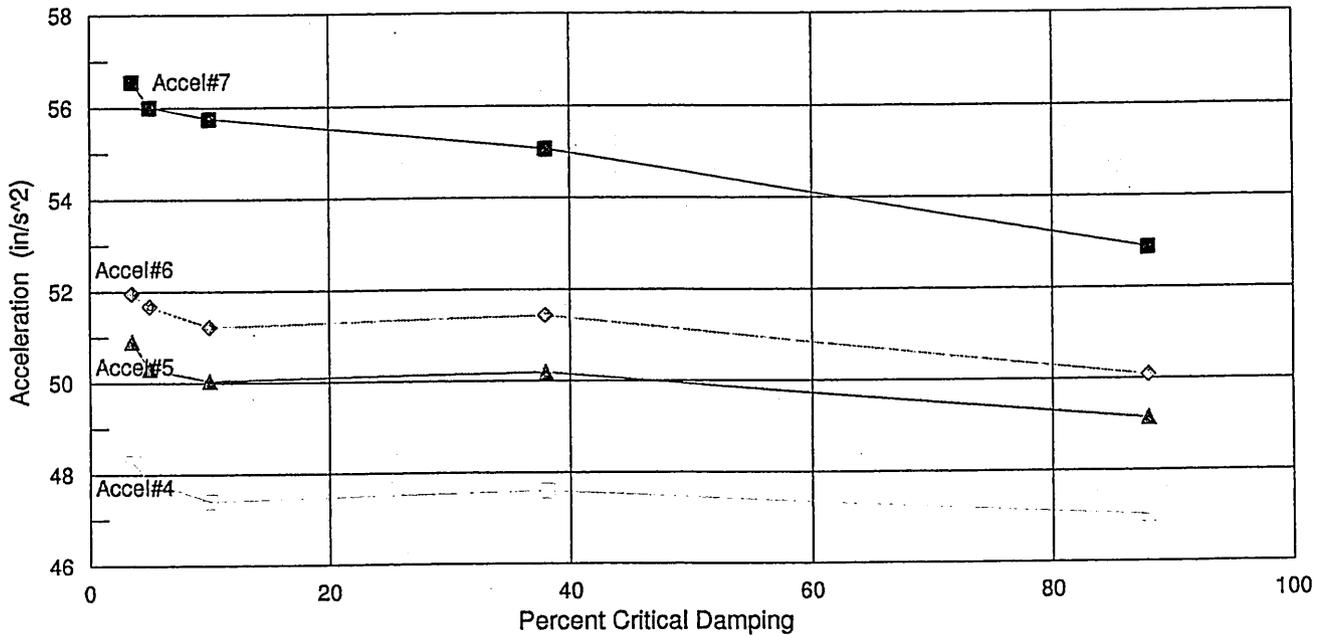
Uncracked Koyna Laboratory Study  
Sensitivity to Variation in Percent Critical Damping

Mesh#3

Modal Damping = ( 3.5%, 5%, 10%, 38% & 88% ) critical

Linear Elastic Material Property Set #4 : Elastic Modulus = 250 ksi; Material Density = 140 pcf

**Peak Accelerations**  
Percent Critical Damping Varied



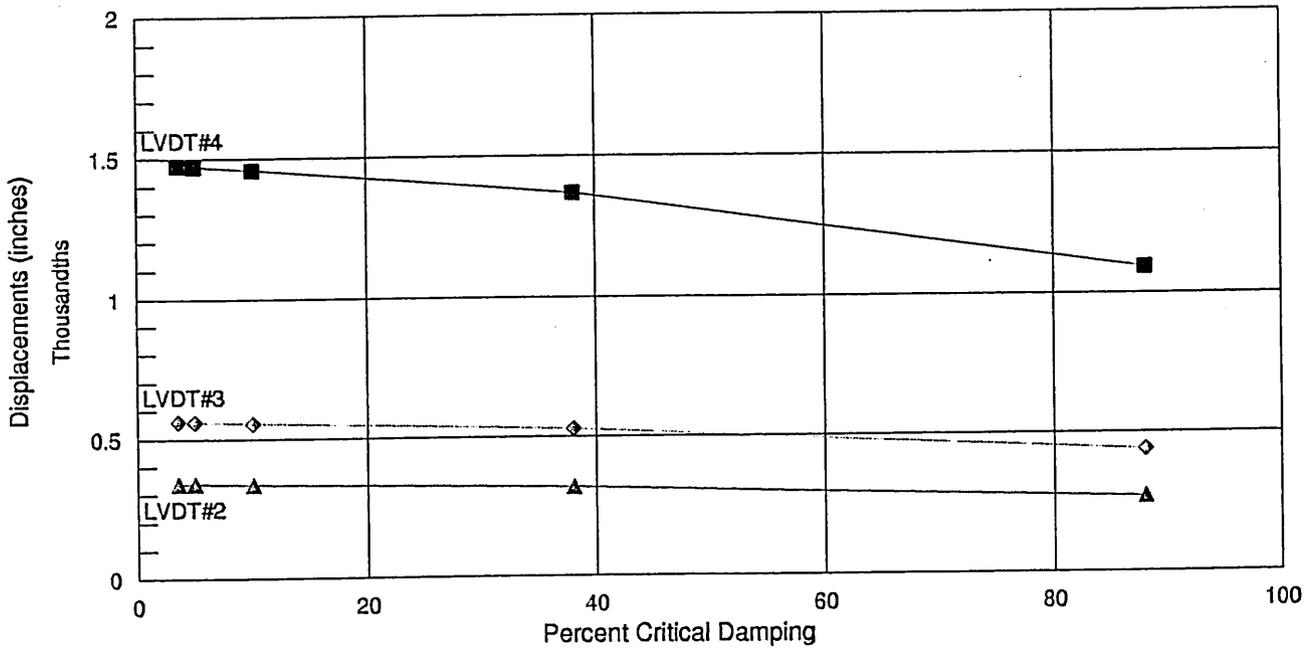
Peak Accelerations ( inch / sec ^ 2 )

Percent Damping	3.5	5	10	38	88	LAB
Accel#7	56.56	56.01	55.76	55.07	52.87	53.26
Accel#6	51.95	51.67	51.22	51.43	50.09	51.72
Accel#5	50.90	50.30	50.04	50.19	49.14	49.26
Accel#4	48.26	47.84	47.41	47.60	47.03	47.72

Uncracked Koyna Laboratory Study  
Sensitivity to Variation in Percent Critical Damping  
Mesh#3  
Modal Damping = (3.5%,5%,10%,38%,&88%) critical

Linear Elastic Material Property Set #1 : Elastic Modulus = 190 ksi; Material Density = 133 pcf

**Peak Displacements**  
Percent Critical Damping Varied



Peak Displacements ( inches )

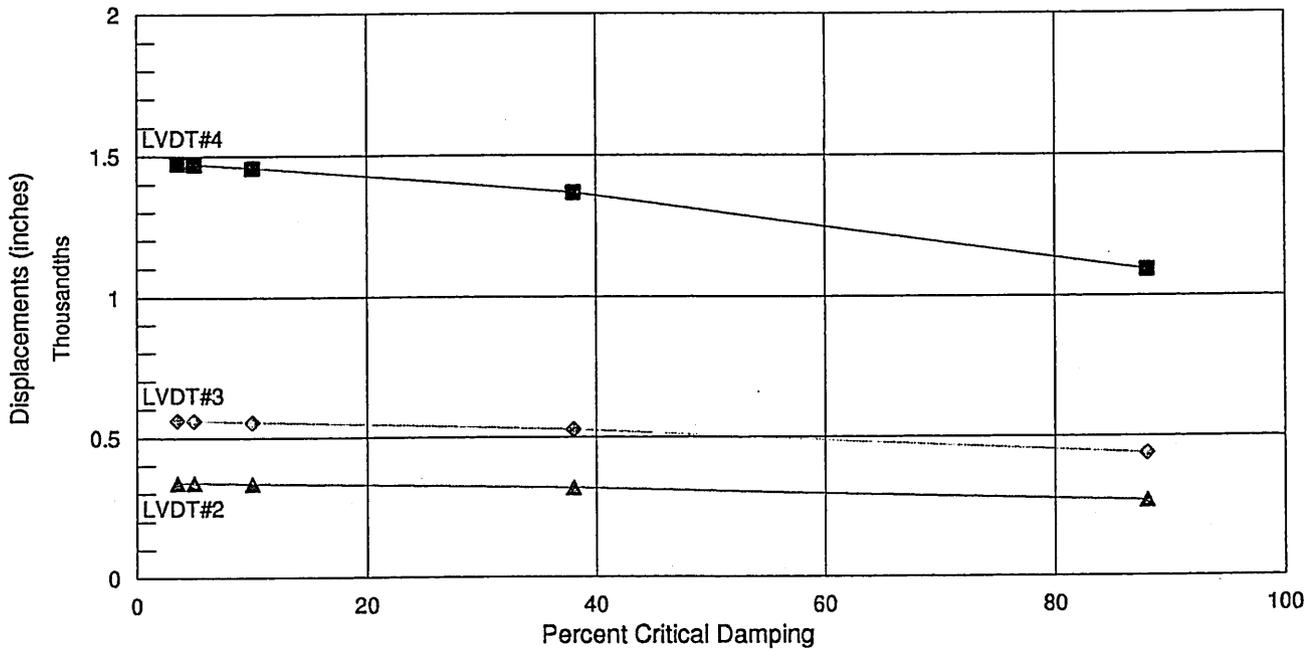
Percent Damping	3.5	5	10	38	88	LAB
LVDT#4	1.5E-03	1.5E-03	1.5E-03	1.4E-03	1.1E-03	7.8E-04
LVDT#3	5.6E-04	5.6E-04	5.5E-04	5.3E-04	4.4E-04	3.0E-04
LVDT#2	3.4E-04	3.4E-04	3.3E-04	3.2E-04	2.7E-04	1.8E-04
CPU seconds	278.83	278.65	278.89	268.59	267.18	

Figure h6

Uncracked Koyna Laboratory Study  
Sensitivity to Variation in Percent Critical Damping  
Mesh#3  
Modal Damping = (3.5%,5%,10%,38%,&88%) critical

Linear Elastic Material Property Set #2 : Elastic Modulus = 200 ksi; Material Density = 140 pcf

**Peak Displacements**  
Percent Critical Damping Varied



Peak Displacements ( inches )

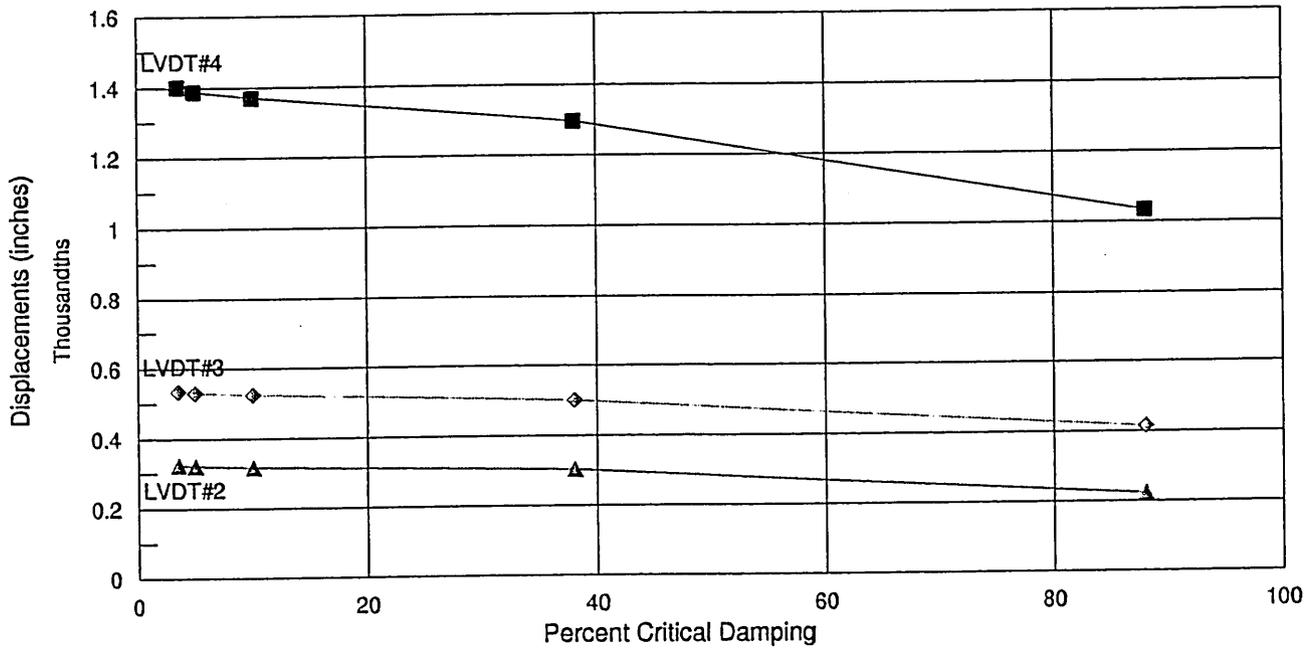
Percent Damping	3.5	5	10	38	88	LAB
LVDT#4	1.5E-03	1.5E-03	1.5E-03	1.4E-03	1.1E-03	7.8E-04
LVDT#3	5.6E-04	5.6E-04	5.5E-04	5.3E-04	4.4E-04	3.0E-04
LVDT#2	3.4E-04	3.4E-04	3.3E-04	3.2E-04	2.7E-04	1.8E-04

Figure h7

Uncracked Koyna Laboratory Study  
Sensitivity to Variation in Percent Critical Damping  
Mesh#3  
Modal Damping = (3.5%,5%,10%,38%,&88%) critical

Linear Elastic Material Property Set #3 : Elastic Modulus = 210 ksi; Material Density = 140 pcf

**Peak Displacements**  
Percent Critical Damping Varied



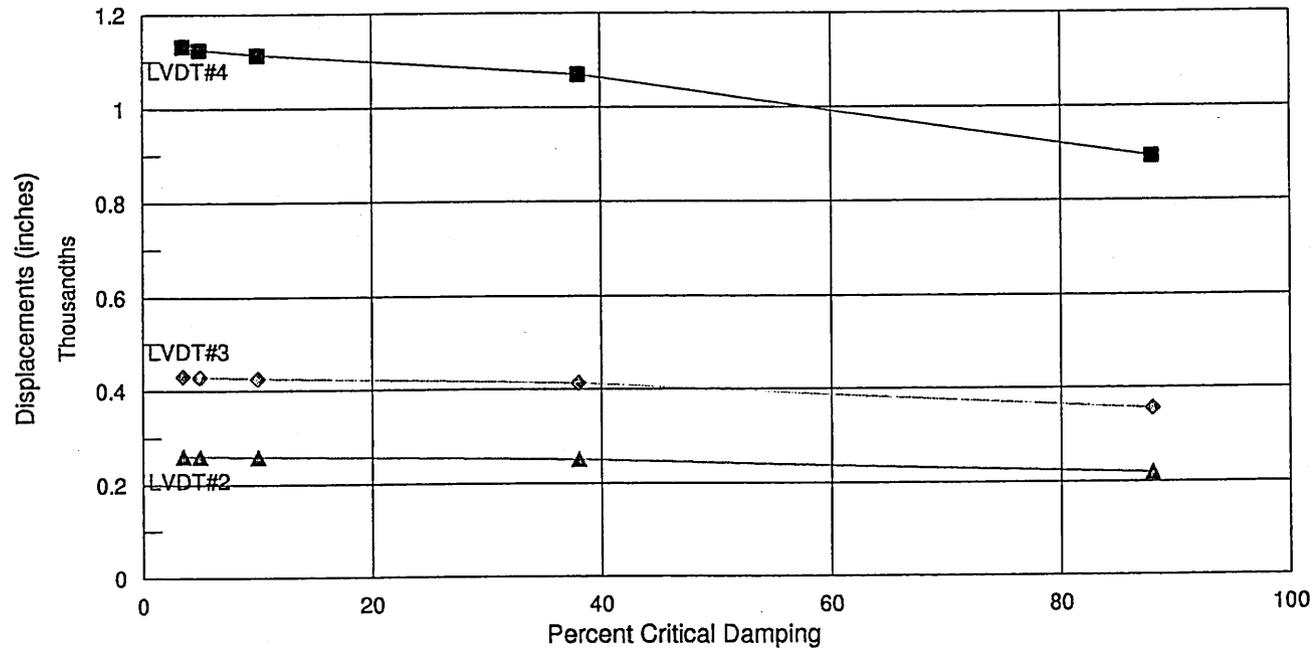
Peak Displacements ( inches )

Percent Damping	3.5	5	10	38	88	LAB
LVDT#4	1.4E-03	1.4E-03	1.4E-03	1.3E-03	1.0E-03	7.8E-04
LVDT#3	5.3E-04	5.3E-04	5.2E-04	5.0E-04	4.1E-04	3.0E-04
LVDT#2	3.2E-04	3.2E-04	3.2E-04	3.0E-04	2.2E-04	1.8E-04

Uncracked Koyna Laboratory Study  
Sensitivity to Variation in Percent Critical Damping  
Mesh#3  
Modal Damping = (3.5%,5%,10%,38%,&88%) critical

Linear Elastic Material Property Set #4 : Elastic Modulus = 250 ksi; Material Density = 140 pcf

**Peak Displacements**  
Percent Critical Damping Varied



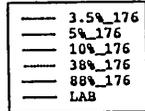
Peak Displacements ( inches )

Percent Damping	3.5	5	10	38	88	LAB
LVDT#4	1.1E-03	1.1E-03	1.1E-03	1.1E-03	8.9E-04	7.8E-04
LVDT#3	4.3E-04	4.3E-04	4.3E-04	4.1E-04	3.6E-04	3.0E-04
LVDT#2	2.6E-04	2.6E-04	2.6E-04	2.5E-04	2.2E-04	1.8E-04

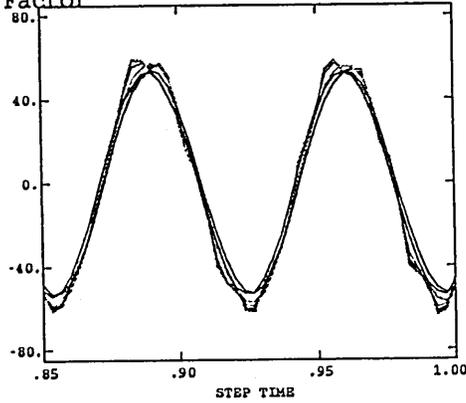
Figure h9

# ABAQUS

Modal Damping Factor  
Varied



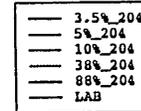
Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model  
Acceleration  
at ACCEL#7  
Elastic Modulus = 190 ksi  
Material Density = 133 pcf  
Filename: SHAKKA  
Total Time = 279.75 to 280 sec



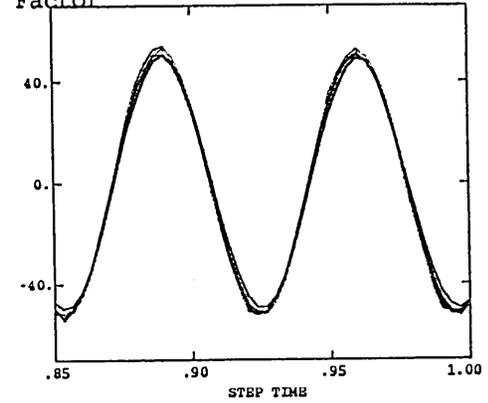
ABAQUS Modal Dynamic Analyses vs Laboratory Measurements

# ABAQUS

Modal Damping Factor  
Varied



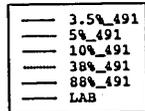
Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model  
Acceleration  
at ACCEL#6  
Material Density = 133 pcf  
Elastic Modulus = 190 ksi  
Filename: SHAKKA  
Total Time = 279.75 to 280 sec



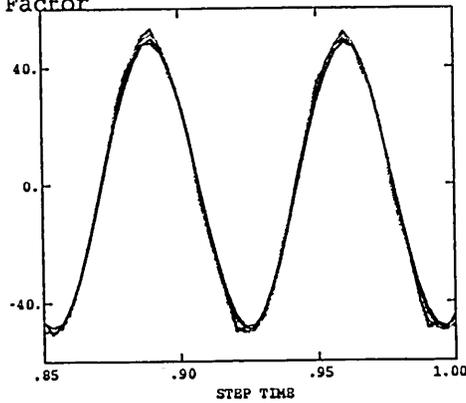
ABAQUS Modal Dynamic Analyses vs Laboratory Measurements

# ABAQUS

Modal Damping Factor  
Varied



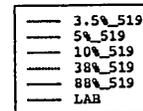
Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model  
Acceleration  
at ACCEL#5  
Elastic Modulus = 190 ksi  
Material Density = 133 pcf  
Filename: SHAKKA  
Total Time = 279.75 to 280 sec



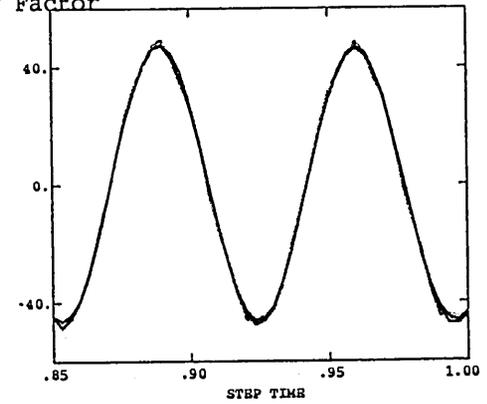
ABAQUS Modal Dynamic Analyses vs Laboratory Measurements

# ABAQUS

Modal Damping Factor  
Varied



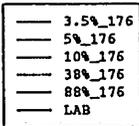
Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model  
Acceleration  
at ACCEL#4  
Elastic Modulus = 190 ksi  
Material Density = 133 pcf  
Filename: SHAKKA  
Total Time = 279.75 to 280 sec



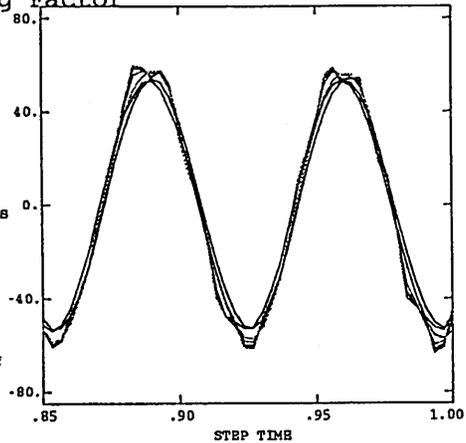
ABAQUS Modal Dynamic Analyses vs Laboratory Measurements

# ABAQUS

Modal Damping Factor  
Varied



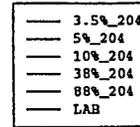
Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model  
Acceleration  
at ACCEL#7  
Elastic Modulus = 200 ksi  
Material Density = 140 pcf  
Filename:SHAKEA  
Total Time : 279.75 to 280 sec



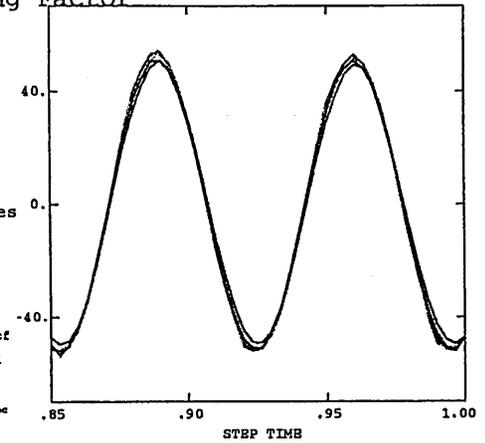
ABAQUS Modal Dynamic Analyses vs Laboratory Measurements

# ABAQUS

Modal Damping Factor  
Varied



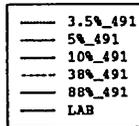
Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model  
Acceleration  
at ACCEL#6  
Material Density = 140 pcf  
Elastic Modulus = 200 ksi  
Filename:SHAKEA  
Total Time : 279.75 to 280 sec



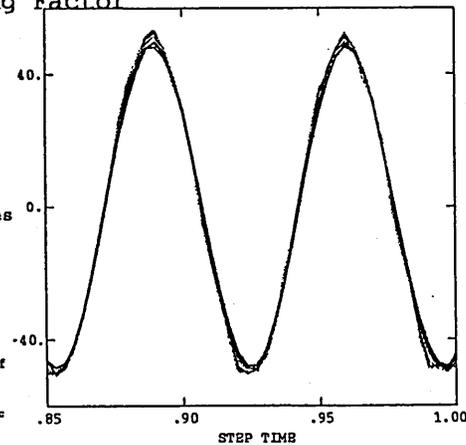
ABAQUS Modal Dynamic Analyses vs Laboratory Measurements

# ABAQUS

Modal Damping Factor  
Varied



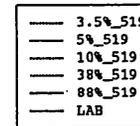
Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model  
Acceleration  
at ACCEL#5  
Elastic Modulus = 200 ksi  
Material Density = 140 pcf  
Filename:SHAKEA  
Total Time : 279.75 to 280 sec



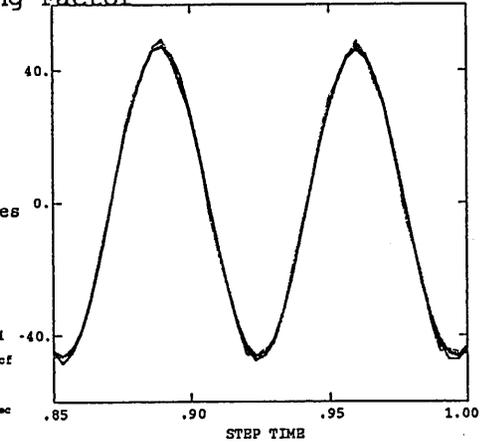
ABAQUS Modal Dynamic Analyses vs Laboratory Measurements

# ABAQUS

Modal Damping Factor  
Varied



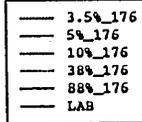
Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model  
Acceleration  
at ACCEL#4  
Elastic Modulus = 200 ksi  
Material Density = 140 pcf  
Filename:SHAKEA  
Total Time : 279.75 to 280 sec



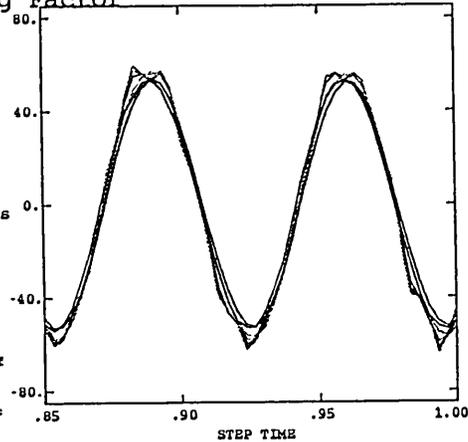
ABAQUS Modal Dynamic Analyses vs Laboratory Measurements

# ABAQUS

Modal Damping Factor  
Varied



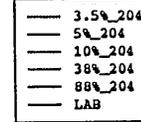
Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model  
Acceleration  
at ACCEL#7  
Elastic Modulus = 210 ksi  
Material Density = 140 pcf  
Filename:SHAKEA  
Total Time : 279.75 to 280 sec



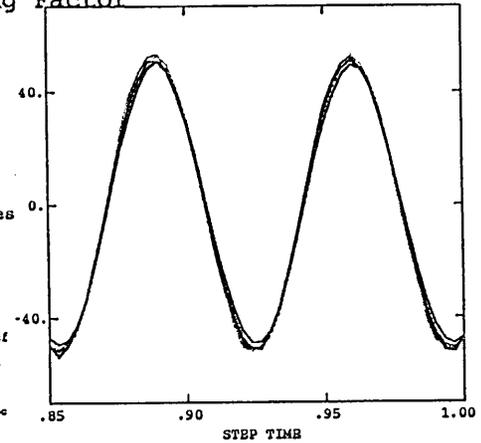
ABAQUS Modal Dynamic Analyses vs Laboratory Measurements

# ABAQUS

Modal Damping Factor  
Varied



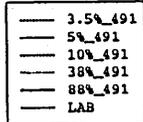
Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model  
Acceleration  
at ACCEL#6  
Material Density = 140 pcf  
Elastic Modulus = 210 ksi  
Filename:SHAKEA  
Total Time : 279.75 to 280 sec



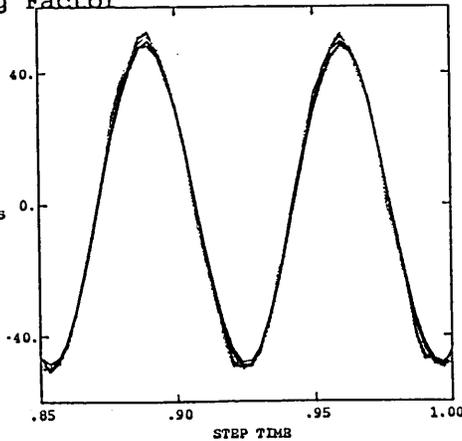
ABAQUS Modal Dynamic Analyses vs Laboratory Measurements

# ABAQUS

Modal Damping Factor  
Varied



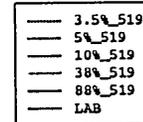
Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model  
Acceleration  
at ACCEL#5  
Elastic Modulus = 210 ksi  
Material Density = 140 pcf  
Filename:SHAKEA  
Total Time : 279.75 to 280 sec



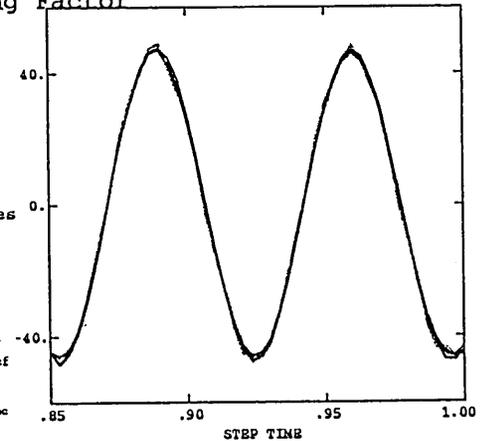
ABAQUS Modal Dynamic Analyses vs Laboratory Measurements

# ABAQUS

Modal Damping Factor  
Varied



Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model  
Acceleration  
at ACCEL#4  
Elastic Modulus = 210 ksi  
Material Density = 140 pcf  
Filename:SHAKEA  
Total Time : 279.75 to 280 sec

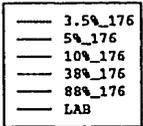


ABAQUS Modal Dynamic Analyses vs Laboratory Measurements

Figure h12

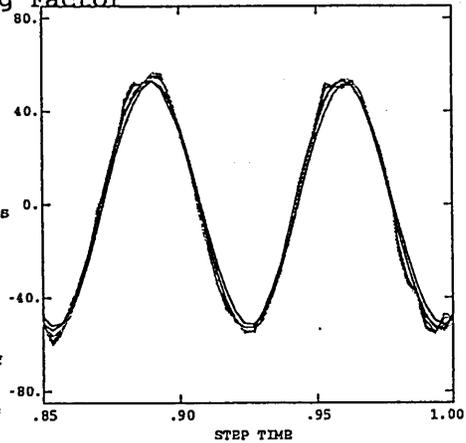
# ABAQUS

Modal Damping Factor  
Varied



Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model  
Acceleration  
at ACCEL#7

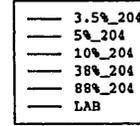
Elastic Modulus = 250 ksi  
Material Density = 140 pcf  
Filename:SHAKEA  
Total Time : 279.75 to 280 sec



ABAQUS Modal Dynamic Analyses vs Laboratory Measurements

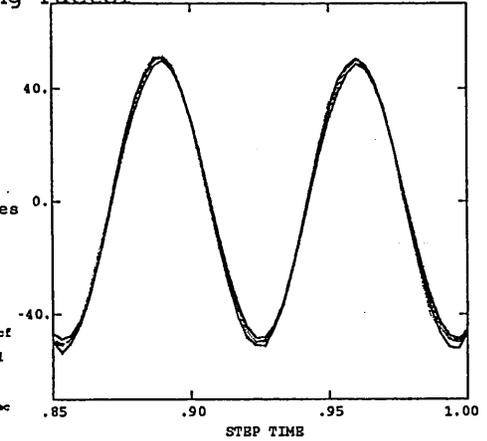
# ABAQUS

Modal Damping Factor  
Varied



Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model  
Acceleration  
at ACCEL#6

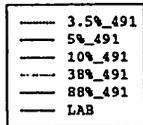
Material Density = 140 pcf  
Elastic Modulus = 250 ksi  
Filename:SHAKEA  
Total Time : 279.75 to 280 sec



ABAQUS Modal Dynamic Analyses vs Laboratory Measurements

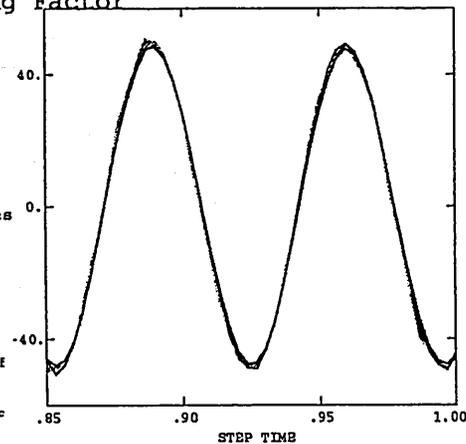
# ABAQUS

Modal Damping Factor  
Varied



Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model  
Acceleration  
at ACCEL#5

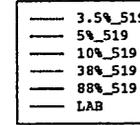
Elastic Modulus = 250 ksi  
Material Density = 140 pcf  
Filename:SHAKEA  
Total Time : 279.75 to 280 sec



ABAQUS Modal Dynamic Analyses vs Laboratory Measurements

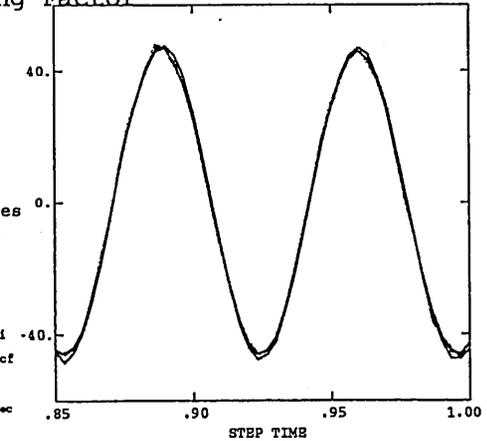
# ABAQUS

Modal Damping Factor  
Varied



Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model  
Acceleration  
at ACCEL#4

Elastic Modulus = 250 ksi  
Material Density = 140 pcf  
Filename:SHAKEA  
Total Time : 279.75 to 280 sec



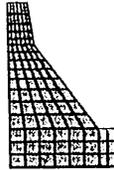
ABAQUS Modal Dynamic Analyses vs Laboratory Measurements

# ABAQUS

Koyna Laboratory Model Study  
 Uncracked Model Study  
 Sensitivity Study  
 Variation of Modal Damping

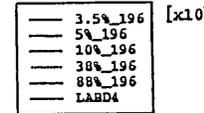
Comparison of Displacements  
 ABAQUS STANDARD  
 Modal Dynamic Analysis

Input Record SHAKEA  
 Elastic Modulus = 190 ksi  
 Density = 133.0 pcf  
 Mesh # 3

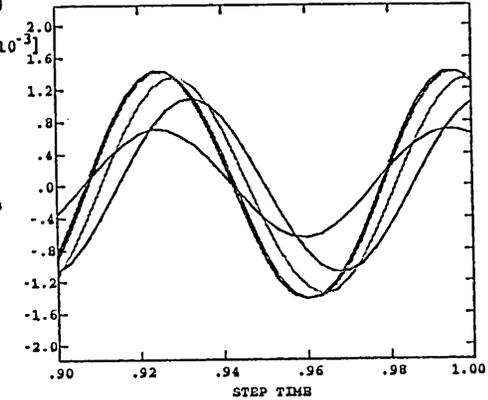


# ABAQUS

Modal Damping



Linear Elastic  
 Material Properties  
 STANDARD Analyses  
 Uncracked Model  
 Displacement  
 at LVDT#4

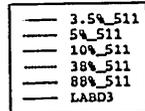


Total Time = 279.90 to 280 sec

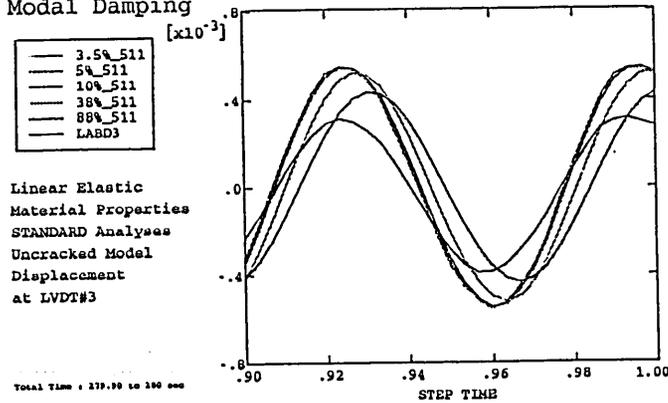
ABAQUS Modal Dynamic Analyses & Laboratory Measurements

# ABAQUS

Modal Damping



Linear Elastic  
 Material Properties  
 STANDARD Analyses  
 Uncracked Model  
 Displacement  
 at LVDT#3

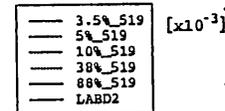


Total Time = 279.90 to 280 sec

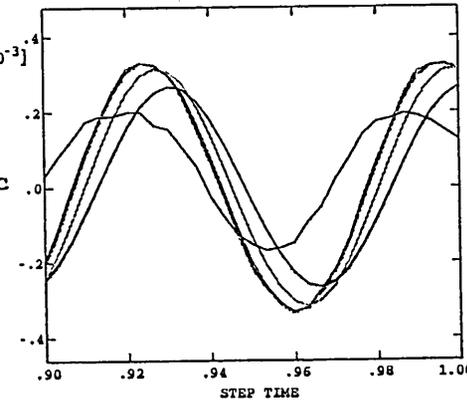
ABAQUS Modal Dynamic Analyses & Laboratory Measurements

# ABAQUS

Modal Damping



Linear Elastic  
 Material Properties  
 STANDARD Analyses  
 Uncracked Model  
 Acceleration  
 at LVDT#2



Total Time = 279.90 to 280 sec

ABAQUS Modal Dynamic Analyses & Laboratory Measurements

Figure h14

# ABAQUS

Koyna Laboratory Model Study  
 Uncracked Model Study  
 Sensitivity Study  
 Variation of Modal Damping

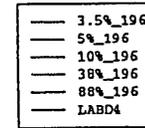
Comparison of Displacement  
 ABAQUS STANDARD  
 Modal Dynamic Analysis

Input Record SHAKEA  
 Elastic Modulus = 200 ksi  
 Density = 140.0 pcf  
 Mesh # 3

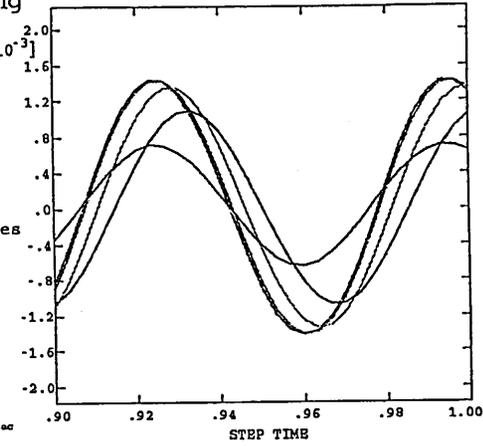


# ABAQUS

Modal Damping



Linear Elastic  
 Material Properties  
 STANDARD Analyses  
 Uncracked Model  
 Displacement  
 at LVDT#4

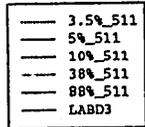


Total Time : 279.90 to 280 sec

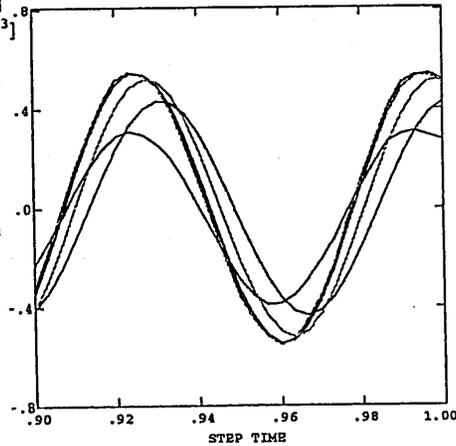
ABAQUS Modal Dynamic Analyses & Laboratory Measurements

# ABAQUS

Modal Damping



Linear Elastic  
 Material Properties  
 STANDARD Analyses  
 Uncracked Model  
 Displacement  
 at LVDT#3

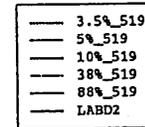


Total Time : 279.90 to 280 sec

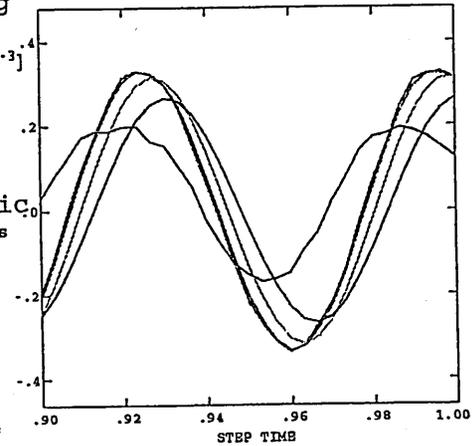
ABAQUS Modal Dynamic Analyses & Laboratory Measurements

# ABAQUS

Modal Damping



Linear Elastic  
 Material Properties  
 STANDARD Analyses  
 Uncracked Model  
 Acceleration  
 at LVDT#2



Total Time : 279.90 to 280 sec

ABAQUS Modal Dynamic Analyses & Laboratory Measurements

Figure h15

# ABAQUS

Koyna Laboratory Model Study  
 Uncracked Model Study  
 Sensitivity Study  
 Variation of Modal Damping

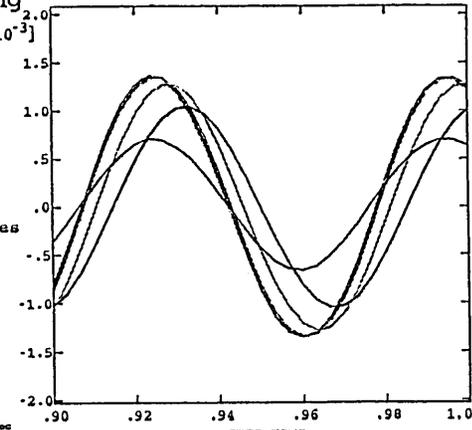
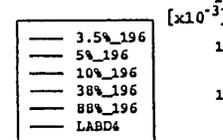
Comparison of Displacement  
 ABAQUS STANDARD  
 Modal Dynamic Analysis

Input Record SHAKEA  
 Elastic Modulus = 210 ksi  
 Density = 140.0 pcf  
 Mesh # 3



# ABAQUS

Modal Damping



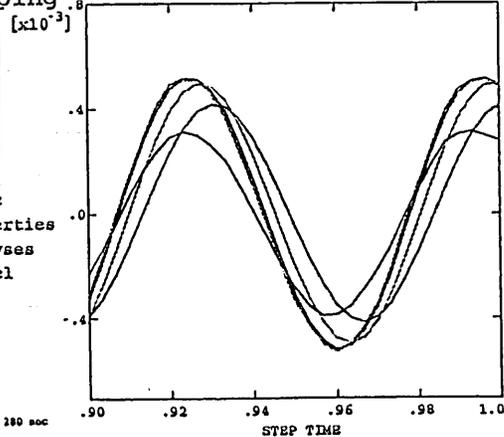
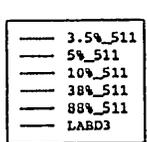
Total Time : 279.90 to 280 sec

ABAQUS Modal Dynamic Analyses & Laboratory Measurements

Linear Elastic  
 Material Properties  
 STANDARD Analyses  
 Uncracked Model  
 Displacement  
 at LVDT#4

# ABAQUS

Modal Damping



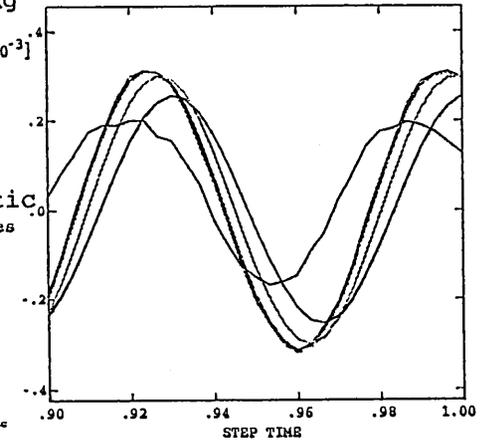
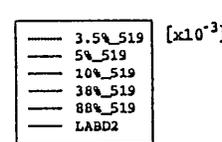
Total Time : 279.90 to 280 sec

ABAQUS Modal Dynamic Analyses & Laboratory Measurements

Linear Elastic  
 Material Properties  
 STANDARD Analyses  
 Uncracked Model  
 Displacement  
 at LVDT#3

# ABAQUS

Modal Damping



Total Time : 279.90 to 280 sec

ABAQUS Modal Dynamic Analyses & Laboratory Measurements

Linear Elastic  
 Material Properties  
 STANDARD Analyses  
 Uncracked Model  
 Acceleration  
 at LVDT#2

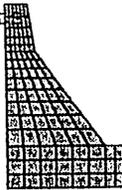
Figure h16

# ABAQUS

Koyna Laboratory Model Study  
 Uncracked Model Study  
 Sensitivity Study  
 Variation of Modal Damping

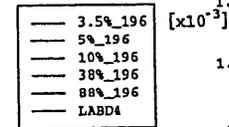
Comparison of Displacement  
 ABAQUS STANDARD  
 Modal Dynamic Analysis

Input Record SHAKEA  
 Elastic Modulus = 250 ksi  
 Density = 140.0 pcf  
 Mesh # 3

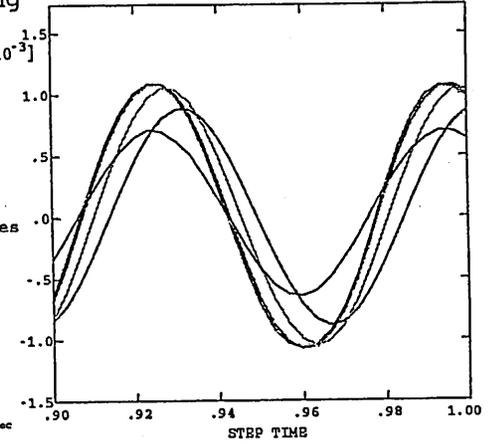


# ABAQUS

Modal Damping



Linear Elastic  
 Material Properties  
 STANDARD Analyses  
 Uncracked Model  
 Displacement  
 at LVDT#4

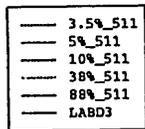


Total Time : 279.90 to 280 sec

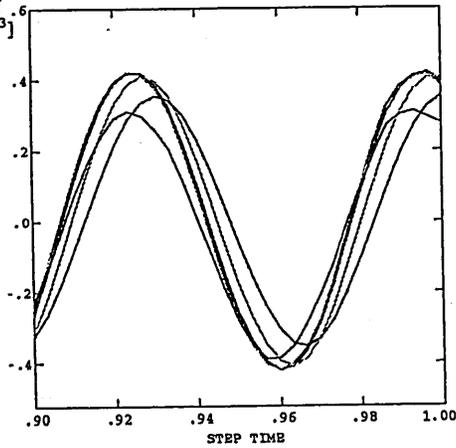
ABAQUS Modal Dynamic Analyses & Laboratory Measurements

# ABAQUS

Modal Damping  
 [x10<sup>-3</sup>]



Linear Elastic  
 Material Properties  
 STANDARD Analyses  
 Uncracked Model  
 Displacement  
 at LVDT#3

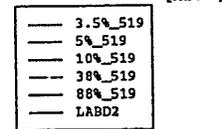


Total Time : 279.90 to 280 sec

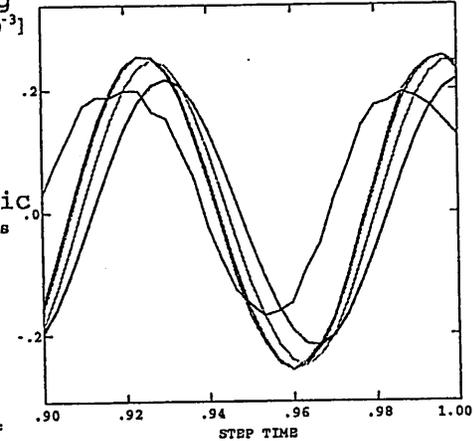
ABAQUS Modal Dynamic Analyses & Laboratory Measurements

# ABAQUS

Modal Damping



Linear Elastic  
 Material Properties  
 STANDARD Analyses  
 Uncracked Model  
 Acceleration  
 at LVDT#2



Total Time : 279.90 to 280 sec

ABAQUS Modal Dynamic Analyses & Laboratory Measurements

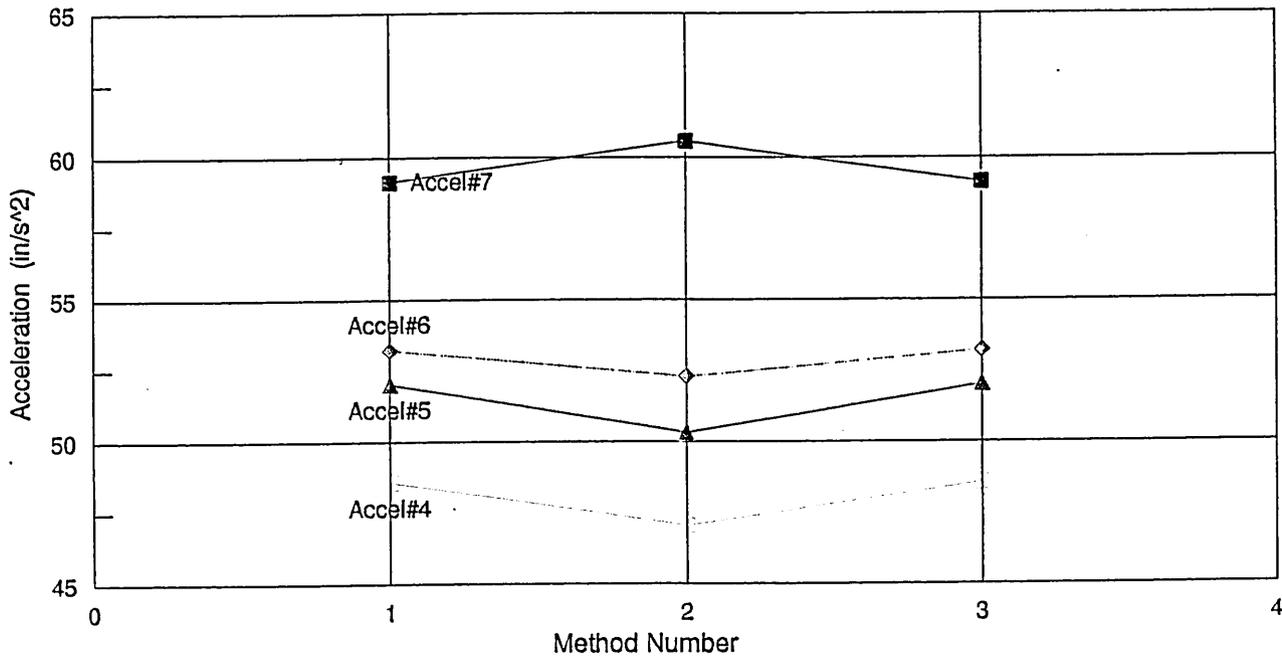
Figure h17

Uncracked Koyna Laboratory Study  
Sensitivity to Variation in Damping Method  
Mesh#3

Modal Damping; Rayleigh Damping; Composite Damping  
10 Percent of Critical Damping

Elastic Modulus = 210 ksi; Material Density = 138.2 pcf

**Peak Accelerations**  
Damping Method Varied



Peak Accelerations ( inch / sec ^ 2 )

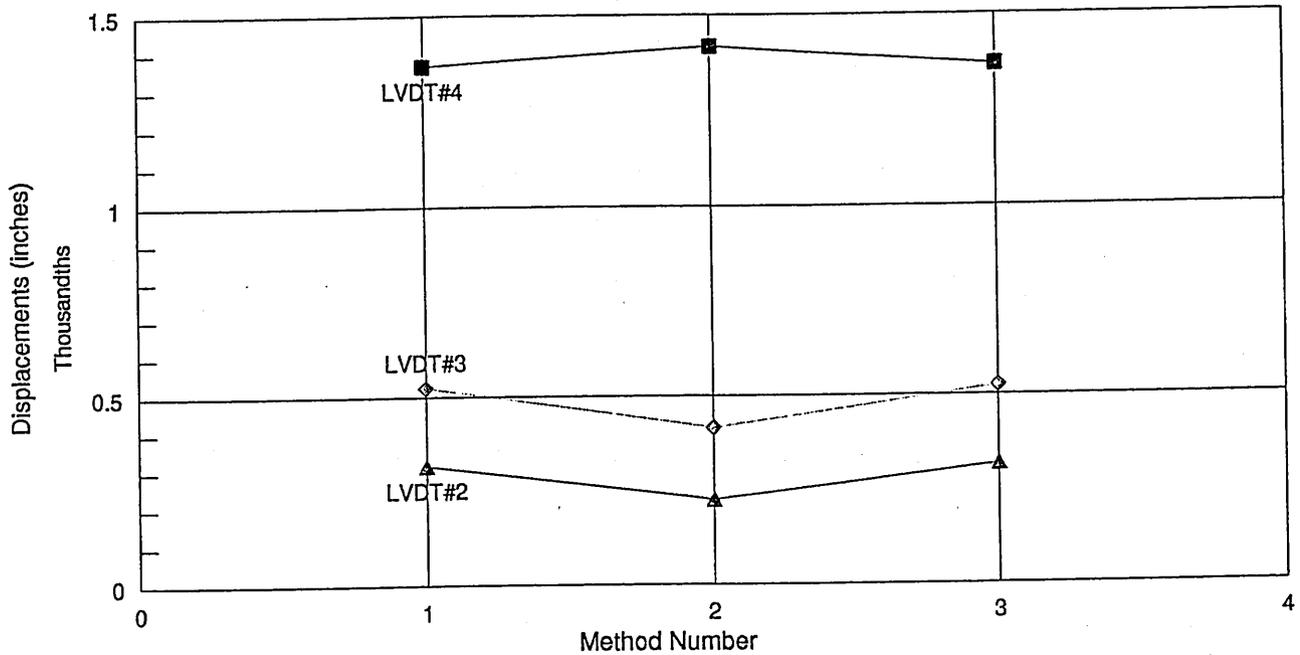
	Modal	Rayleigh	Composite	
Method Number	1	2	3	LAB
Accel#7	59.15	60.57	59.15	53.26
Accel#6	53.21	52.29	53.21	51.72
Accel#5	52.02	50.31	52.02	49.26
Accel#4	48.57	47.06	48.57	47.72
CPU TIME (SEC)	264	264	263	

Figure h18

Uncracked Koyna Laboratory Study  
Sensitivity to Variation in Damping Method  
Mesh#3  
Modal Damping; Rayleigh Damping; Composite Damping  
10 Percent of Critical Damping

Elastic Modulus = 210 ksi; Material Density = 138.2 pcf

**Peak Displacements**  
Damping Method Varied



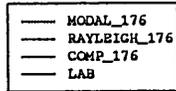
Peak Displacements ( inches )

	Modal	Rayleigh	Composite	
Method Number	1	2	3	LAB
LVDT#4	1.4E-03	1.4E-03	1.4E-03	7.8E-04
LVDT#3	5.2E-04	4.1E-04	5.2E-04	3.0E-04
LVDT#2	3.2E-04	2.2E-04	3.2E-04	1.8E-04
CPU TIME (SEC)	264	264	263	

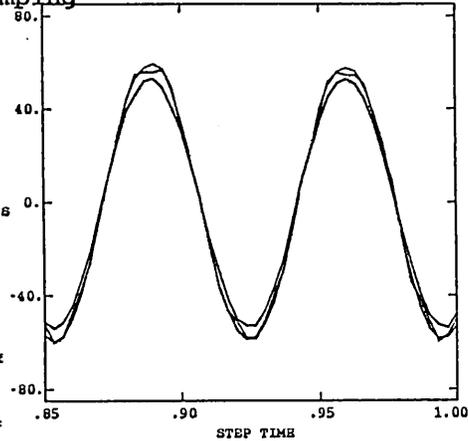
Figure h19

# ABAQUS

Method of Damping  
Varied

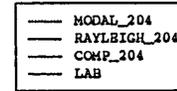


Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model  
Acceleration  
at ACCEL#7  
Elastic Modulus = 210 ksi  
Material Density = 140 pcf  
Filename:SHAKEA  
10% Critical Damping  
Total Time : 279.75 to 280 sec

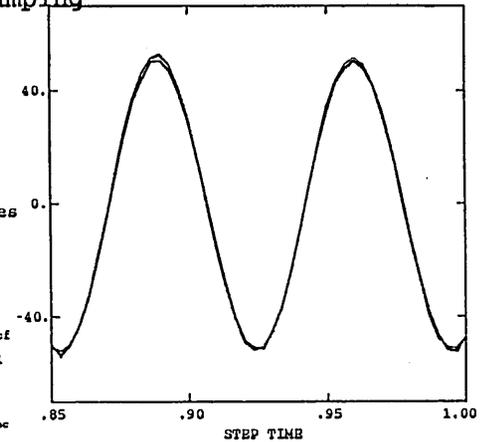


# ABAQUS

Method of Damping  
Varied

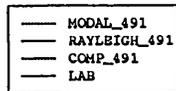


Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model  
Acceleration  
at ACCEL#6  
Material Density = 140 pcf  
Elastic Modulus = 210 ksi  
Filename:SHAKEA  
10% Critical Damping  
Total Time : 279.75 to 280 sec

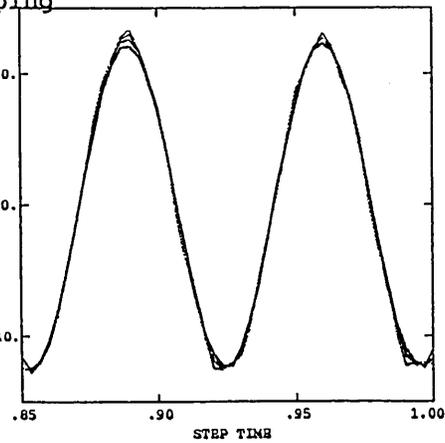


# ABAQUS

Method of Damping  
Varied

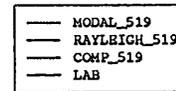


Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model  
Acceleration  
at ACCEL#5  
Elastic Modulus = 210 ksi  
Material Density = 140 pcf  
Filename:SHAKEA  
10% Critical Damping  
Total Time : 279.75 to 280 sec



# ABAQUS

Method of Damping  
Varied



Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model  
Acceleration  
at ACCEL#4  
Elastic Modulus = 210 ksi  
Material Density = 140 pcf  
Filename:SHAKEA  
10% Critical Damping  
Total Time : 279.75 to 280 sec

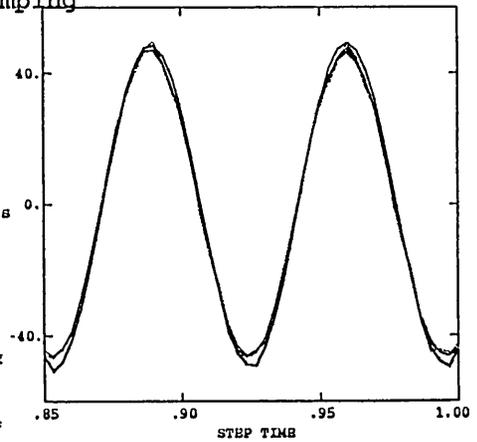


Figure h20

# ABAQUS

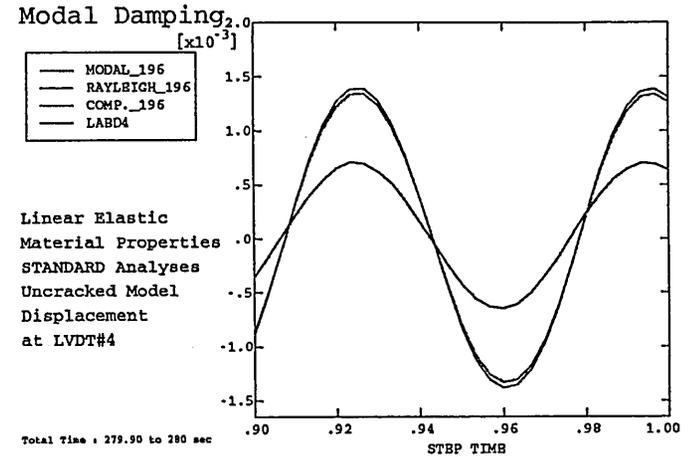
Koyna Laboratory Model Study  
 Uncracked Model Study  
 Sensitivity Study  
 Variation of Damping Method

Comparison of Displacements  
 ABAQUS STANDARD  
 Modal Dynamic Analysis

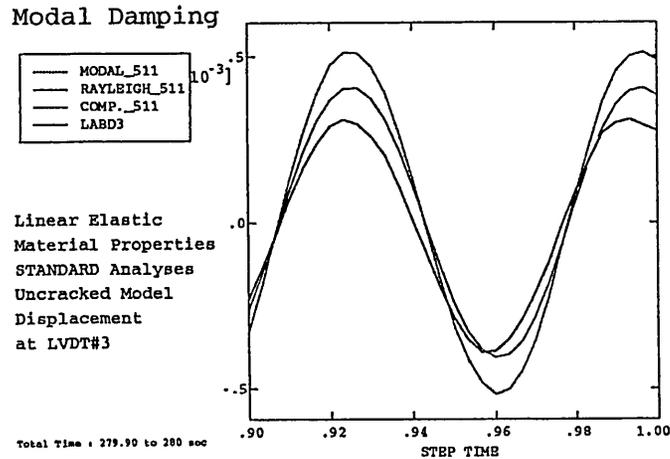
Input Record SHAKEA  
 Elastic Modulus = 210 ksi  
 Density = 140.0 pcf  
 Mesh # 3  
 10 Percent Critical Damping



# ABAQUS



# ABAQUS



# ABAQUS

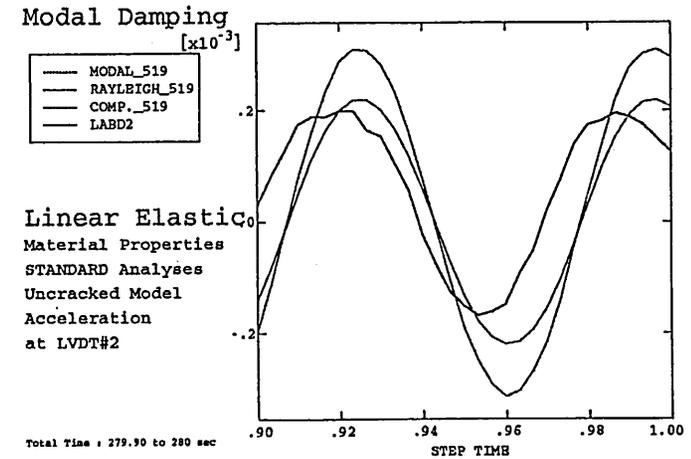


Figure h21

**Appendix I**  
**Sensitivity to Variation of Analysis Time Increment**

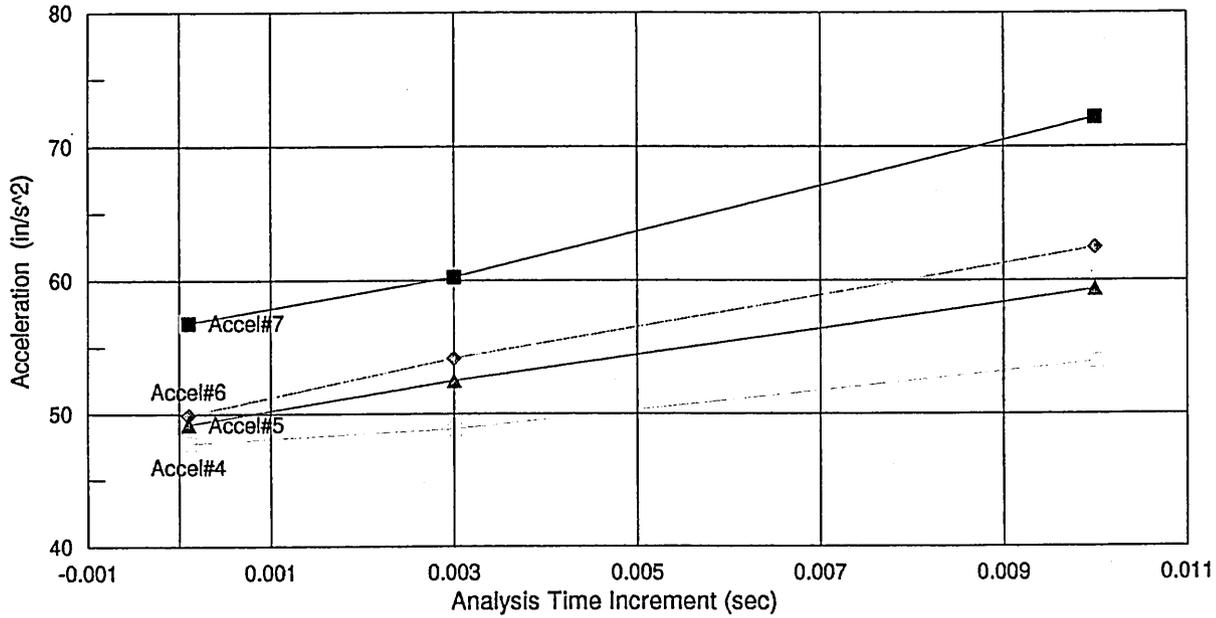
Uncracked Koyna Laboratory Study

Direct Integration Dynamic Analysis  
Sensitivity to Variation in Direct Time Step Parameter  
Mesh#3

Elastic Modulus = 210 ksi;

Material Density = 140 pcf

**Peak Accelerations**  
Direct Time Step Parameter Varied



Peak Accelerations ( inch / sec ^ 2 )

Direct Time Step	0.0001	0.003	0.01	LAB
Accel#7	56.81	60.26	72.18	53.26
Accel#6	49.87	54.17	62.47	51.72
Accel#5	49.19	52.47	59.36	49.26
Accel#4	47.75	48.86	53.94	47.72
CPU Time (sec)	39564	1441	557	

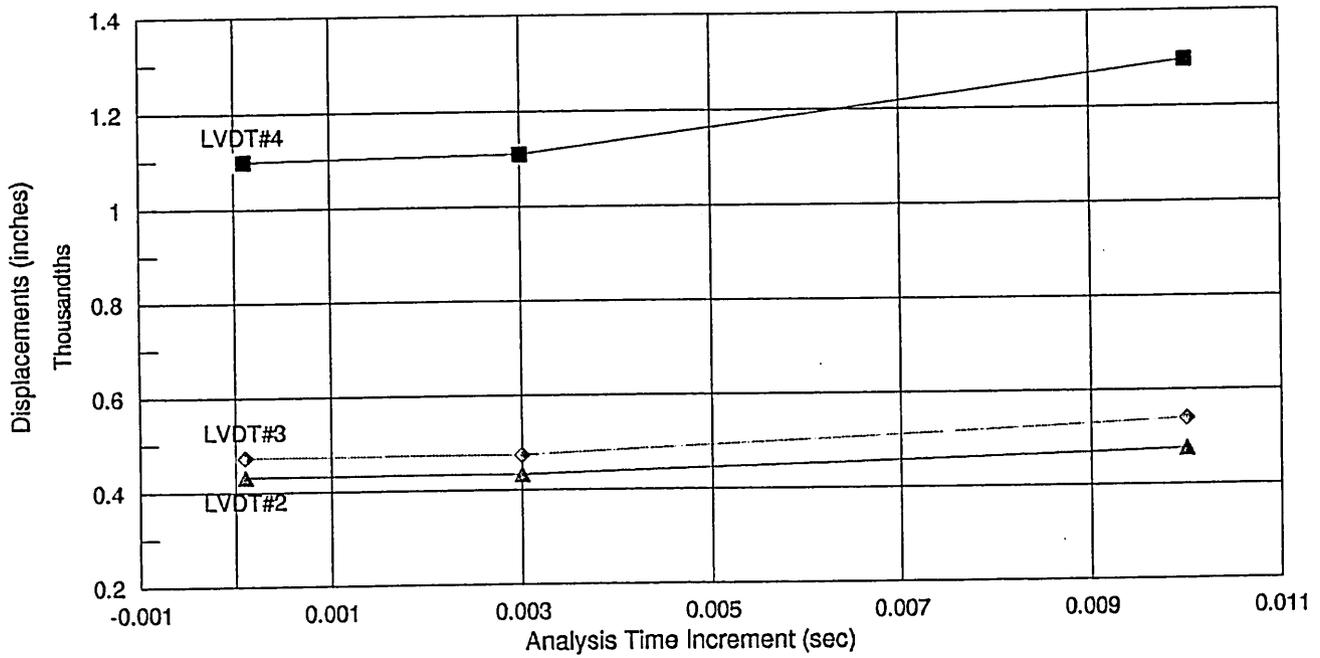
Figure i1

Uncracked Koyna Laboratory Study

Direct Integration Dynamic Analysis  
Sensitivity to Variation in Direct Time Increment Parameter  
Mesh#3

Elastic Modulus = 210 ksi;      Material Density = 140 pcf

**Peak Displacements**  
Direct Time Step Parameter Varied



Peak Displacements ( inches )					
Haftol Parameter	0.0001	0.003	0.01	LAB	
LVDT#4	1.1E-03	1.1E-03	1.3E-03	7.8E-04	
LVDT#3	4.7E-04	4.7E-04	5.4E-04	3.0E-04	
LVDT#2	4.3E-04	4.3E-04	4.7E-04	1.8E-04	
CPU Time (sec)	39564	1441	557		

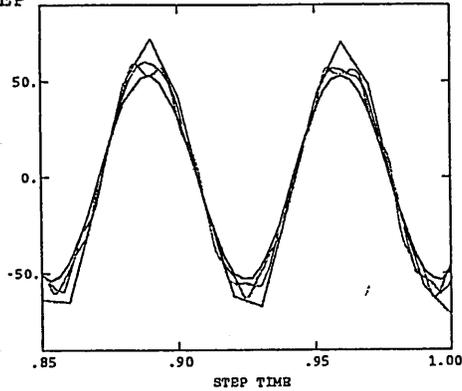
Figure i2

# ABAQUS

DIRECT TIME STEP  
Varied

— TS.0001\_176  
— TS.003\_176  
— TS.01\_176  
— LAB

Linear Elastic  
Material Properties  
Uncracked Model  
Acceleration  
at ACCEL#7  
Direct Integration  
Dynamic Analysis  
Material Density = 140 pcf  
Elastic Modulus = 210 ksi  
Filename: 81A2A

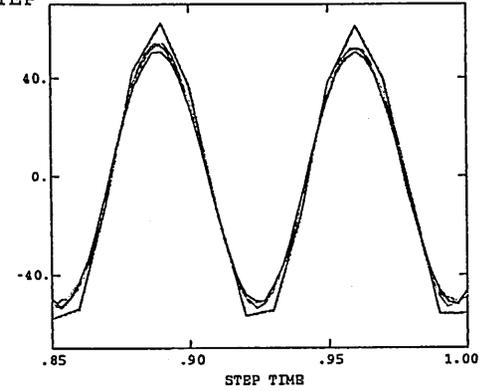


# ABAQUS

DIRECT TIME STEP  
Varied

— TS.0001\_204  
— TS.003\_204  
— TS.01\_204  
— LAB

Linear Elastic  
Material Properties  
Uncracked Model  
Acceleration  
at ACCEL#6  
Direct Integration  
Dynamic Analysis  
Material Density = 140 pcf  
Elastic Modulus = 210 ksi  
Filename: 81A2A

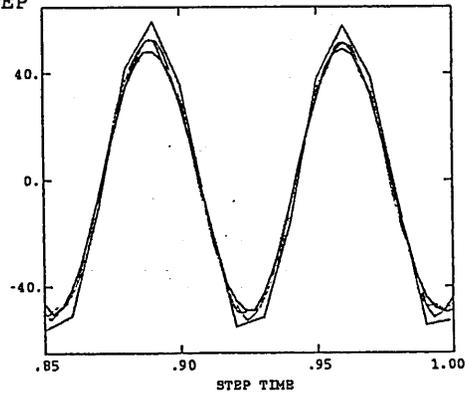


# ABAQUS

DIRECT TIME STEP  
Varied

— TS.0001\_491  
— TS.003\_491  
— TS.01\_491  
— LAB

Linear Elastic  
Material Properties  
Uncracked Model  
Acceleration  
at ACCEL#5  
Direct Integration  
Dynamic Analysis  
Material Density = 140 pcf  
Elastic Modulus = 210 ksi  
Filename: 81A2A

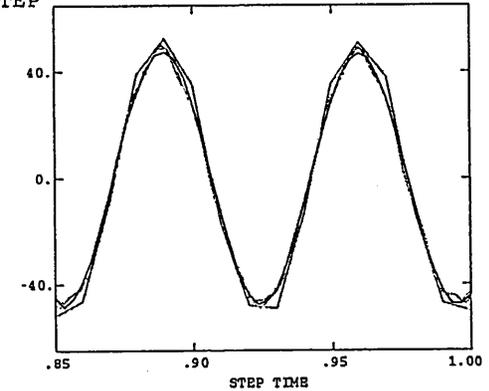


# ABAQUS

DIRECT TIME STEP  
Varied

— TS.0001\_519  
— TS.003\_519  
— TS.01\_519  
— LAB

Linear Elastic  
Material Properties  
Uncracked Model  
Acceleration  
at ACCEL#4  
Direct Integration  
Dynamic Analysis  
Material Density = 140 pcf  
Elastic Modulus = 210 ksi  
Filename: 81A2A

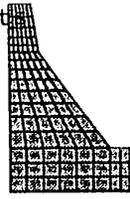


# ABAQUS

Koyna Laboratory Model Study  
 Uncracked Model Study  
 Sensitivity Study  
 Variation of Direct Time Step

Comparison of Displacement  
 Direct Integration  
 Dynamic Analysis

Input Record SHAKEA  
 Mesh # 3  
 Density = 140 pcf  
 Elastic Modulus = 210 ksi  
 Time Step = .0001, .003, & .01 sec

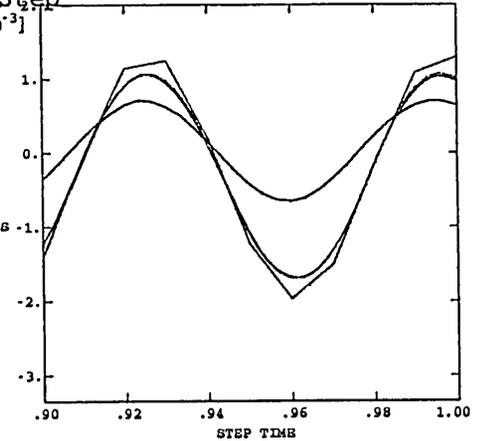


# ABAQUS

Direct Time Step  
 Varied [ $\times 10^{-3}$ ]

— TS\_0001  
 — TS\_003  
 — TS\_01  
 — LABD4

Linear Elastic  
 Material Properties -1.  
 STANDARD Analyses  
 Uncracked Model  
 Displacement  
 at LVDT#4

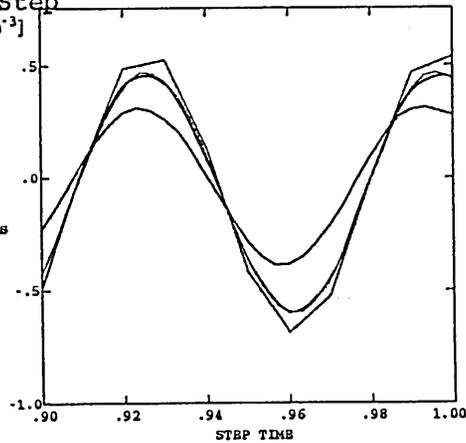


# ABAQUS

Direct Time Step  
 Varied [ $\times 10^{-3}$ ]

— TS\_0001  
 — TS\_003  
 — TS\_01  
 — LABD3

Linear Elastic  
 Material Properties  
 STANDARD Analyses  
 Uncracked Model  
 Displacement  
 at LVDT#3



# ABAQUS

Direct Time Step  
 Varied [ $\times 10^{-3}$ ]

— TS\_0001  
 — TS\_003  
 — TS\_01  
 — LABD2

Linear Elastic  
 Material Properties  
 STANDARD Analyses  
 Uncracked Model  
 Acceleration  
 at LVDT#2

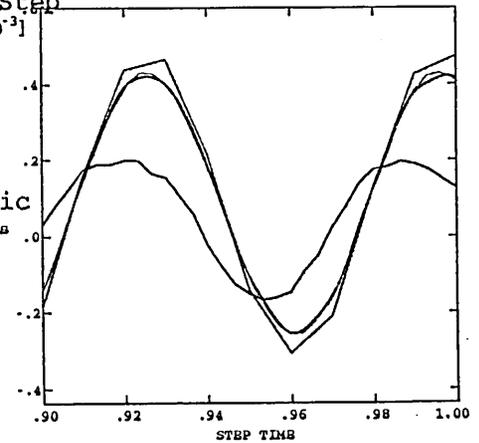


Figure 14

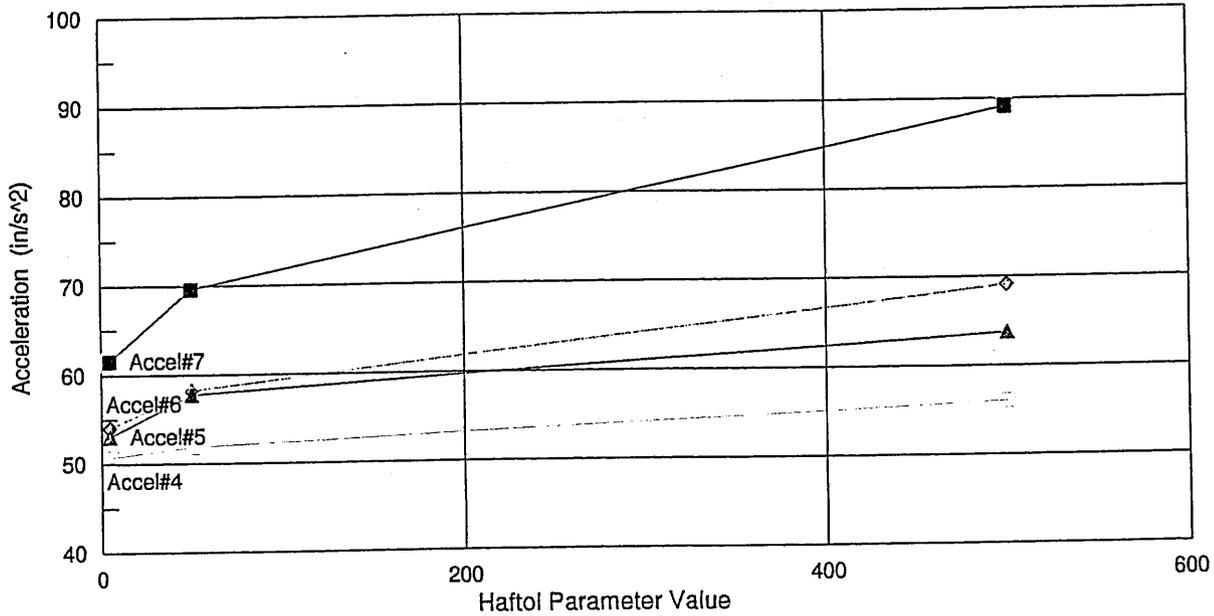
Uncracked Koyna Laboratory Study

Direct Integration Dynamic Analysis  
Sensitivity to Variation in Haftol Parameter  
Mesh#3

Elastic Modulus = 210 ksi;

Material Density = 140 pcf

**Peak Accelerations**  
Haftol Parameter Varied



Peak Accelerations ( inch / sec ^ 2 )

Haftol Parameter	5	50	500	LAB
Accel#7	61.51	69.62	89.07	53.26
Accel#6	54.09	58.23	69.14	51.72
Accel#5	53.04	57.73	63.71	49.26
Accel#4	50.75	51.88	56.01	47.72
CPU Time (sec)	3179	1230	785	

Figure i5

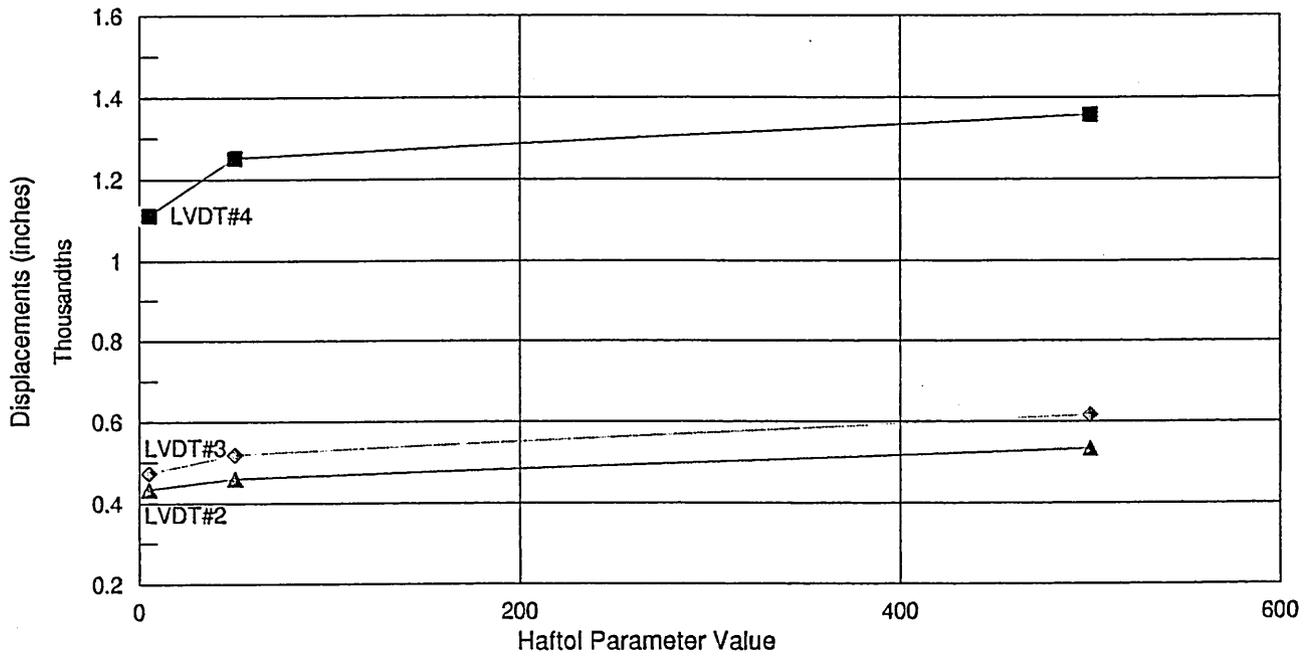
Uncracked Koyna Laboratory Study

Direct Integration Dynamic Analysis  
Sensitivity to Variation in Haftol Parameter  
Mesh#3

Elastic Modulus = 210 ksi;

Material Density = 140 pcf

**Peak Displacements**  
Haftol Parameter Varied



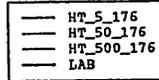
Peak Displacements ( inches )

Haftol Parameter	5	50	500	LAB
LVDT#4	1.1E-03	1.3E-03	1.4E-03	7.8E-04
LVDT#3	4.7E-04	5.2E-04	6.2E-04	3.0E-04
LVDT#2	4.3E-04	4.6E-04	5.3E-04	1.8E-04
CPU Time (sec)	3179	1230	785	

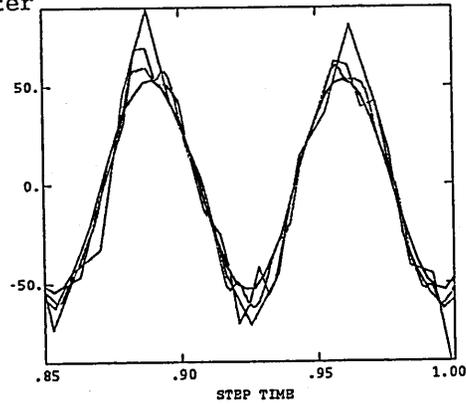
Figure i6

# ABAQUS

Haftol Parameter Varied

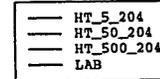


Linear Elastic  
Material Properties  
Uncracked Model  
Acceleration  
at ACCEL#7  
Direct Integration  
Dynamic Analysis  
Material Density = 140 pcf  
Elastic Modulus = 210 ksi  
file name: P10A22A

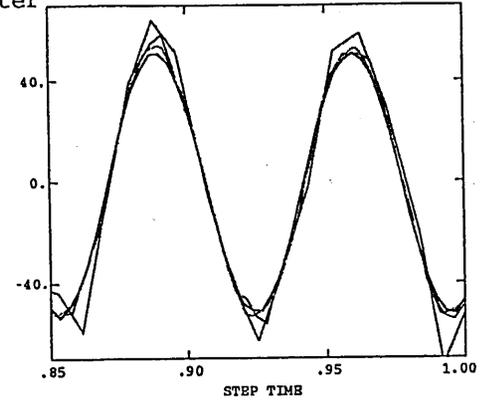


# ABAQUS

Haftol Parameter Varied

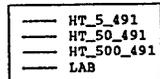


Linear Elastic  
Material Properties  
Uncracked Model  
Acceleration  
at ACCEL#6  
Direct Integration  
Dynamic Analysis  
Material Density = 140 pcf  
Elastic Modulus = 210 ksi  
file name: P10A22A

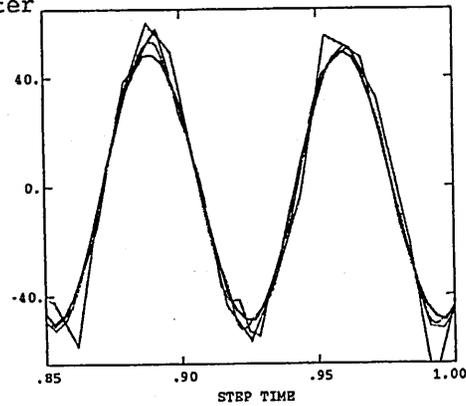


# ABAQUS

Haftol Parameter Varied

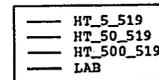


Linear Elastic  
Material Properties  
Uncracked Model  
Acceleration  
at ACCEL#5  
Direct Integration  
Dynamic Analysis  
Material Density = 140 pcf  
Elastic Modulus = 210 ksi  
file name: P10A22A



# ABAQUS

Haftol Parameter Varied



Linear Elastic  
Material Properties  
Uncracked Model  
Acceleration  
at ACCEL#4  
Direct Integration  
Dynamic Analysis  
Material Density = 140 pcf  
Elastic Modulus = 210 ksi  
file name: P10A22A

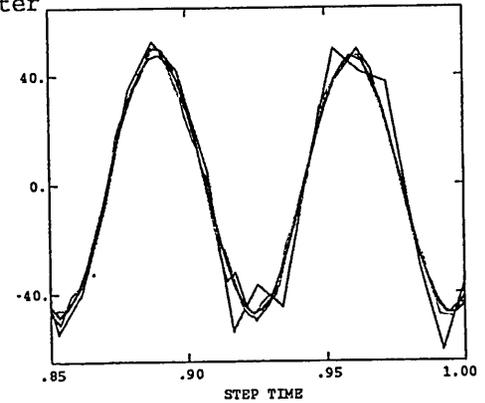


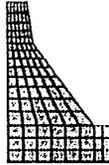
Figure 17

# ABAQUS

Koyna Laboratory Model Study  
 Uncracked Model Study  
 Sensitivity Study  
 Variation of Haftol Parameter

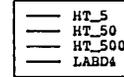
Comparison of Displacements  
 Direct Integration  
 Dynamic Analysis

Input Record SHAKEA  
 Haftol = 5, 50, & 500  
 Density = 140 pcf  
 Elastic Modulus = 210 ksi  
 Mesh # 3

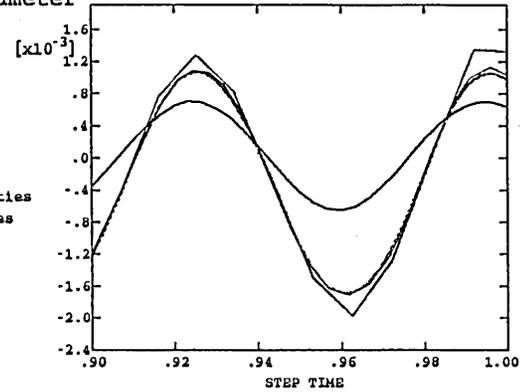


# ABAQUS

Haftol Parameter  
 Varied

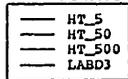


Linear Elastic  
 Material Properties  
 STANDARD Analyses  
 Uncracked Model  
 Displacement  
 at LVDT#4

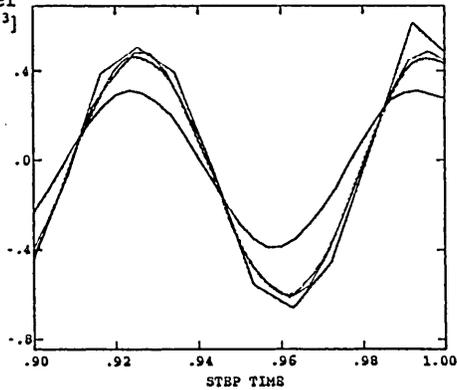


# ABAQUS

Haftol Parameter  
 Varied [ $\times 10^{-3}$ ]

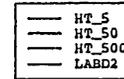


Linear Elastic  
 Material Properties  
 STANDARD Analyses  
 Uncracked Model  
 Displacement  
 at LVDT#3



# ABAQUS

Haftol Parameter  
 Varied [ $\times 10^{-3}$ ]



Linear Elastic  
 Material Properties  
 STANDARD Analyses  
 Uncracked Model  
 Acceleration  
 at LVDT#2

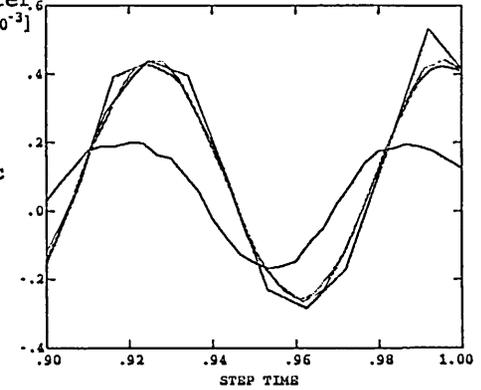
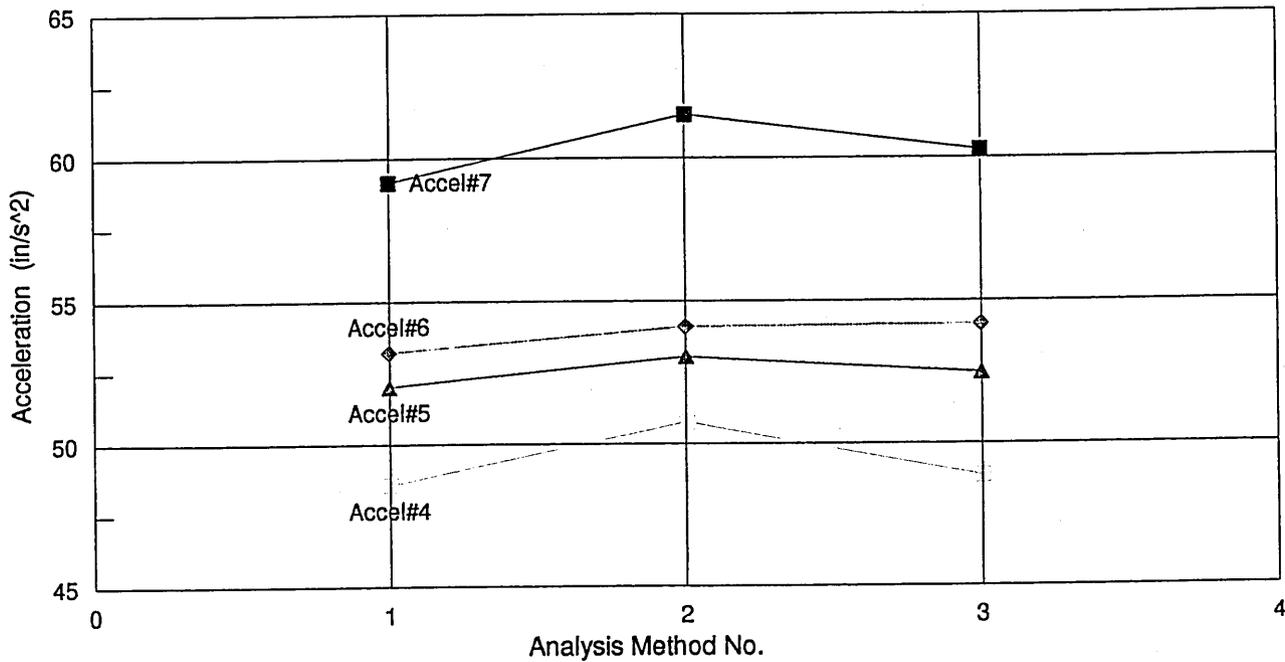


Figure 18

**Appendix J**  
**Comparison of**  
**Analysis Procedures**

Uncracked Koyna Laboratory Study  
 Sensitivity to Variation Analysis Method  
 Mesh#3  
 Modal Analysis Methods  
 Direct Integration using Haftol Parameter = 5  
 Direct Integration using Direct time Step = .003 sec  
 Modal Analysis  
 10 Percent of Critical Damping  
 Elastic Modulus = 210 ksi; Material Density = 139 pcf

**Peak Accelerations**  
 Analysis Method Varied



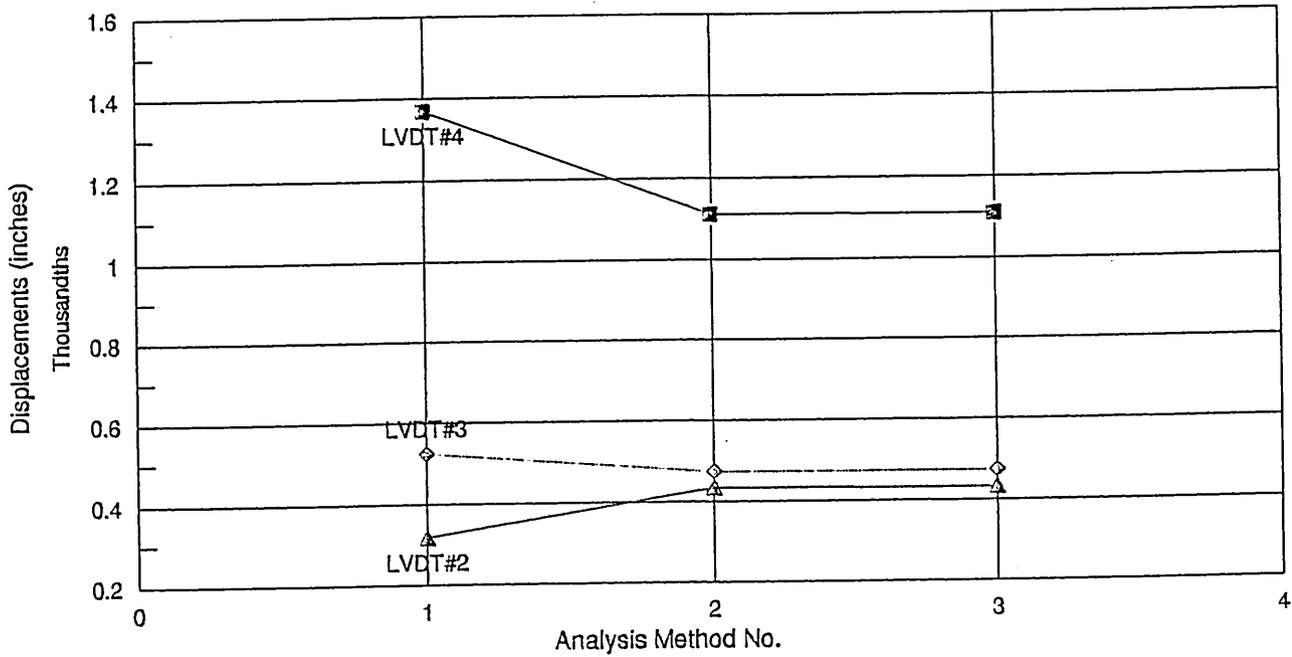
Peak Accelerations ( inch / sec ^ 2 )

	Modal	Direct Haftol=5	Direct Time Step=.003	LAB
Method Number	1	2	3	
Accel#7	59.15	61.51	60.26	53.26
Accel#6	53.21	54.09	54.17	51.72
Accel#5	52.02	53.04	52.47	49.26
Accel#4	48.57	50.75	48.86	47.72
CPU TIME (SEC)	264	3179	1441	

Figure j1

Uncracked Koyna Laboratory Study  
 Sensitivity to Variation Analysis Method  
 Mesh#3  
 Modal Analysis Methods  
 Direct Integration using Haftol Parameter = 5  
 Direct Integration using Direct time Step = .003 sec  
 Modal Analysis  
 10 Percent of Critical Damping  
 Elastic Modulus = 210 ksi; Material Density = 139 pcf

**Peak Displacements**  
 Analysis Method Varied



Peak Displacements ( inches )

	Modal	Direct Haftol=5	Direct Time Step=.003	LAB
Method Number	1	2	3	
LVDT#4	1.4E-03	1.1E-03	1.1E-03	7.8E-04
LVDT#3	5.2E-04	4.7E-04	4.7E-04	3.0E-04
LVDT#2	3.2E-04	4.3E-04	4.3E-04	1.8E-04
CPU TIME (SEC)	264	3179	1441	

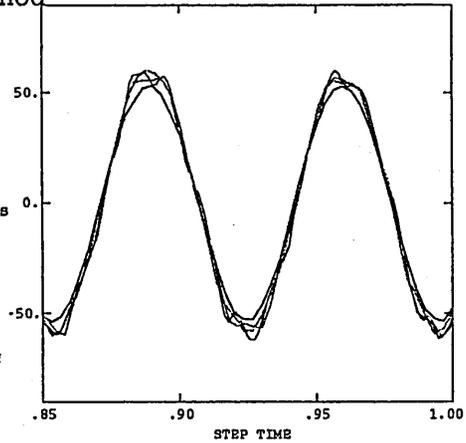
Figure j2

# ABAQUS

Analysis Method  
Varied

— MODAL\_176  
— HT\_5\_176  
— TS.003\_176  
— LAB

Linear Elastic  
Material Properties  
Uncracked Model  
Acceleration  
at ACCEL#7  
Modal & Direct  
Dynamic Analysis  
Material Density = 140 pcf  
Elastic Modulus = 210 ksi  
Filename:SHAKEA

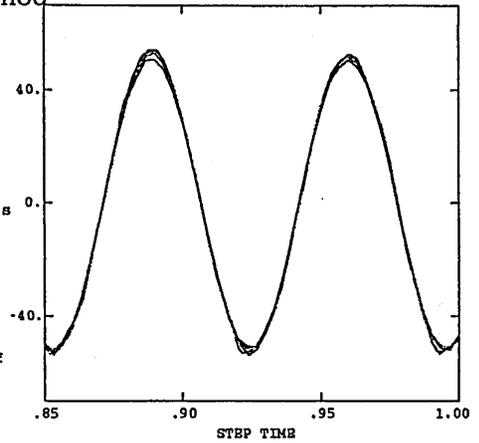


# ABAQUS

Analysis Method  
Varied

— MODAL\_204  
— HT\_5\_204  
— TS.003\_204  
— LAB

Linear Elastic  
Material Properties  
Uncracked Model  
Acceleration  
at ACCEL#6  
Modal & Direct  
Dynamic Analysis  
Material Density = 140 pcf  
Elastic Modulus = 210 ksi  
Filename:SHAKEA

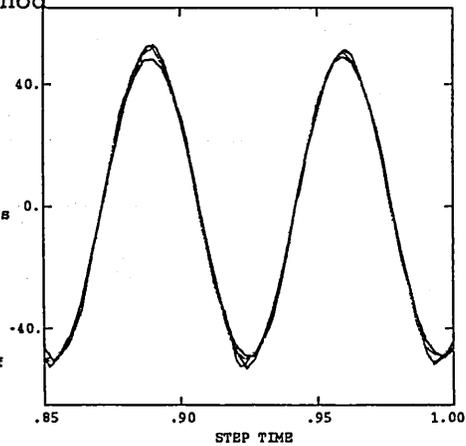


# ABAQUS

Analysis Method  
Varied

— MODAL\_491  
— HT\_5\_491  
— TS.003\_491  
— LAB

Linear Elastic  
Material Properties  
Uncracked Model  
Acceleration  
at ACCEL#5  
Modal & Direct  
Dynamic Analysis  
Material Density = 140 pcf  
Elastic Modulus = 210 ksi  
Filename:SHAKEA



# ABAQUS

Analysis Method  
Varied

— MODAL\_519  
— HT\_5\_519  
— TS.003\_519  
— LAB

Linear Elastic  
Material Properties  
Uncracked Model  
Acceleration  
at ACCEL#4  
Modal & Direct  
Dynamic Analysis  
Material Density = 140 pcf  
Elastic Modulus = 210 ksi  
Filename:SHAKEA

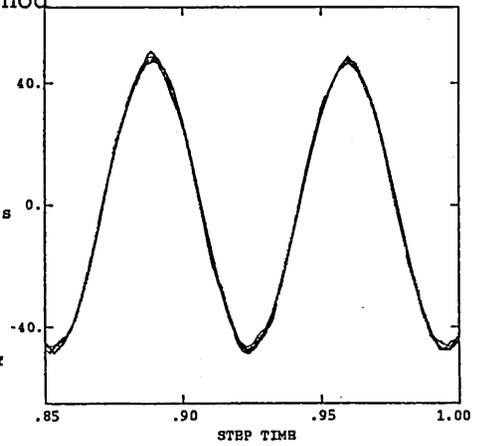


Figure j3

# ABAQUS

Koyna Laboratory Model Study  
 Uncracked Model Study  
 Sensitivity Study  
 Variation of Analysis Method

Comparison of Displacements  
 Modal & Direct Integration  
 Dynamic Analysis

Input Record SHAKEA  
 Mesh # 3  
 Density = 140 pcf  
 Elastic Modulus = 210 ksi

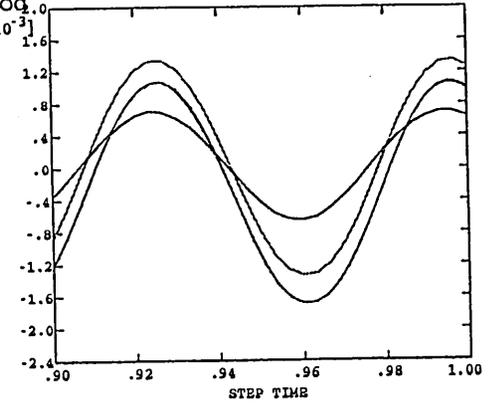


# ABAQUS

Analysis Method  
 Varied [ $\times 10^{-3}$ ]

— MODAL\_196  
 — HT\_5  
 — TS.003  
 — LABD4

Linear Elastic  
 Material Properties  
 STANDARD Analyses  
 Uncracked Model  
 Displacement  
 at LVDT#4

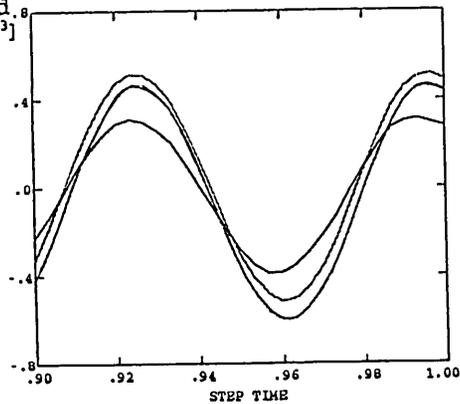


# ABAQUS

Analysis Method  
 Varied [ $\times 10^{-3}$ ]

— MODAL\_511  
 — HT\_5  
 — TS.003  
 — LABD3

Linear Elastic  
 Material Properties  
 STANDARD Analyses  
 Uncracked Model  
 Displacement  
 at LVDT#3



# ABAQUS

Analysis Method  
 Varied [ $\times 10^{-3}$ ]

— MODAL\_519  
 — HT\_5  
 — TS.003  
 — LABD2

Linear Elastic  
 Material Properties  
 STANDARD Analyses  
 Uncracked Model  
 Acceleration  
 at LVDT#2

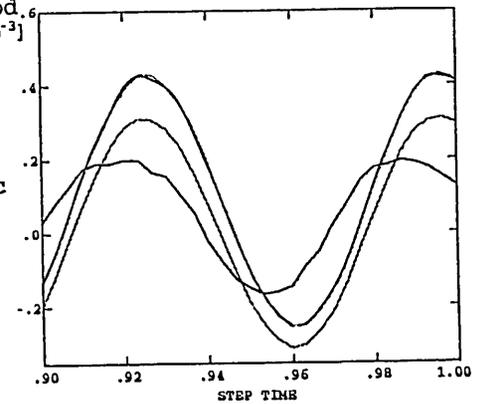


Figure 14

**Appendix K**  
**Nonlinear Analysis**

# ABAQUS

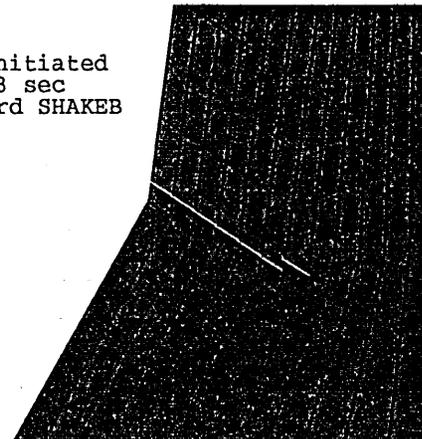
Koyna Laboratory Model Study  
Uncracked Model Study

Determination of Mesh Sensitivity  
Non-linear Material Propertys  
Failure Stress = 55 psi  
Mode I Fracture Energy = 0.2012  
Crack Opening Strain = .001375

Explicit Analysis  
with Mesh #3

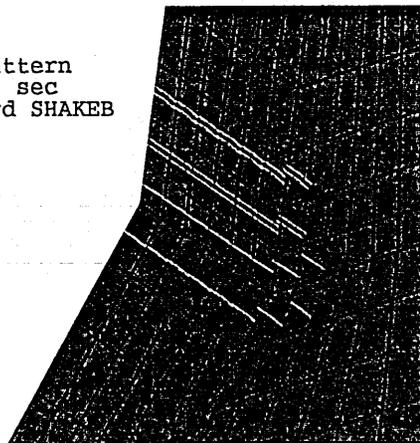
# ABAQUS

Cracking Initiated  
at 401.3 sec  
Input Record SHAKEB



# ABAQUS

Cracking Pattern  
at 401.5 sec  
Input Record SHAKEB



# ABAQUS

Cracking Pattern  
at 401.6 sec  
Input Record SHAKEB

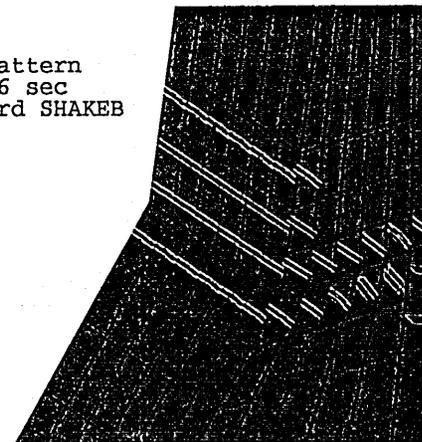


Figure k1

# ABAQUS

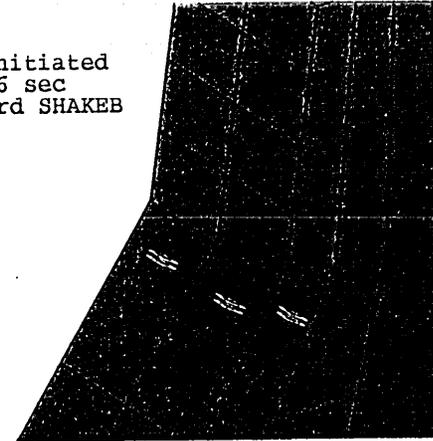
Koyna Laboratory Model Study  
Uncracked Model Study

Determination of Mesh Sensitivity  
Non-linear Material Propertys  
Failure Stress = 55 psi  
Mode I Fracture Energy = 0.2012  
Crack Opening Strain = .001375

Explicit Analysis  
with Mesh #5

# ABAQUS

Cracking Initiated  
at 407.6 sec  
Input Record SHAKEB



# ABAQUS

Cracking Pattern  
at 407.7 sec  
Input Record SHAKEB



# ABAQUS

Cracking Pattern  
at 407.75 sec  
Input Record SHAKEB

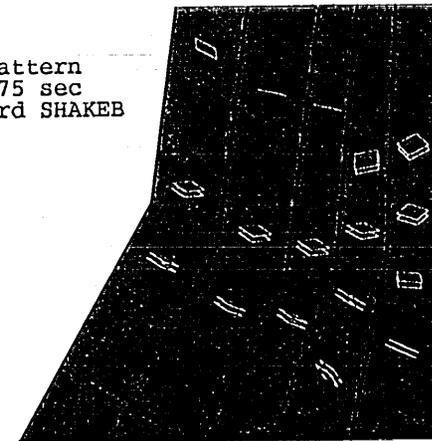


Figure k2

# ABAQUS

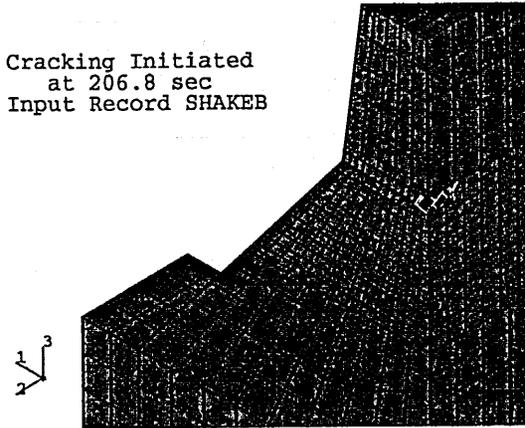
Koyna Laboratory Model Study  
Uncracked Model Study

Determination of Mesh Sensitivity  
Non-linear Material Propertys  
Failure Stress = 55 psi  
Mode I Fracture Energy = 0.2012  
Crack Opening Strain = .001375

Explicit Analysis  
with Mesh #1

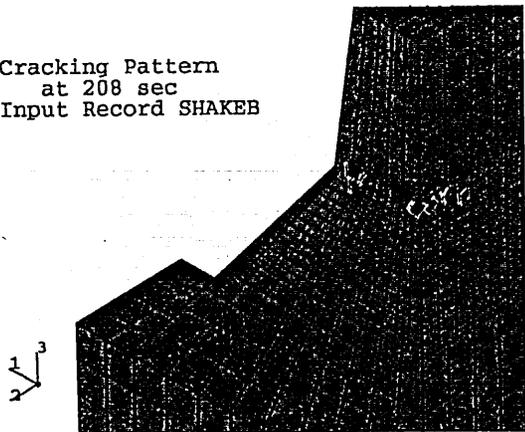
# ABAQUS

Cracking Initiated  
at 206.8 sec  
Input Record SHAKEB



# ABAQUS

Cracking Pattern  
at 208 sec  
Input Record SHAKEB



# ABAQUS

Cracking Pattern  
at 210.5 sec  
Input Record SHAKEB

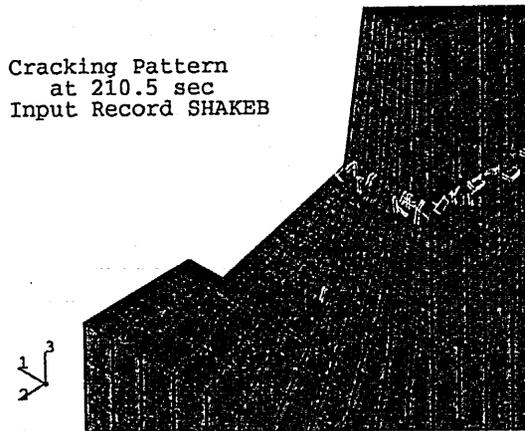


Figure k3

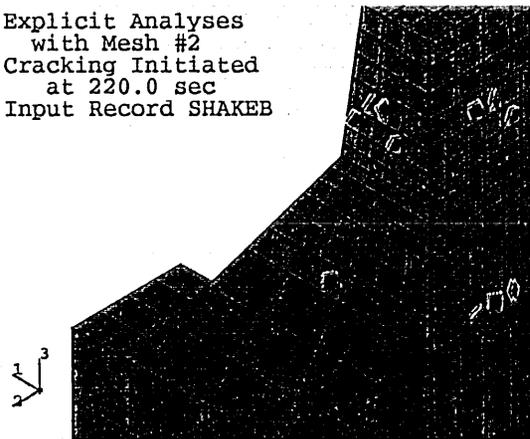
# ABAQUS

Koyna Laboratory Model Study  
Uncracked Model Study

Determination of Mesh Sensitivity  
Non-linear Material Propertys  
Failure Stress = 55 psi  
Mode I Fracture Energy = 0.2012  
Crack Opening Strain = .001375

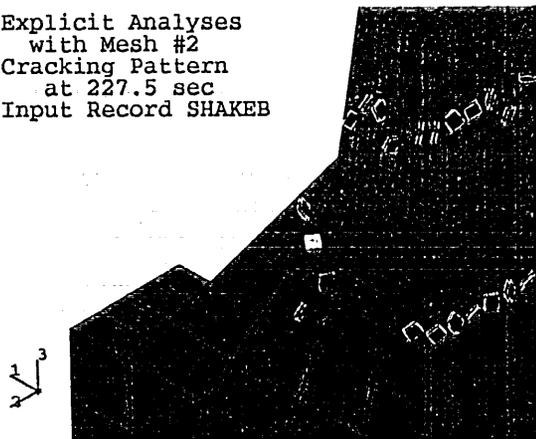
# ABAQUS

Explicit Analyses  
with Mesh #2  
Cracking Initiated  
at 220.0 sec  
Input Record SHAKEB



# ABAQUS

Explicit Analyses  
with Mesh #2  
Cracking Pattern  
at 227.5 sec  
Input Record SHAKEB



# ABAQUS

Explicit Analyses  
with Mesh #2  
Cracking Failure  
at 232.5 sec  
Input Record SHAKEB

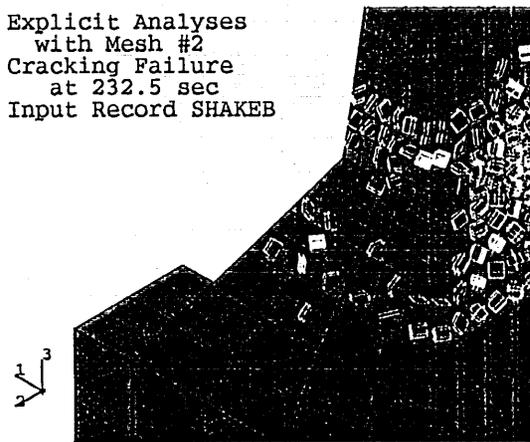


Figure k4

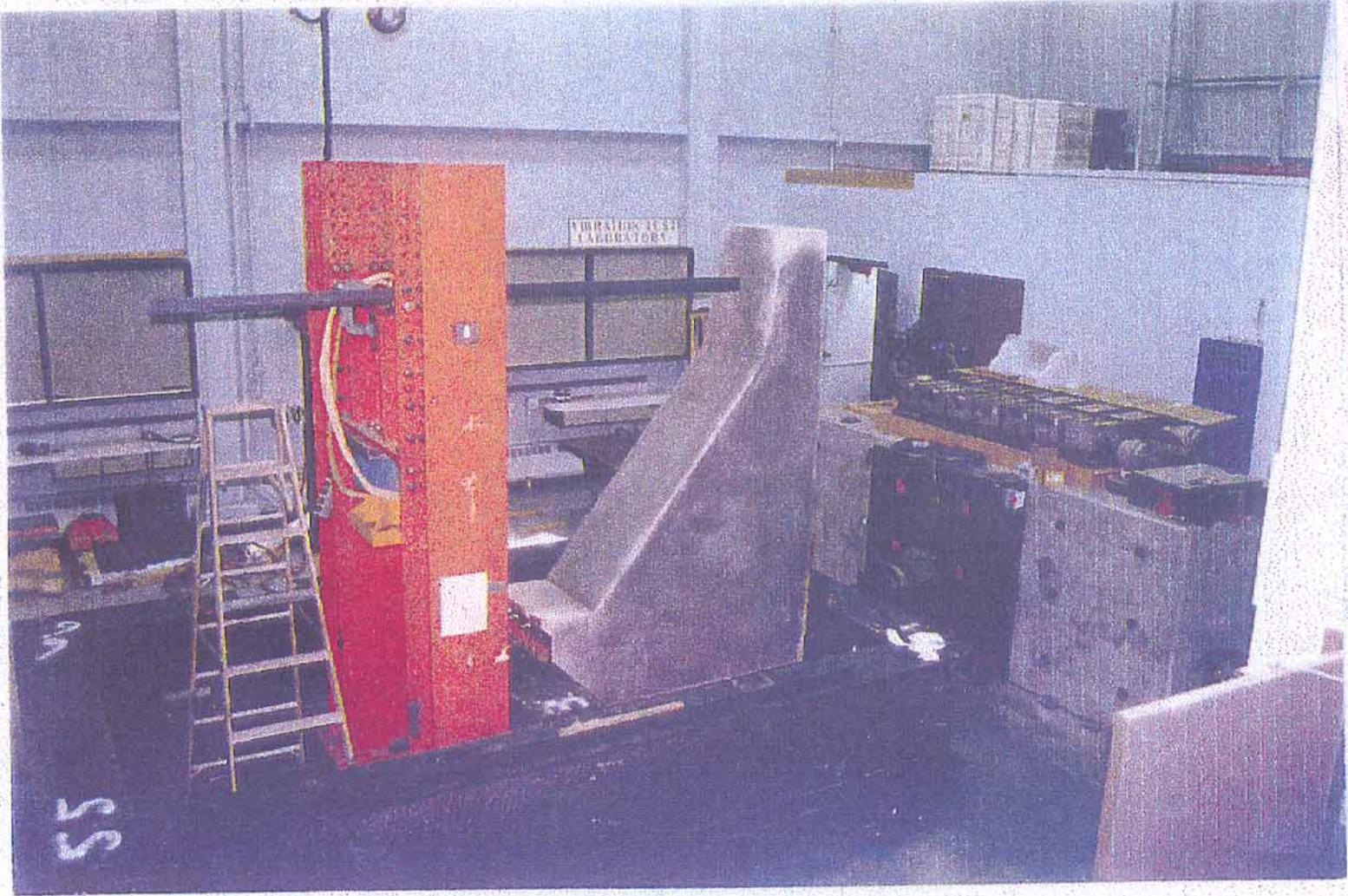


Figure b1

# ABAQUS

— ACCIN

Input Motion

SHAKEA

(inch/sec<sup>2</sup>)

XMIN .000E+00  
XMAX 4.862E+02  
YMIN -1.382E+02  
YMAX 1.253E+02

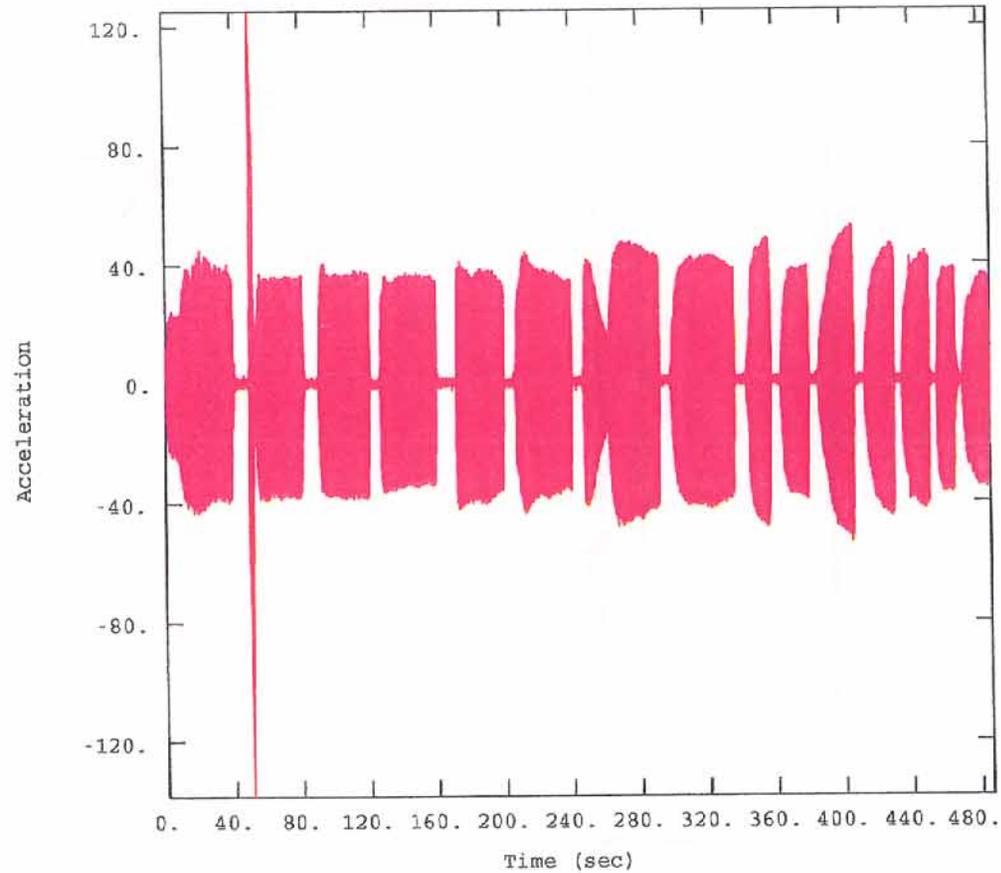


Figure b4

# ABAQUS

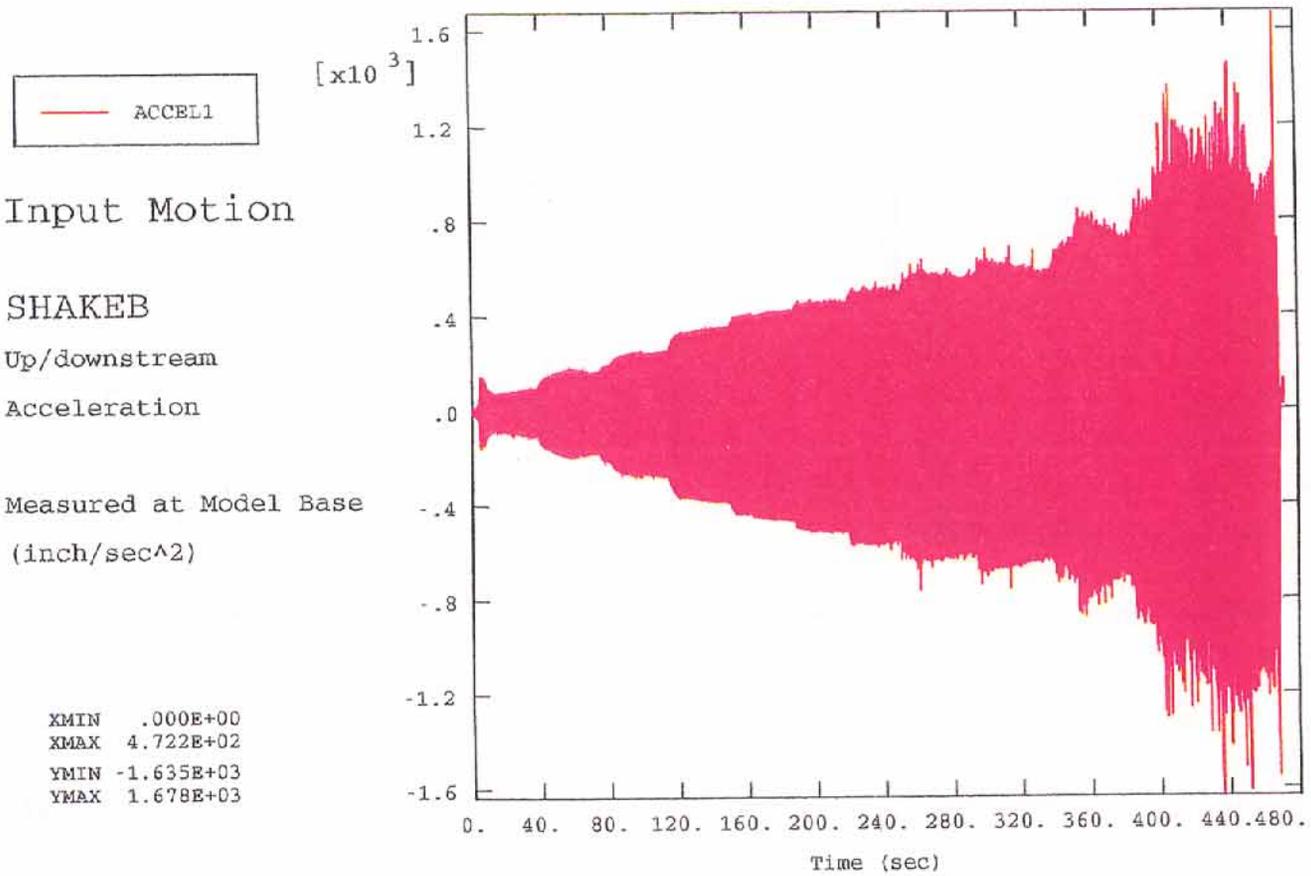
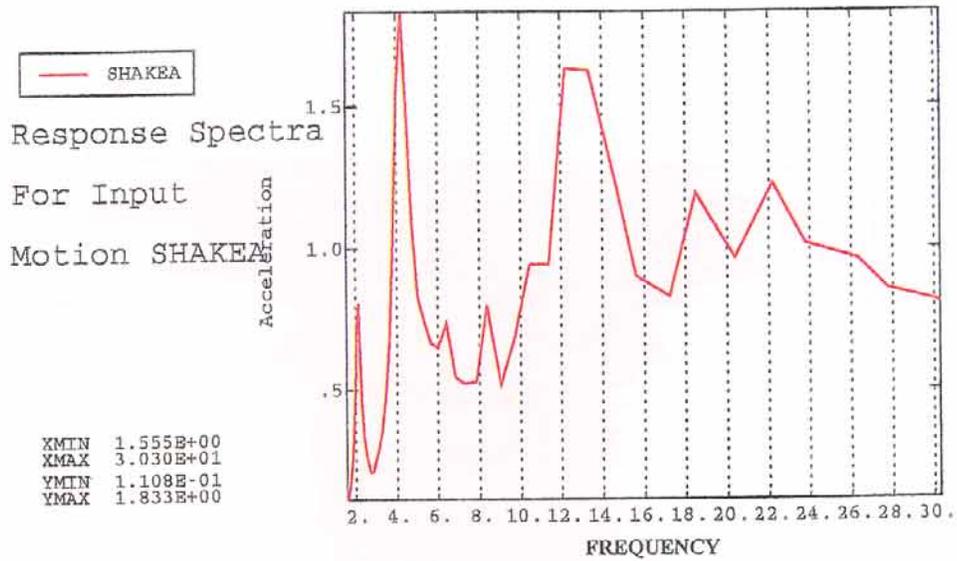


Figure b5

# ABAQUS



# ABAQUS

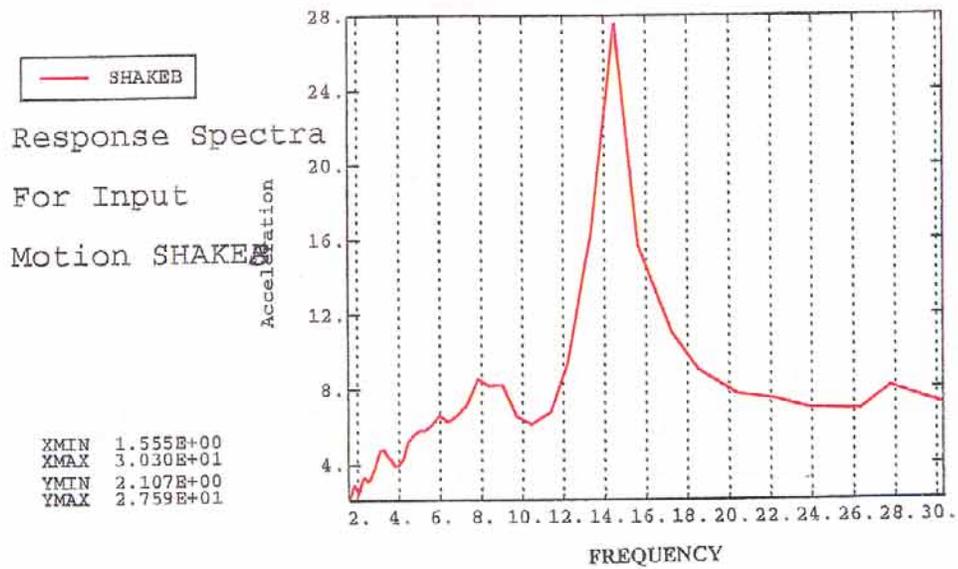


Figure b6

# ABAQUS

— LVDT1

Up/downstream  
Displacement  
Input Motion SHAKEB  
LVDT # 1  
(inches)

XMIN .000E+00  
XMAX 4.722E+02  
YMIN -1.811E-01  
YMAX 4.953E-02

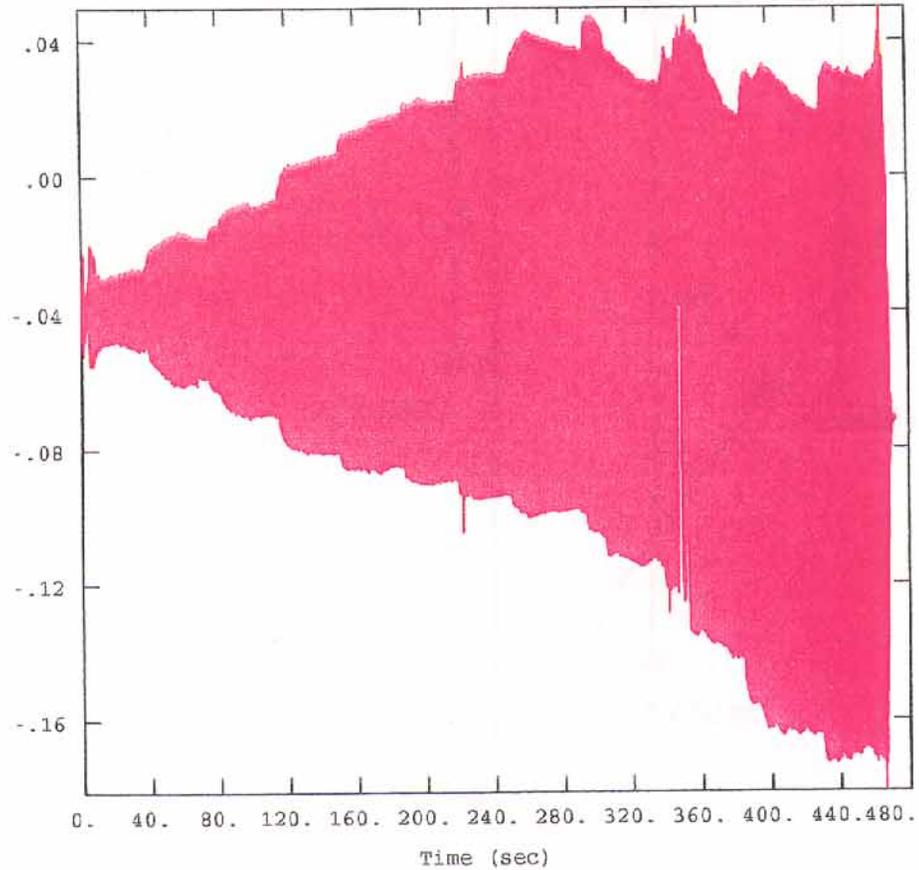
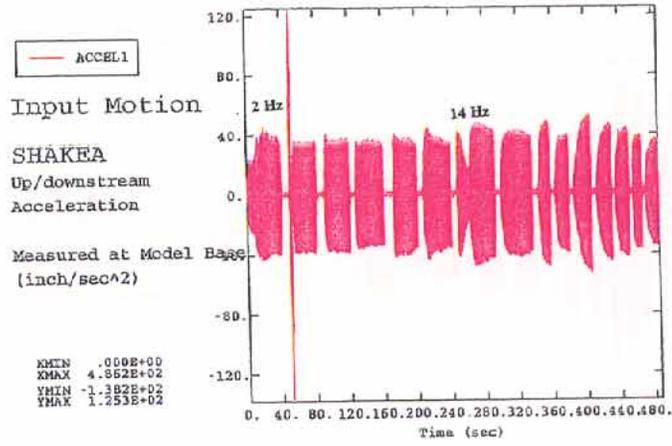
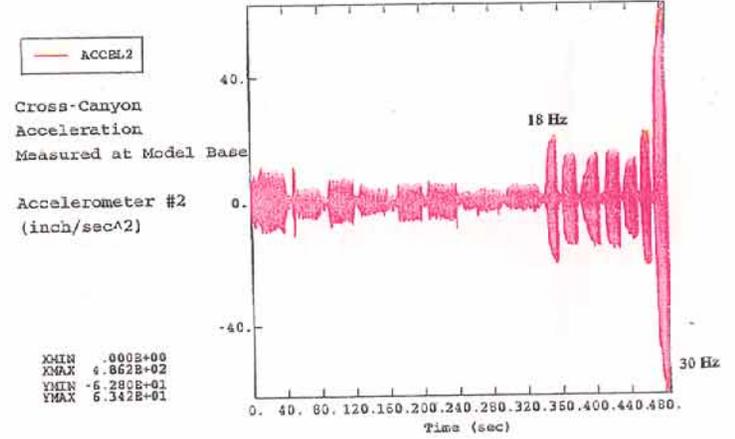


Figure b7

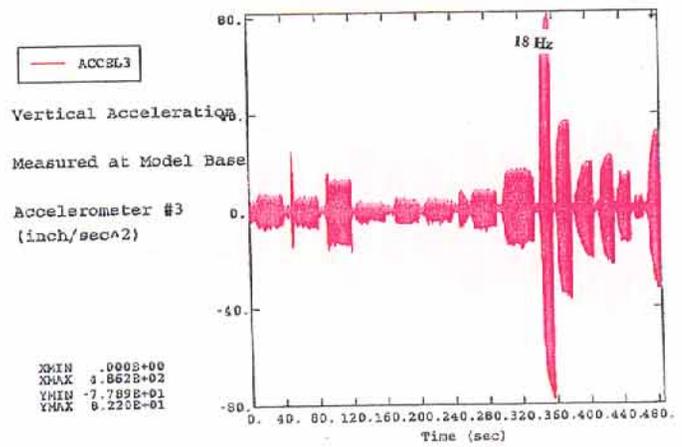
# ABAQUS



# ABAQUS



# ABAQUS



# ABAQUS

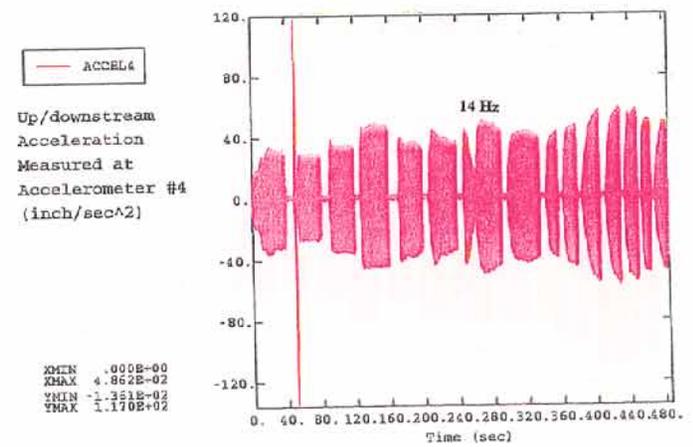
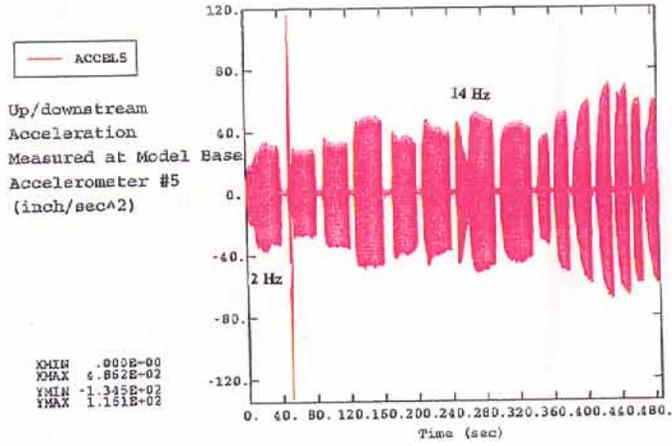
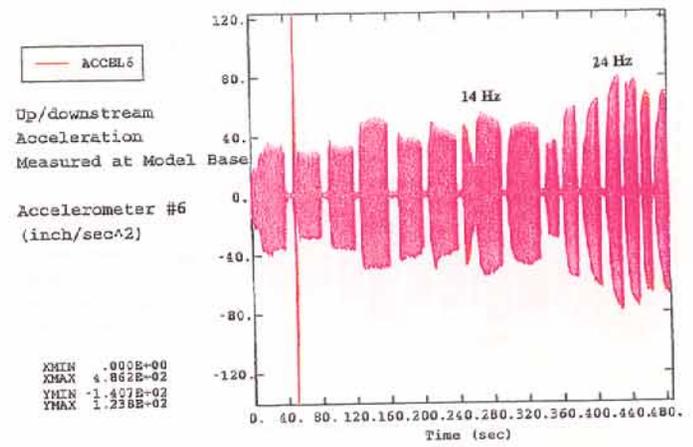


Figure c1

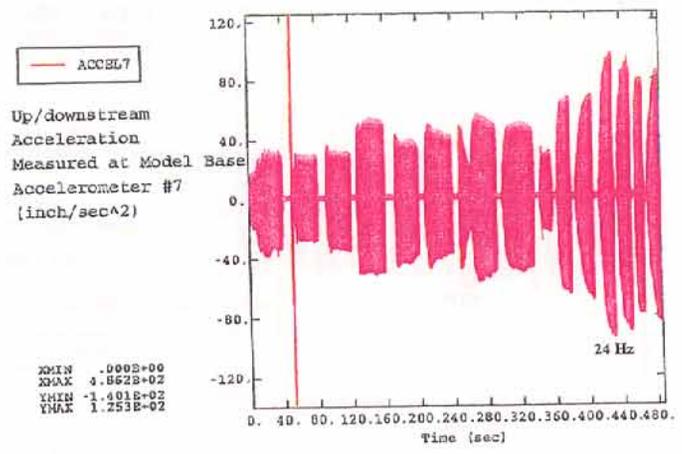
# ABAQUS



# ABAQUS



# ABAQUS



# ABAQUS

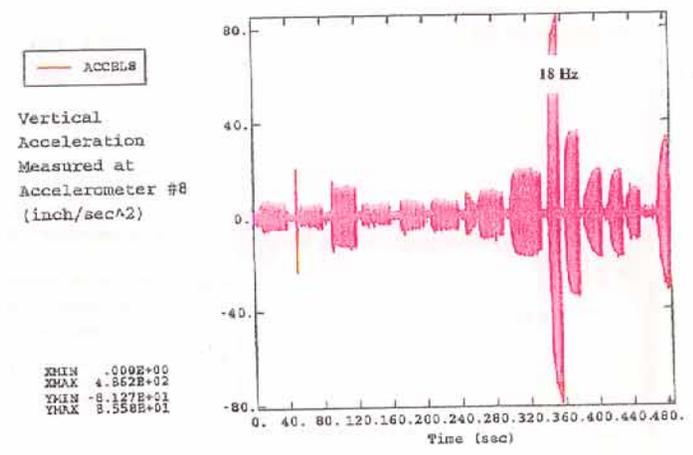


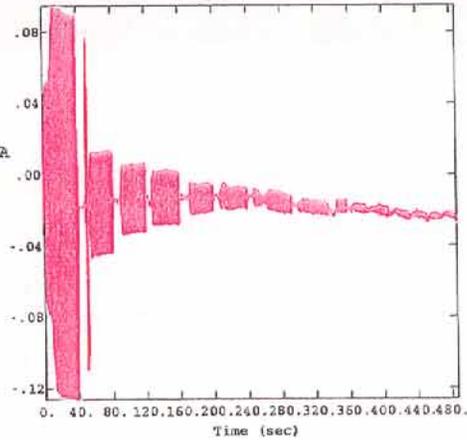
Figure c2

# ABAQUS

— LVDT1

Up/downstream  
Displacement  
Input Motion SHAKEA  
LVDT # 1  
(inches)

XMIN .000E+00  
XMAX 9.852E-02  
YMIN -1.262E-01  
YMAX 9.494E-02

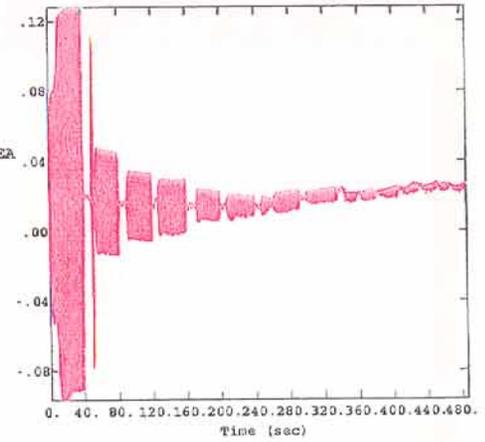


# ABAQUS

— LVDT2

Up/downstream  
Displacement  
Input Motion SHAKEA  
LVDT # 2  
(inches)

XMIN .000E+00  
XMAX 4.862E-02  
YMIN -9.638E-02  
YMAX 1.280E-01

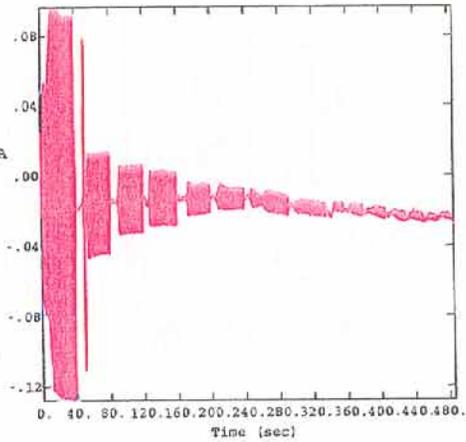


# ABAQUS

— LVDT3

Up/downstream  
Displacement  
Input Motion SHAKEA  
LVDT # 3  
(inches)

XMIN .000E+00  
XMAX 4.852E-02  
YMIN -1.233E-01  
YMAX 9.658E-02



# ABAQUS

— LVDT4

Up/downstream  
Displacement  
Input Motion SHAKEA  
LVDT # 4  
(inches)

XMIN .000E+00  
XMAX 4.862E-02  
YMIN -1.285E-01  
YMAX 9.738E-02

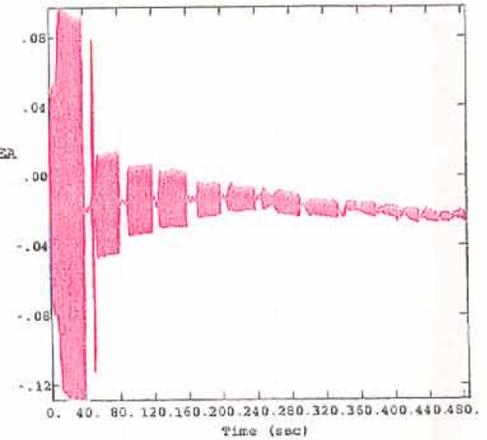
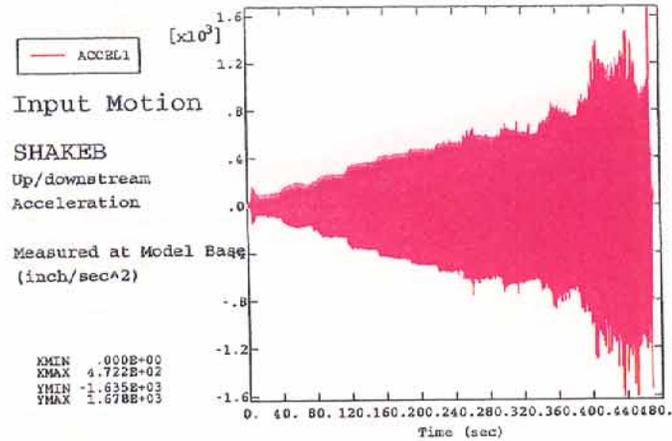
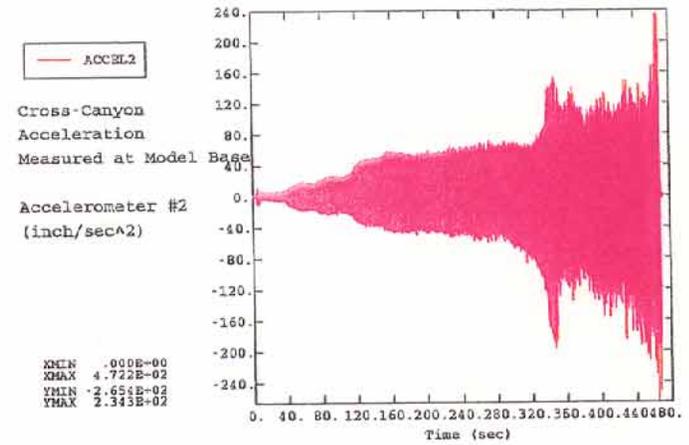


Figure C4

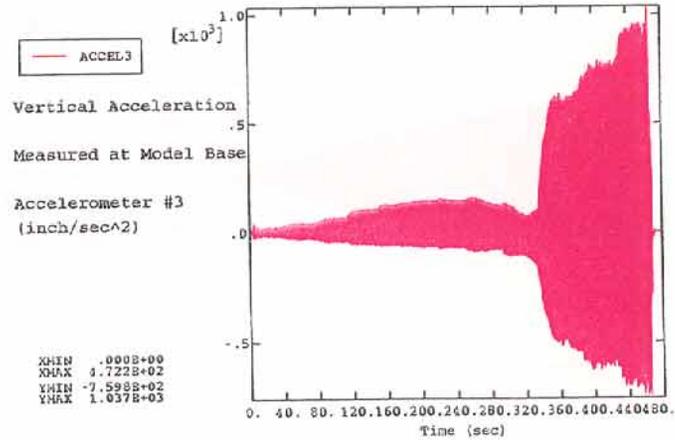
# ABAQUS



# ABAQUS



# ABAQUS



# ABAQUS

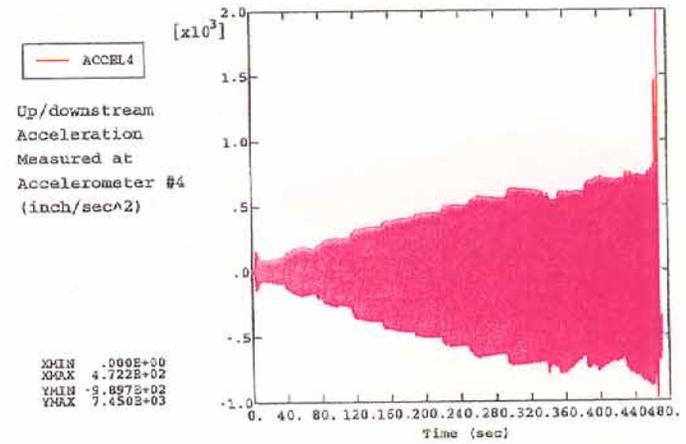
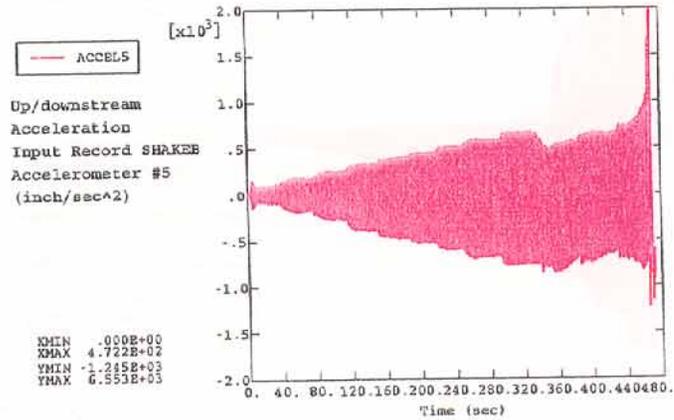
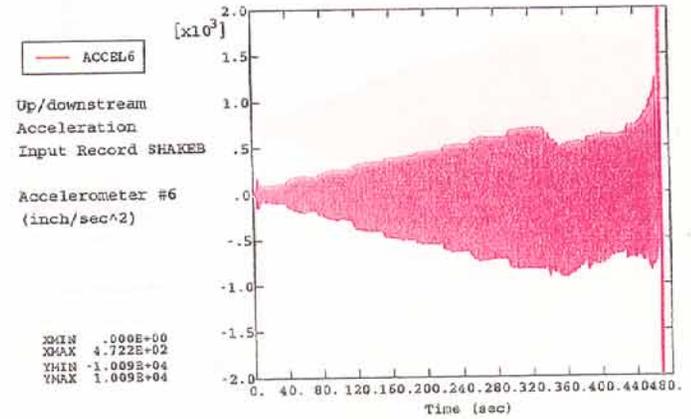


Figure c5

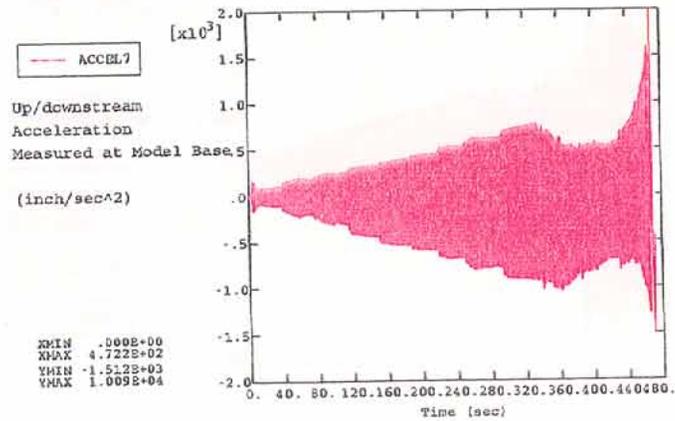
# ABAQUS



# ABAQUS



# ABAQUS



# ABAQUS

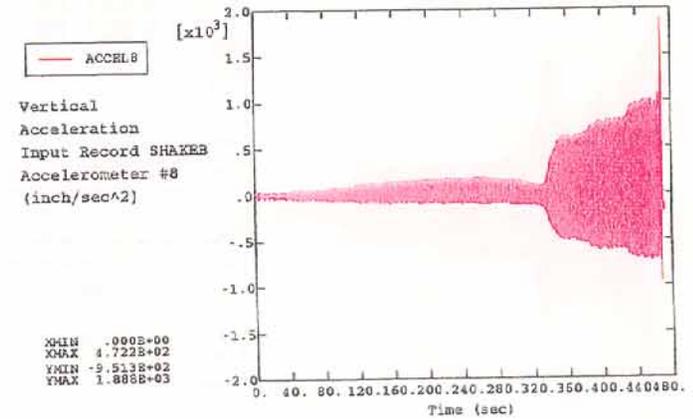
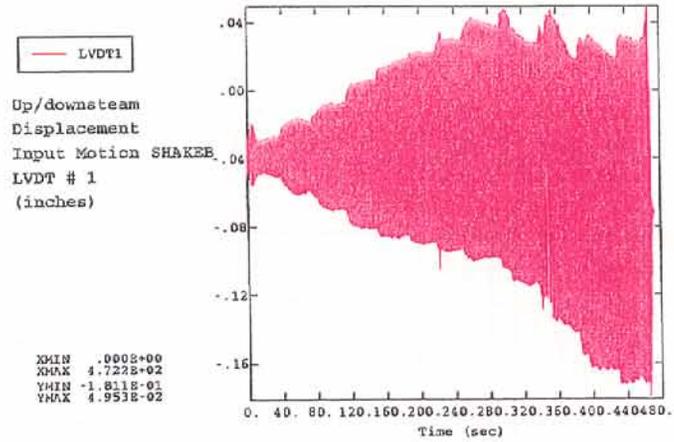
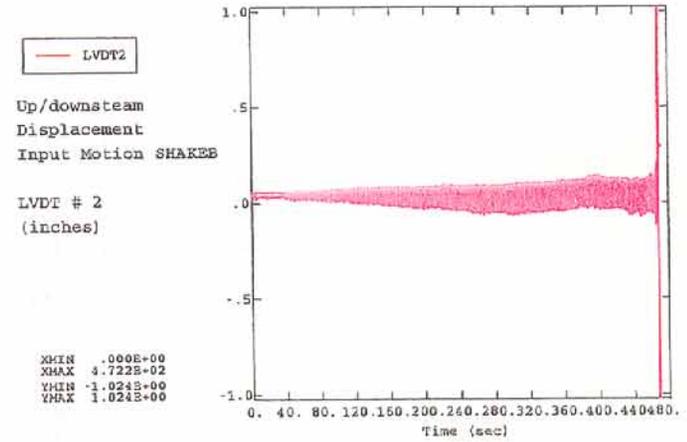


Figure c6

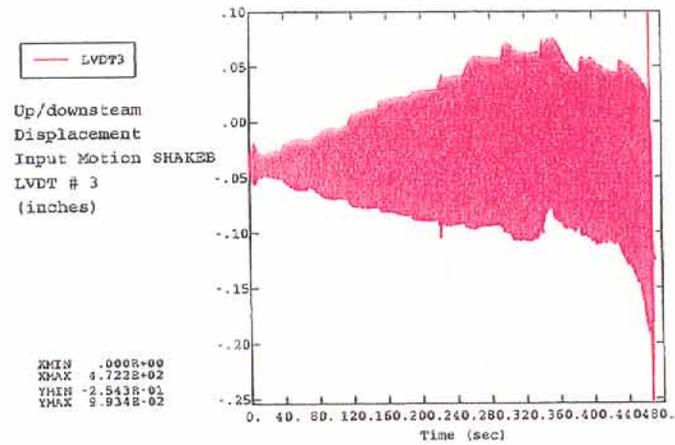
# ABAQUS



# ABAQUS



# ABAQUS



# ABAQUS

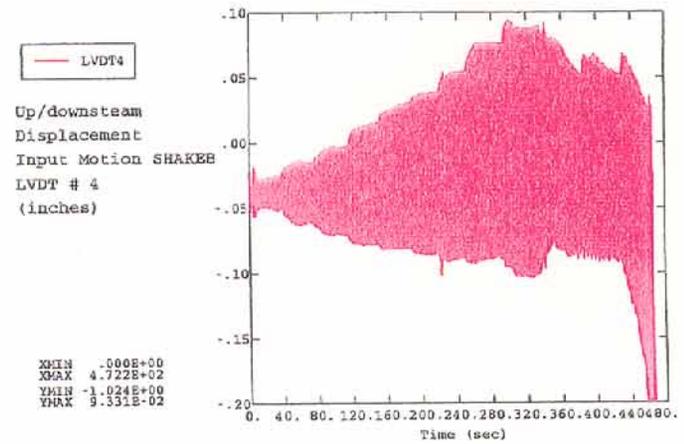


Figure c7

# Koyna Laboratory Model Test Final Cracking Pattern

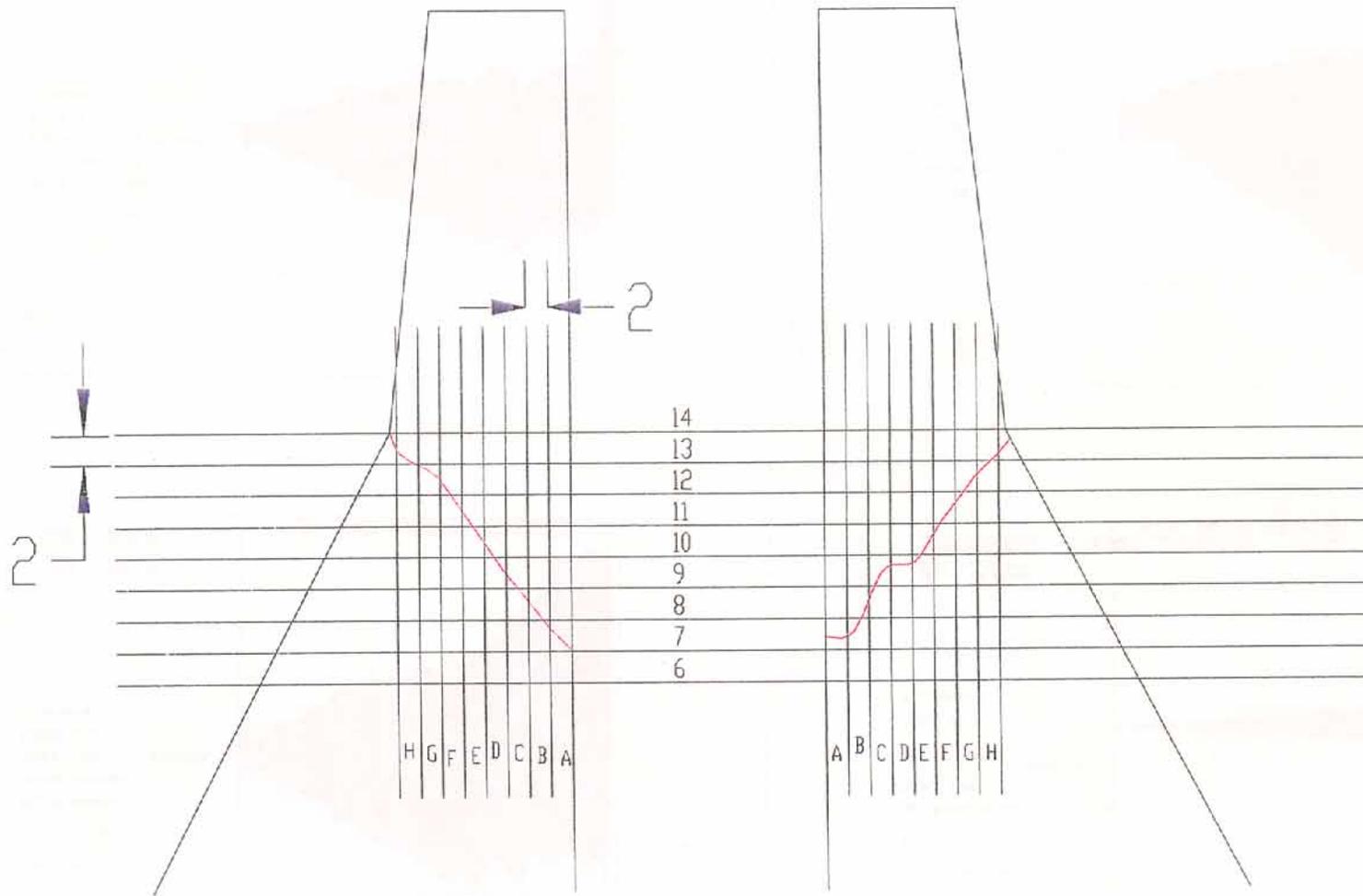


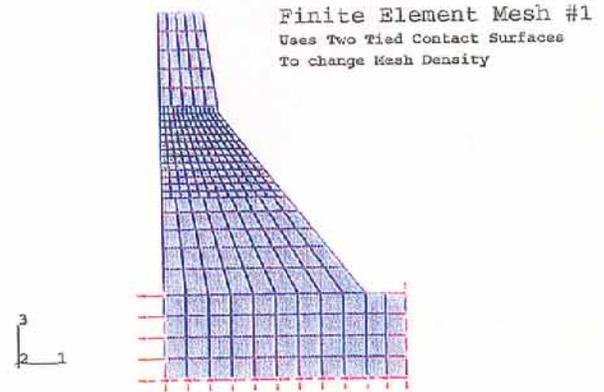
Figure c8

# ABAQUS

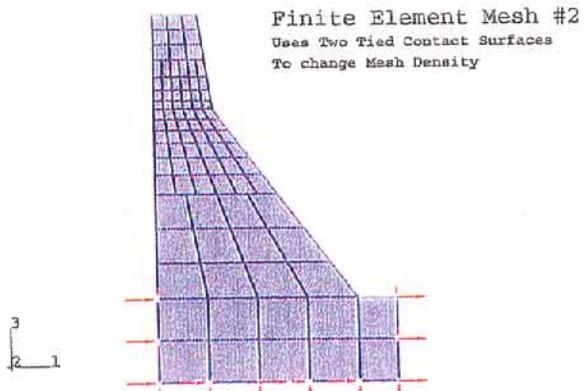
Koyna Laboratory Model Study  
Uncracked Model Study  
Used to Evaluate  
Linear and Non-linear  
Material Propertys  
For  
ABAQUS STANDARD & EXPLICIT

Determination of Mesh Sensitivity  
Non-linear Material Propertys  
Failure Stress = 55 psi  
Mode I Fracture Energy = 0.2012  
Crack Opening Strain = .001375

# ABAQUS



# ABAQUS



# ABAQUS

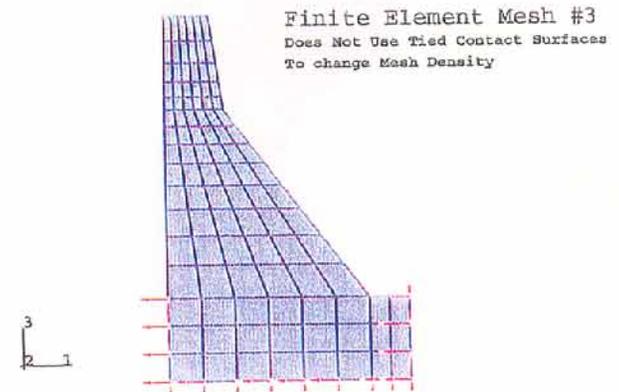


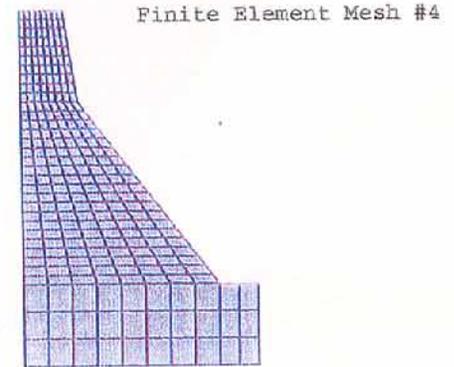
Figure d1

# ABAQUS

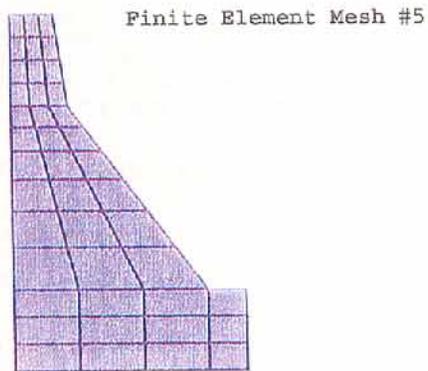
Koyna Laboratory Model Study  
Uncracked Model Study  
Used to Evaluate  
Linear and Non-linear  
Material Propertys  
For  
ABAQUS STANDARD & EXPLICIT

Determination of Mesh Sensitivity

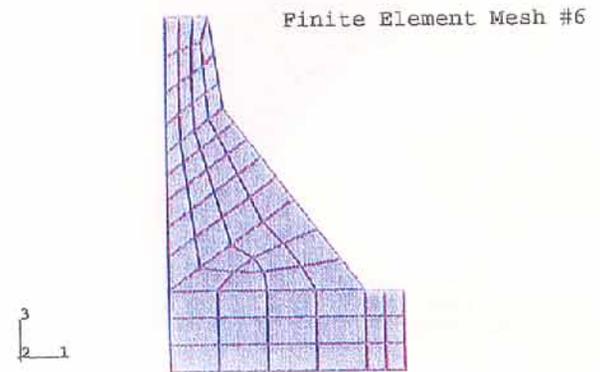
# ABAQUS



# ABAQUS



# ABAQUS



# ABAQUS

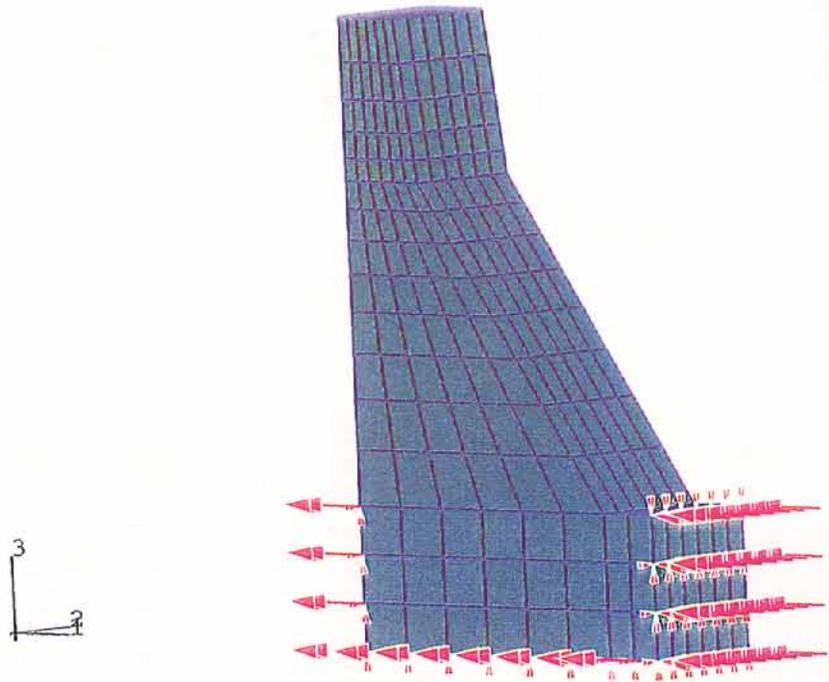


Figure d3

# ABAQUS

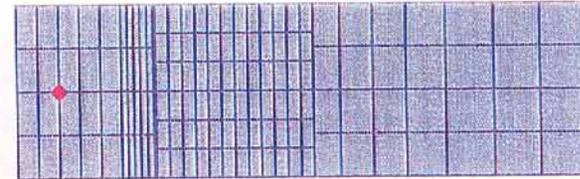
Koyna Laboratory Model Study  
Locations of Instrumentation  
Uncracked Model Study

Laboratory Test Model

Instrument	Elevation	Face	Corresponding Node
Accel04	49.6 inches	Upstream	503
Accel05	71.5 inches	Upstream	1534
Accel06	81.6 inches	Upstream	1955
Accel07	103.6 inches	Upstream	2075
Accel08	103.6 inches	Top	2085
LVDT01	23.6 inches	Downstream	298
LVDT02	49.6 inches	Upstream	503
LVDT03	61.6 inches	Downstream	1135
LVDT04	90.1 inches	Downstream	2010

# ABAQUS

Location of Nodes in ABAQUS Model ( Mesh #1 )  
Used for Comparisons  
of Disp. and Accel. Time Histories  
Vertical Accelerometer ACCEL08



Plan View - Node 2085 - Center of Top Face

# ABAQUS



Location of Nodes in  
ABAQUS Model ( Mesh #1 )  
Elev. View - Vertical Face  
Used for Comparisons of  
Disp. and Accel. Time Histories  
Horizontal Accelerometers

Node	Elevation
2075	103.6 inches
1955	82.3 inches
1534	70.9 inches
503	50.9 inches

# ABAQUS



Location of Nodes in  
ABAQUS Model ( Mesh #1 )  
Elev. View  
Downstream (Sloped) Face  
Used for Comparisons of  
Disp. and Accel. Time Histories

Horizontal LVDT's

Node	Elevation
2010	87.6 inches
1135	60.8 inches
298	23.6 inches

# ABAQUS

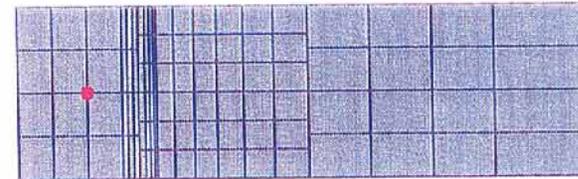
Koyna Laboratory Model Study  
Locations of Instrumentation  
Uncracked Model Study

Laboratory Test Model

Instrument	Elevation	Face	Corresponding Node
Accel104	49.6 inches	Upstream	118
Accel105	71.5 inches	Upstream	267
Accel106	81.6 inches	Upstream	610
Accel107	103.6 inches	Upstream	707
Accel108	103.6 inches	Top	717
LVDT01	23.6 inches	Downstream	8
LVDT02	49.6 inches	Upstream	118
LVDT03	61.6 inches	Downstream	407
LVDT04	90.1 inches	Downstream	762

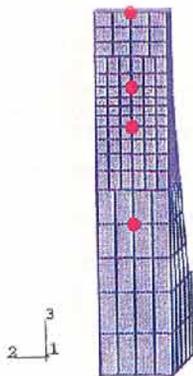
# ABAQUS

Location of Nodes in ABAQUS Model ( Mesh #2 )  
Used for Comparisons  
of Disp. and Accel. Time Histories  
Vertical Accelerometer ACCEL08



Plan View - Node 717 - Center of Top Face

# ABAQUS



Location of Nodes in  
ABAQUS Model ( Mesh #2 )  
Elev. View - Vertical Face  
Used for Comparisons of  
Disp. and Accel. Time Histories  
Horizontal Accelerometers

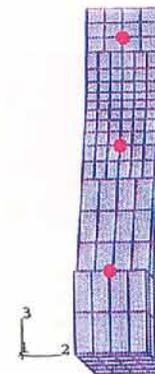
Node	Elevation
707	103.6 inches
610	82.3 inches
267	70.9 inches
118	43.1 inches

# ABAQUS

Location of Nodes in  
ABAQUS Model ( Mesh #2 )  
Elev. View  
Downstream (Sloped) Face  
Used for Comparisons of  
Disp. and Accel. Time Histories

Horizontal LVDT's

Node	Elevation
762	95.1 inches
407	63.2 inches
8	23.6 inches



# ABAQUS

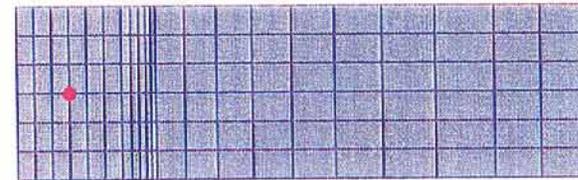
Koyna Laboratory Model Study  
Locations of Instrumentation  
Uncracked Model Study

Laboratory Test Model

Instrument	Elevation	Face	Corresponding Node
Accel04	49.6 inches	Upstream	519
Accel05	71.5 inches	Upstream	419
Accel06	81.6 inches	Upstream	204
Accel07	103.6 inches	Upstream	176
Accel08	103.6 inches	Top	179
LVDT01	23.6 inches	Downstream	859
LVDT02	49.6 inches	Upstream	519
LVDT03	61.6 inches	Downstream	511
LVDT04	90.1 inches	Downstream	196

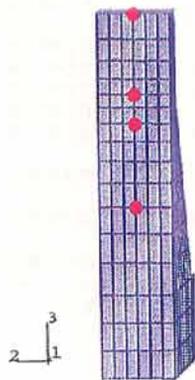
# ABAQUS

Location of Nodes in ABAQUS Model ( Mesh#3 )  
Used for Comparisons  
of Disp. and Accel. Time Histories  
Vertical Accelerometer ACCEL08



2  
Plan View - Node 179 - Center of Top Face

# ABAQUS



Location of Nodes in  
ABAQUS Model ( Mesh #3 )  
Elev. View - Vertical Face  
Used for Comparisons of  
Disp. and Accel. Time Histories  
Horizontal Accelerometers

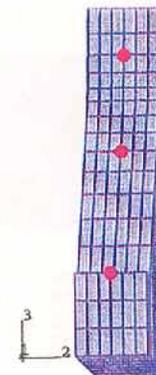
Node	Elevation
176	103.6 inches
204	80.6 inches
491	72.3 inches
519	48.6 inches

# ABAQUS

Location of Nodes in  
ABAQUS Model ( Mesh#3 )  
Elev. View  
Downstream (Sloped) Face  
Used for Comparisons of  
Disp. and Accel. Time Histories

Horizontal LVDT's

Node	Elevation
196	90.1 inches
511	61.6 inches
859	23.6 inches



# ABAQUS

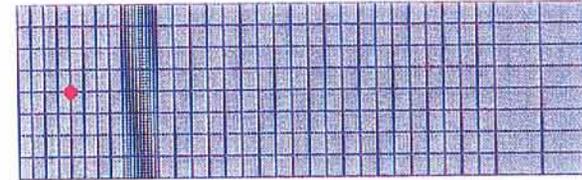
Koyna Laboratory Model Study  
Locations of Instrumentation  
Uncracked Model Study

Laboratory Test Model

Instrument	Elevation	Face	Corresponding Node
Accel04	49.6 inches	Upstream	118
Accel05	71.5 inches	Upstream	267
Accel06	81.6 inches	Upstream	610
Accel07	103.6 inches	Upstream	707
Accel08	103.6 inches	Top	717
LVDT01	23.6 inches	Downstream	8
LVDT02	49.6 inches	Upstream	118
LVDT03	61.6 inches	Downstream	407
LVDT04	90.1 inches	Downstream	762

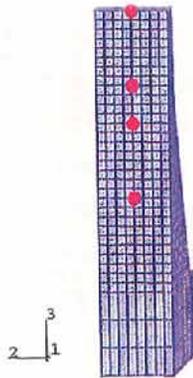
# ABAQUS

Location of Nodes in ABAQUS Model ( Mesh #4 )  
Used for Comparisons  
of Disp. and Accel. Time Histories  
Vertical Accelerometer ACCEL08



Plan View - Node 401 - Center of Top Face

# ABAQUS

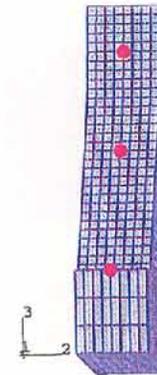


Location of Nodes in  
ABAQUS Model ( Mesh #2 )  
Elev. View - Vertical Face  
Used for Comparisons of  
Disp. and Accel. Time Histories  
Horizontal Accelerometers

Node	Elevation
397	103.6 inches
469	82.2 inches
1621	71.6 inches
1693	50.3 inches

# ABAQUS

Location of Nodes in  
ABAQUS Model ( Mesh #4 )  
Elev. View  
Downstream (Sloped) Face  
Used for Comparisons of  
Disp. and Accel. Time Histories



Horizontal LVDT's

Node	Elevation
450	90.3 inches
1665	60.9 inches
2788	23.6 inches

# ABAQUS

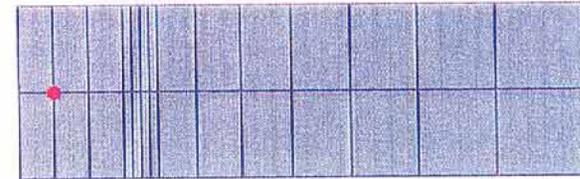
Koyna Laboratory Model Study  
Locations of Instrumentation  
Uncracked Model Study

Laboratory Test Model

Instrument	Elevation	Face	Corresponding Node
Accel04	49.6 inches	Upstream	118
Accel05	71.5 inches	Upstream	267
Accel06	81.6 inches	Upstream	610
Accel07	103.6 inches	Upstream	707
Accel08	103.6 inches	Top	717
LVDT01	23.6 inches	Downstream	8
LVDT02	49.6 inches	Upstream	118
LVDT03	61.6 inches	Downstream	407
LVDT04	90.1 inches	Downstream	762

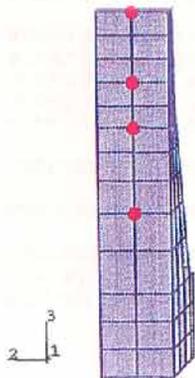
# ABAQUS

Location of Nodes in ABAQUS Model ( Mesh #5 )  
Used for Comparisons  
of Disp. and Accel. Time Histories  
Vertical Accelerometer ACCEL08



Plan View - Node 22 - Center of Top Face

# ABAQUS



Location of Nodes in  
ABAQUS Model ( Mesh #5 )  
Elev. View - Vertical Face  
Used for Comparisons of  
Disp. and Accel. Time Histories  
Horizontal Accelerometers

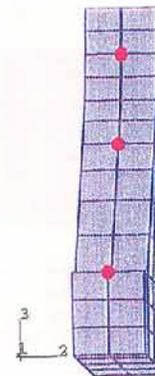
Node	Elevation
21	103.6 inches
33	83.6 inches
85	70.7 inches
97	46.4 inches

# ABAQUS

Location of Nodes in  
ABAQUS Model ( Mesh #5 )  
Elev. View  
Downstream (Sloped) Face  
Used for Comparisons of  
Disp. and Accel. Time Histories

Horizontal LVDT's

Node	Elevation
32	90.3 inches
92	63.8 inches
173	23.6 inches



# ABAQUS

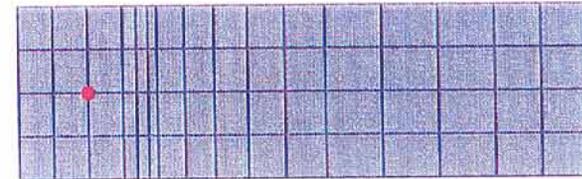
Koyna Laboratory Model Study  
Locations of Instrumentation  
Uncracked Model Study

Laboratory Test Model

Instrument	Elevation	Face	Corresponding Node
Accel04	49.6 inches	Upstream	196
Accel05	71.5 inches	Upstream	104
Accel06	81.6 inches	Upstream	124
Accel07	103.6 inches	Upstream	163
Accel08	103.6 inches	Top	165
LVDT01	23.6 inches	Downstream	289
LVDT02	49.6 inches	Upstream	196
LVDT03	61.6 inches	Downstream	232
LVDT04	90.1 inches	Downstream	140

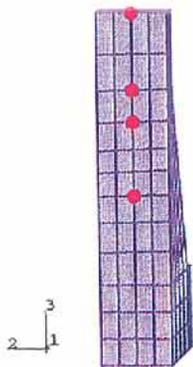
# ABAQUS

Location of Nodes in ABAQUS Model ( Mesh#6 )  
Used for Comparisons  
of Disp. and Accel. Time Histories  
Vertical Accelerometer ACCEL08



Plan View - Node 165 - Center of Top Face

# ABAQUS



Location of Nodes in  
ABAQUS Model ( Mesh #6 )  
Elev. View - Vertical Face  
Used for Comparisons of  
Disp. and Accel. Time Histories  
Horizontal Accelerometers

Node	Elevation
163	103.6 inches
124	80.8 inches
104	71.5 inches
196	49.8 inches

# ABAQUS

Location of Nodes in  
ABAQUS Model ( Mesh#6 )  
Elev. View  
Downstream (Sloped) Face  
Used for Comparisons of  
Disp. and Accel. Time Histories

Horizontal LVDT's

Node	Elevation
140	92.8 inches
232	62.5 inches
289	23.6 inches



# ABAQUS

— ACTLVDT

LVDT Displacement  
Record In  
Actuator  
(inches)

XMIN .000E+00  
XMAX 4.862E+02  
YMIN -1.056E-01  
YMAX 1.397E-01

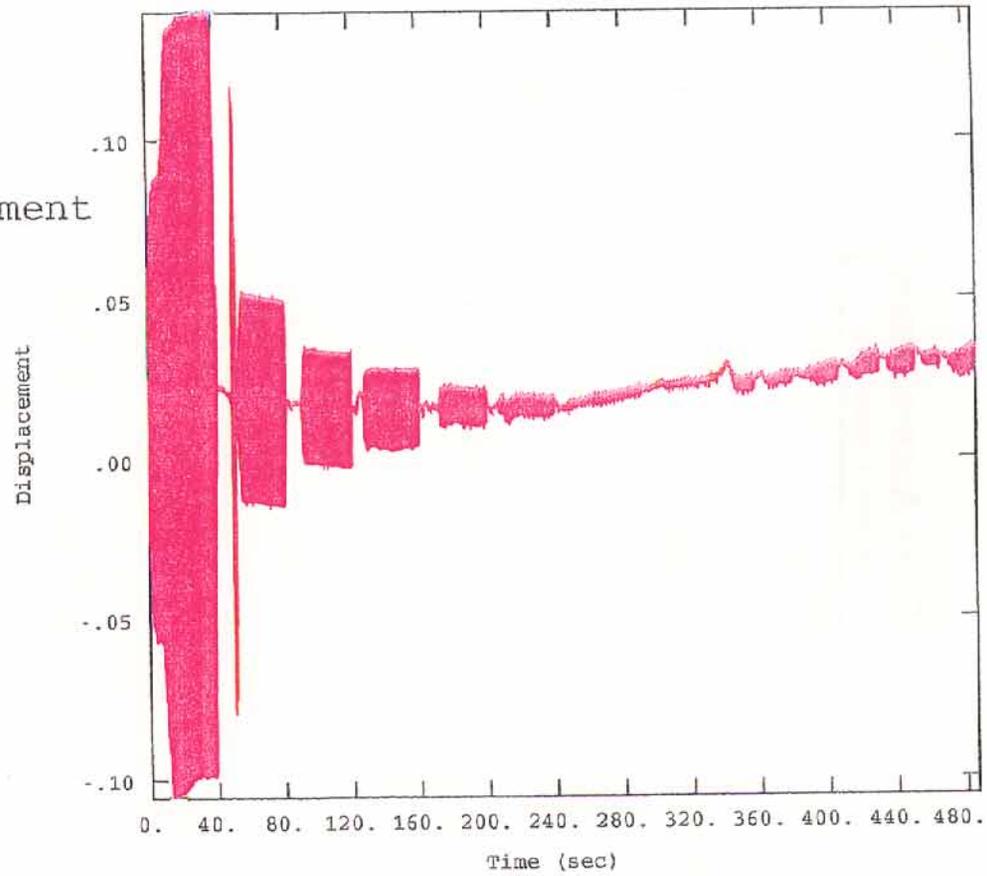


Figure e1

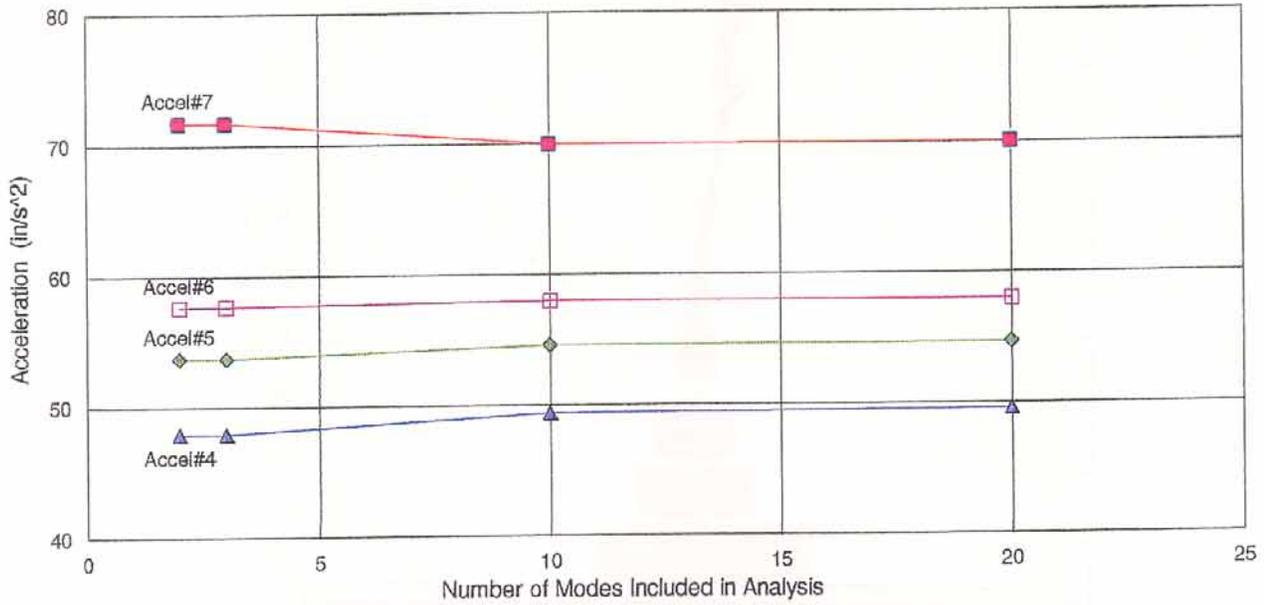
Uncracked Koyna Laboratory Study  
 Determination of the Number of Modes Required  
 Mesh#3

Material Properties

E = 150 ksi  
 Material Density = 138.2 pcf

Damping = 5% critical  
 Rayleigh Damping Factors  
 Alpha=2.827433, Beta=.000318

**Peak Accelerations**  
 Number of Modes Varied



Peak Accelerations ( inch / sec ^ 2 )

Number of Modes Used	2	3	10	20	LAB
Accel#7	71.71	71.71	69.98	69.99	53.26
Accel#6	57.60	57.66	57.99	57.99	51.72
Accel#5	53.67	53.67	54.55	54.64	49.26
Accel#4	47.89	47.89	49.35	49.56	47.72
CPU Time (sec)	53.04	56.91	163.21	210.94	

Figure e2

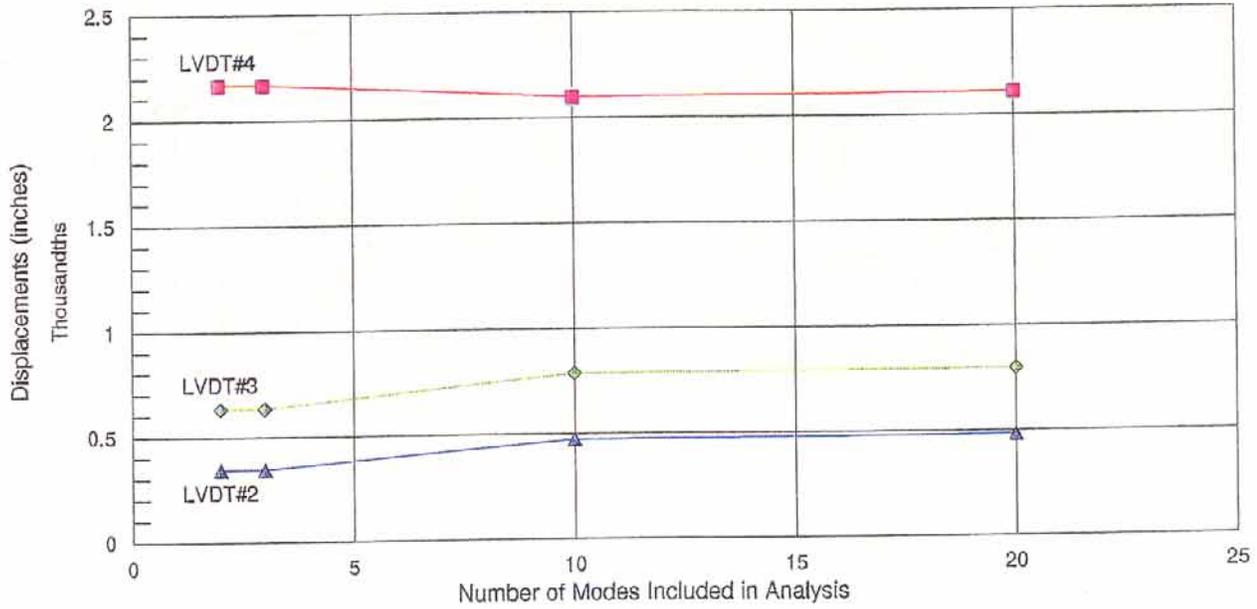
Uncracked Koyna Laboratory Study  
 Determination of the Number of Modes Required  
 Mesh#3

Material Properties

E = 150 ksi  
 Material Density = 138.2 pcf

Damping = 5% critical  
 Rayleigh Damping Factors  
 Alpha=2.827433, Beta=.000318

**Peak Displacements**  
 Number of Modes Varied



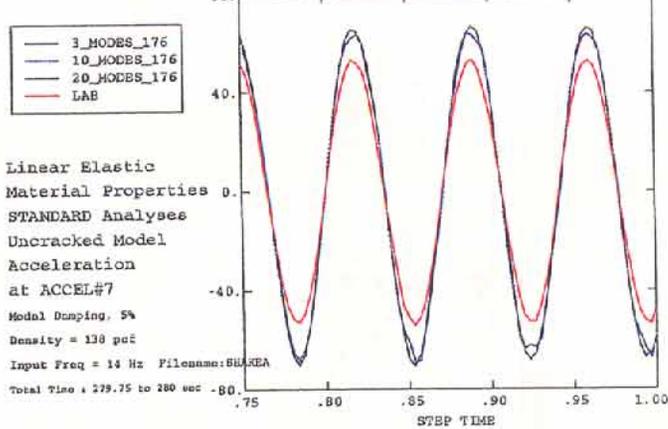
Peak Displacements ( inches )

Number of Modes Used	2	3	10	20	LAB
LVDT#4	2.2E-03	2.2E-03	2.1E-03	2.1E-03	7.2E-04
LVDT#3	6.3E-04	6.3E-04	7.9E-04	7.9E-04	3.1E-04
LVDT#2	3.4E-04	3.4E-04	4.7E-04	4.8E-04	2.1E-04

Figure e3

# ABAQUS

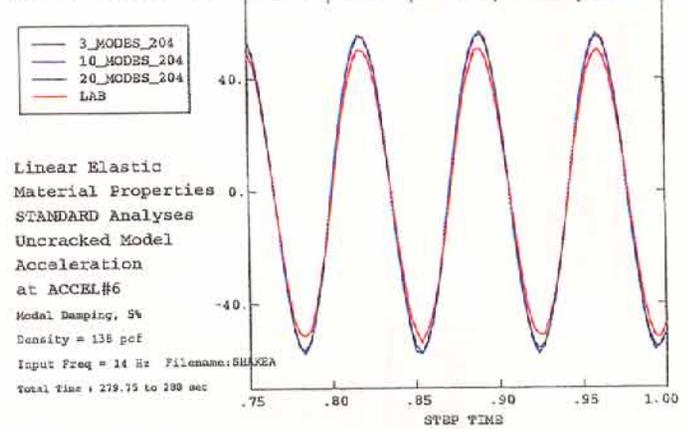
Number of Modes Extracted in Frequency Analysis Varied



ABAQUS Modal Dynamic Analyses vs Laboratory Measurements

# ABAQUS

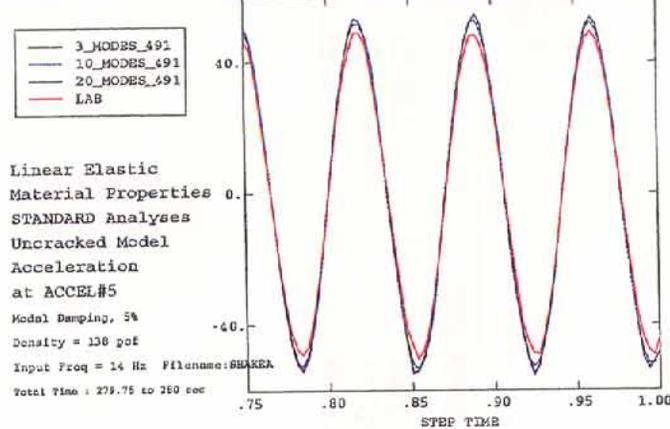
Number of Modes Extracted in Frequency Analysis Varied



ABAQUS Modal Dynamic Analyses vs Laboratory Measurements

# ABAQUS

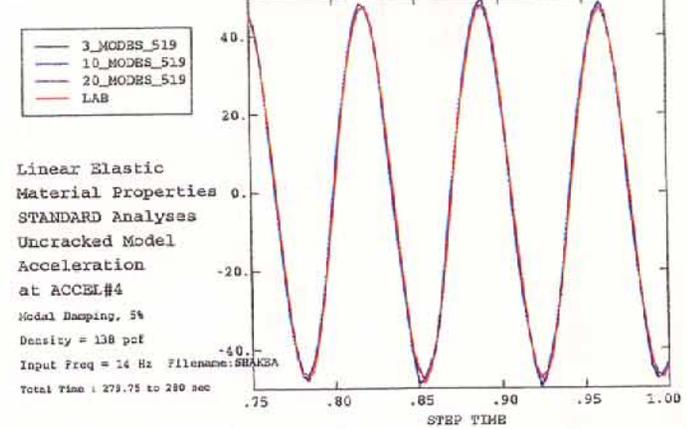
Number of Modes Extracted in Frequency Analysis Varied



ABAQUS Modal Dynamic Analyses vs Laboratory Measurements

# ABAQUS

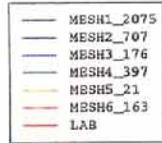
Number of Modes Extracted in Frequency Analysis Varied



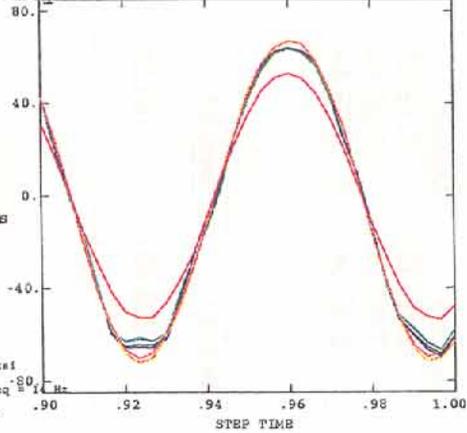
ABAQUS Modal Dynamic Analyses vs Laboratory Measurements

# ABAQUS

## Mesh Sensitivity



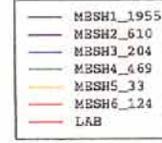
Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model  
Acceleration  
at ACCEL#7  
Modal Damping, 5%  
Density=138 pcf, E = 150 ksi  
Filename:SHAKEA, Input Freq = 14 Hz  
Total Time = 279.75 to 280 sec



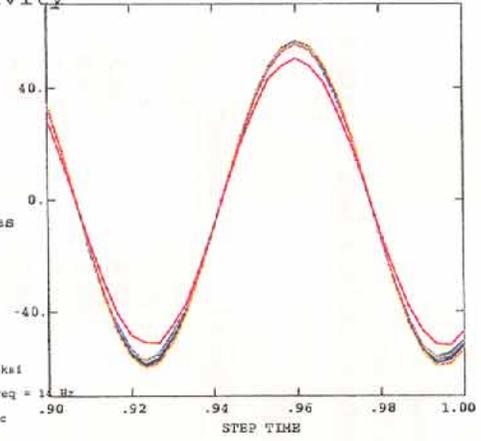
ABAQUS Modal Dynamic Analyses & Laboratory Measurements

# ABAQUS

## Mesh Sensitivity



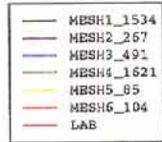
Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model  
Acceleration  
at ACCEL#6  
Modal Damping, 5%  
Density=138 pcf, E = 150 ksi  
Filename:SHAKEA, Input Freq = 14 Hz  
Total Time = 279.75 to 280 sec



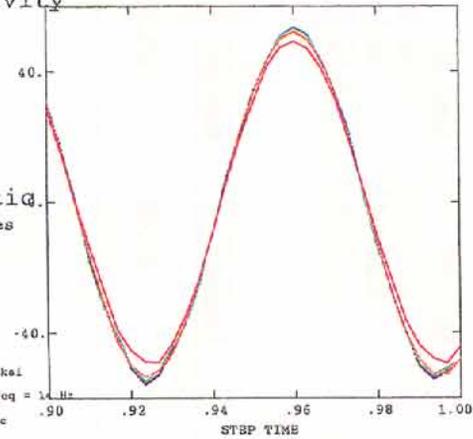
ABAQUS Modal Dynamic Analyses & Laboratory Measurements

# ABAQUS

## Mesh Sensitivity



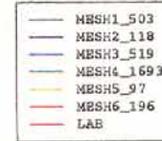
Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model  
Acceleration  
at ACCEL#5  
Modal Damping, 5%  
Density=138 pcf, E = 150 ksi  
Filename:SHAKEA, Input Freq = 14 Hz  
Total Time = 279.75 to 280 sec



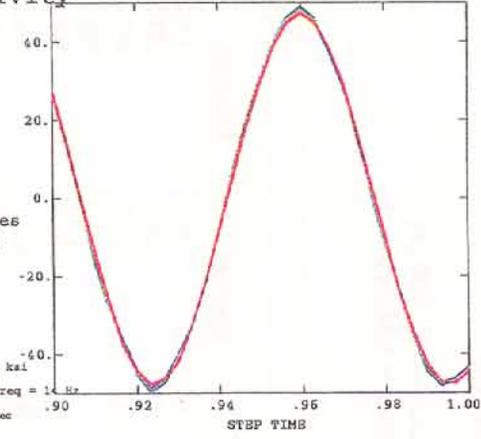
ABAQUS Modal Dynamic Analyses & Laboratory Measurements

# ABAQUS

## Mesh Sensitivity



Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model  
Acceleration  
at ACCEL#4  
Modal Damping, 5%  
Density=138 pcf, E = 150 ksi  
Filename:SHAKEA, Input Freq = 14 Hz  
Total Time = 279.75 to 280 sec



ABAQUS Modal Dynamic Analyses & Laboratory Measurements

# ABAQUS

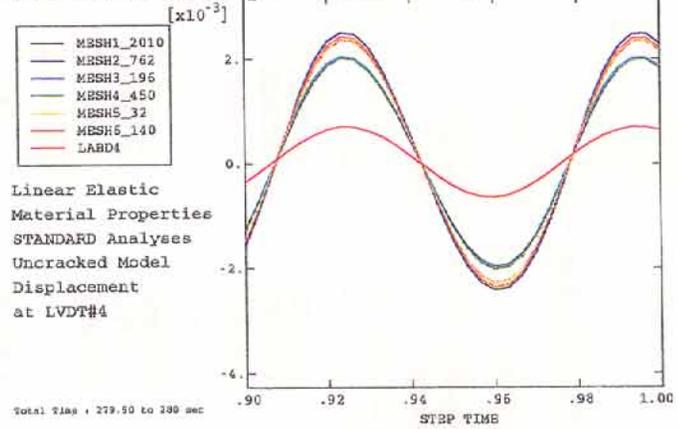
Koyna Laboratory Model Study  
 Uncracked Model Study  
 Sensitivity Study  
 Mesh Density

Comparison of Displacements  
 ABAQUS STANDARD  
 Modal Dynamic Analysis

Input Record SHAKEA  
 Modal Damping, 3.5%  
 Elastic Modulus = 150 ksi  
 Density = 138.2 pcf

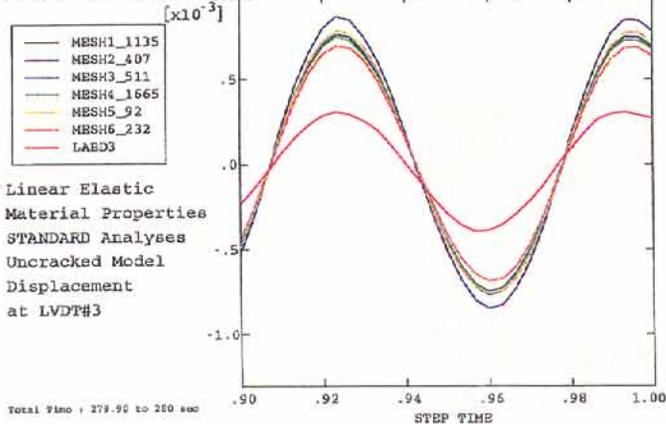
# ABAQUS

## Mesh Sensitivity



# ABAQUS

## Mesh Sensitivity



# ABAQUS

## Mesh Sensitivity

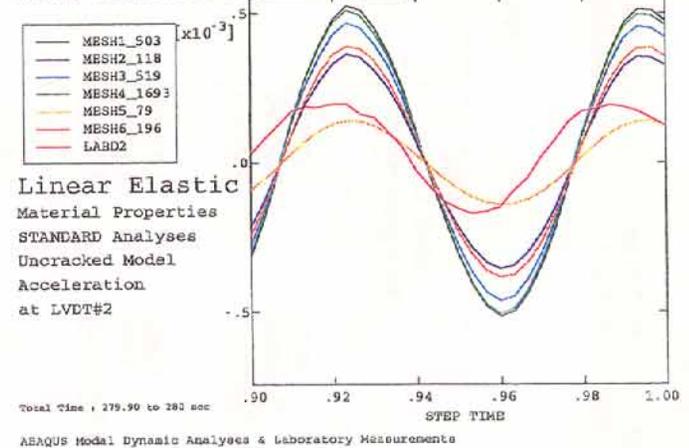


Figure 13

ABAQUS

Response Spectrum Analysis

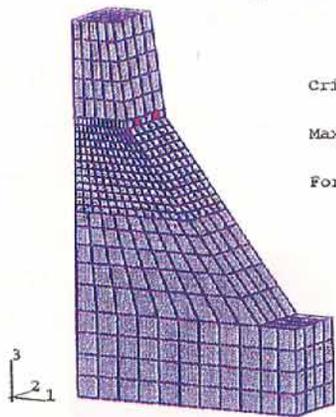
Mesh#1

Critical Element #1366,1369

Maximum Principal Stress

For Input Record SHAKEA

23.04 psi



ABAQUS

Response Spectrum Analysis

Mesh#2

Critical Elements #120 & #123

Maximum Principal Stress

For Input Record SHAKEA

15.22 psi

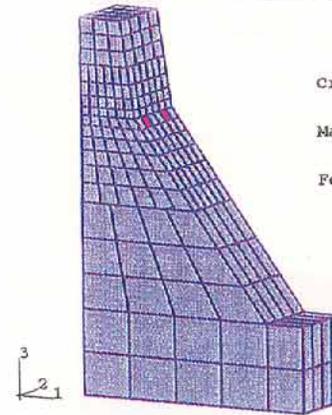
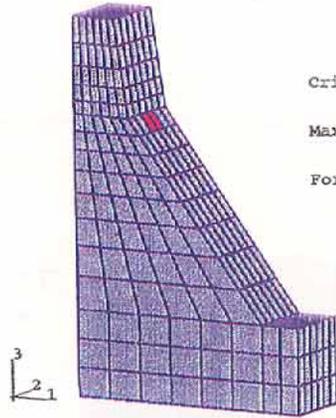


Figure F5

# ABAQUS

## Response Spectrum Analysis



Mesh#3

Critical Element #282 & #330

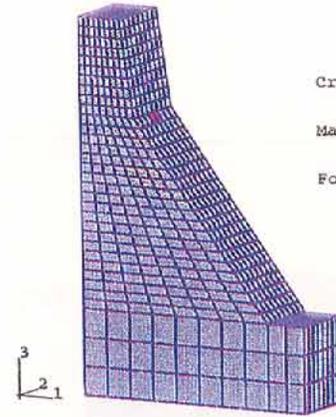
Maximum Principal Stress

For Input Record SHAKEA

14.59 psi

# ABAQUS

## Response Spectrum Analysis



Mesh#4

Critical Elements #1128 & #1288

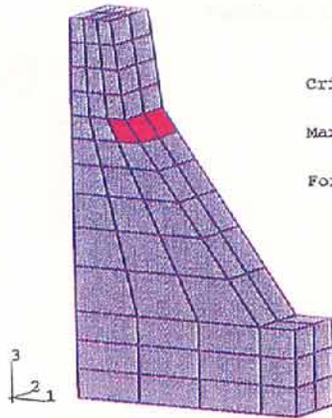
Maximum Principal Stress

For Input Record SHAKEA

17 psi

# ABAQUS

## Response Spectrum Analysis



Mesh#5

Critical Elements #27 & #45

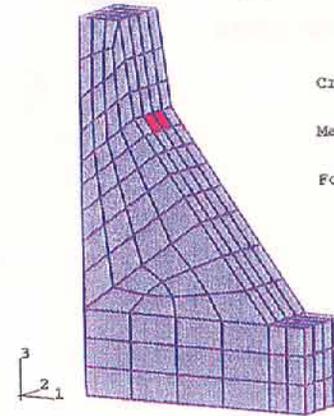
Maximum Principal Stress

For Input Record SHAKEA

9.42 psi

# ABAQUS

## Response Spectrum Analysis



Mesh#6

Critical Elements #74 & #75

Maximum Principal Stress

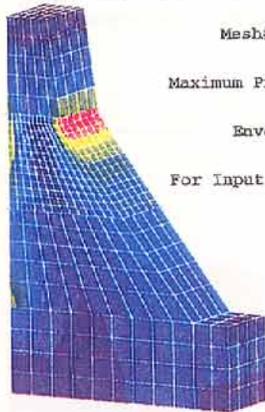
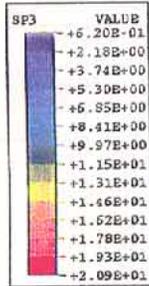
For Input Record SHAKEA

9.35 psi

Figure F6

ABAQUS

Response Spectrum Analysis



Mesh#1

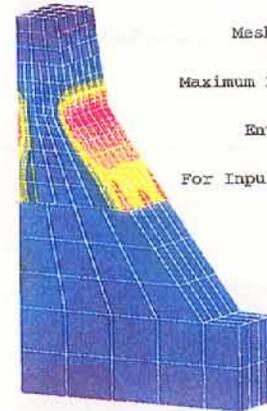
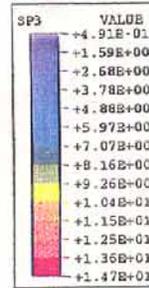
Maximum Principal Stress

Envelope

For Input Record SHAKEA

ABAQUS

Response Spectrum Analysis



Mesh#2

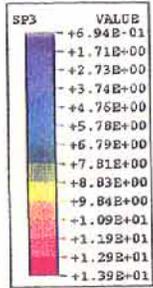
Maximum Principal Stress

Envelope

For Input Record SHAKEA

Figure f7

ABAQUS



Response Spectrum Analysis

Mesh#3

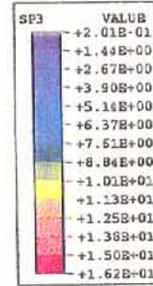
Maximum Principal Stress

Envelope

For Input Record SHAKEA



ABAQUS



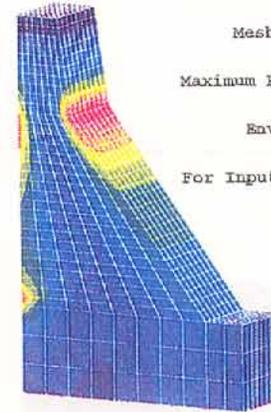
Response Spectrum Analysis

Mesh#4

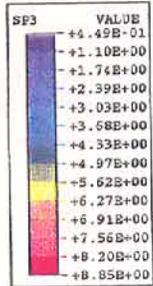
Maximum Principal Stress

Envelope

For Input Record SHAKEA



ABAQUS



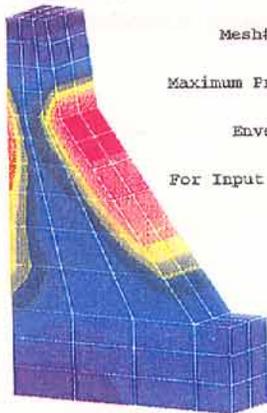
Response Spectrum Analysis

Mesh#5

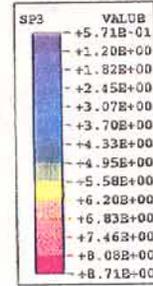
Maximum Principal Stress

Envelope

For Input Record SHAKEA



ABAQUS



Response Spectrum Analysis

Mesh#6

Maximum Principal Stress

Envelope

For Input Record SHAKEA

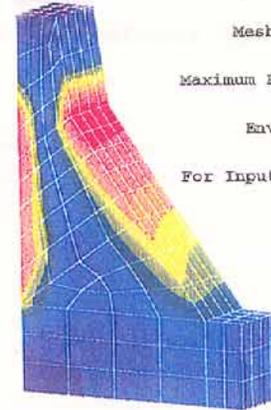


Figure F8

ABAQUS

Response Spectrum Analysis

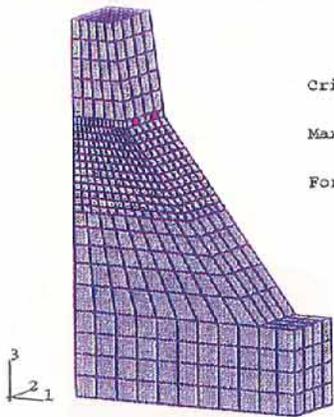
Mesh#1

Critical Element #1366,1369

Maximum Principal Stress

For Input Record SHAKEB

227.60 psi



ABAQUS

Response Spectrum Analysis

Mesh#2

Critical Elements #120 & #123

Maximum Principal Stress

For Input Record SHAKEB

149 psi

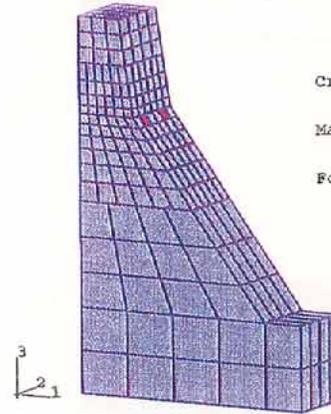
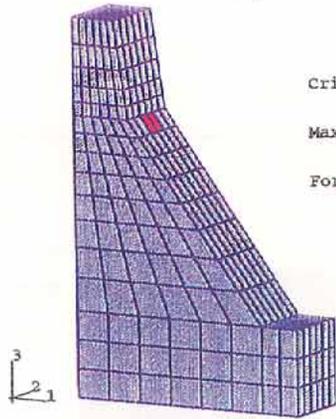


Figure F9

ABAQUS

Response Spectrum Analysis



Mesh#3

Critical Element #282 & #330

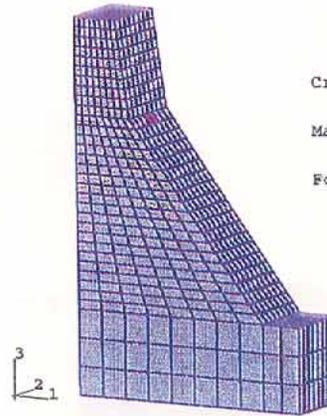
Maximum Principal Stress

For Input Record SHAKEB

143.20 psi

ABAQUS

Response Spectrum Analysis



Mesh#4

Critical Elements #1128 & #1288

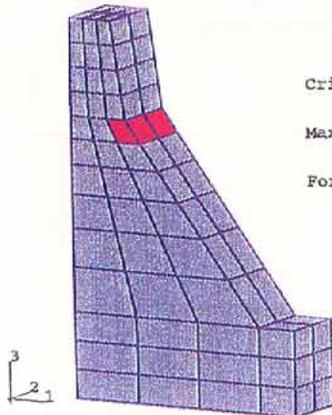
Maximum Principal Stress

For Input Record SHAKEB

168 psi

ABAQUS

Response Spectrum Analysis



Mesh#5

Critical Elements #27 & #45

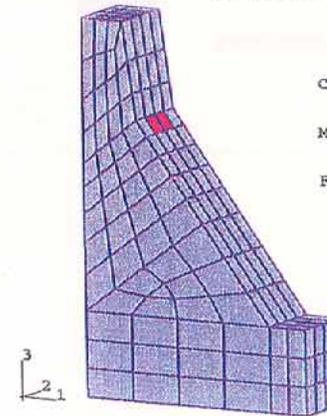
Maximum Principal Stress

For Input Record SHAKEB

88.98 psi

ABAQUS

Response Spectrum Analysis



Mesh#6

Critical Elements #74 & #75

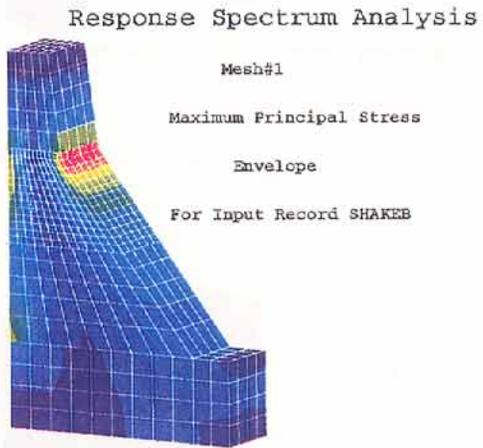
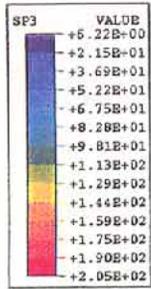
Maximum Principal Stress

For Input Record SHAKEB

88 psi

Figure F10

ABAQUS



ABAQUS

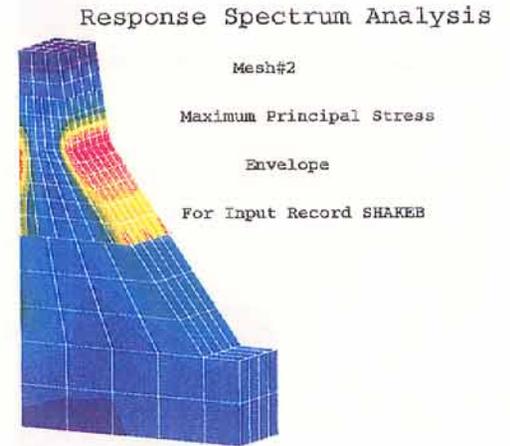
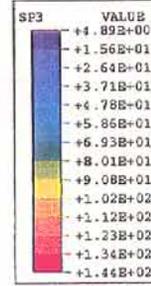
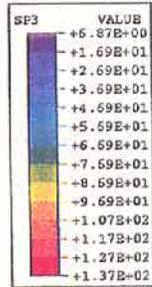
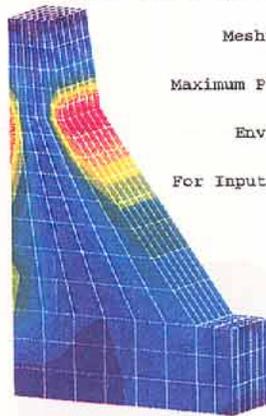


Figure F11

ABAQUS

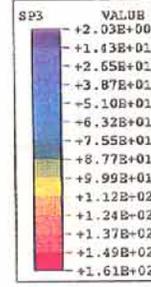


Response Spectrum Analysis

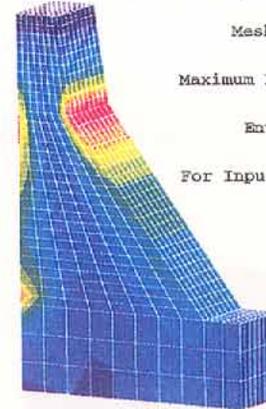


Mesh#3  
Maximum Principal Stress  
Envelope  
For Input Record SHAKEB

ABAQUS

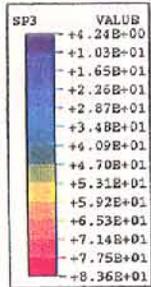


Response Spectrum Analysis

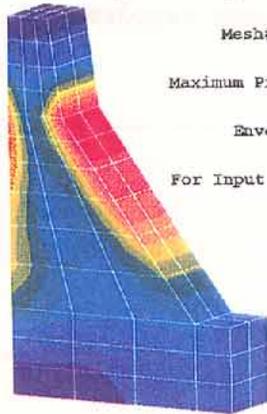


Mesh#4  
Maximum Principal Stress  
Envelope  
For Input Record SHAKEB

ABAQUS

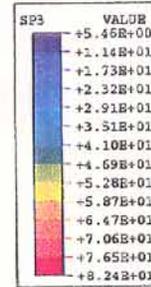


Response Spectrum Analysis

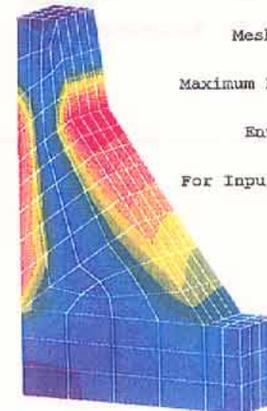


Mesh#5  
Maximum Principal Stress  
Envelope  
For Input Record SHAKEB

ABAQUS



Response Spectrum Analysis



Mesh#6  
Maximum Principal Stress  
Envelope  
For Input Record SHAKEB

Figure F12

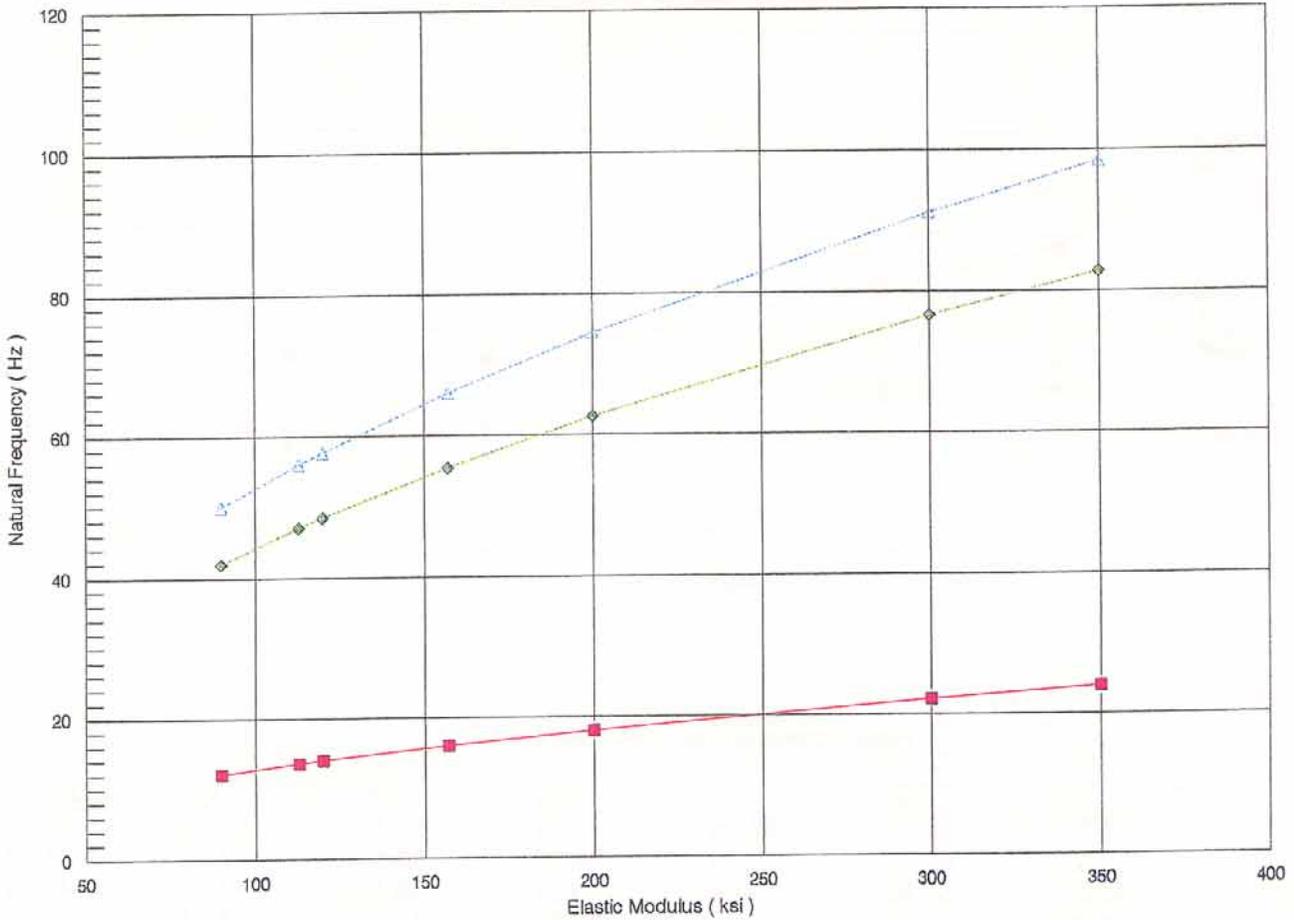
Uncracked Koyna Laboratory Study  
Sensitivity to Variation in Elastic Modulus  
Mesh#3

Material Properties

E = ( 90, 113, 120, 157, 200, 300, 350 ksi )  
Material Density = 138.2 pcf

Damping = 3.5% critical  
Rayleigh Damping Factors  
Alpha = 1.954769; Beta = .000248

**Natural Frequencies**  
Elastic Modulus Varied



Natural Frequencies (Hz)								
Mode	90	113	120	157	200	300	350	LAB
1	12.1	13.6	14.0	16.0	18.0	22.2	23.9	18.0
2	23.2	26.0	26.8	30.6	34.6	42.4	45.7	24.0
3	41.9	47.0	48.4	55.4	62.5	76.6	82.7	30.0
4	49.9	55.9	57.6	65.9	74.4	91.1	98.4	
5	52.1	58.4	60.2	68.8	77.7	95.2	102.8	
6	53.8	60.2	62.1	71.0	80.1	98.1	106.0	
7	57.1	64.0	65.9	75.4	85.1	104.2	112.6	
8	57.8	64.8	66.8	76.4	86.2	105.6	114.0	
9	58.4	65.4	67.4	77.1	87.0	106.6	115.1	
10	59.5	66.7	68.7	78.6	88.7	108.7	117.4	

Figure g1

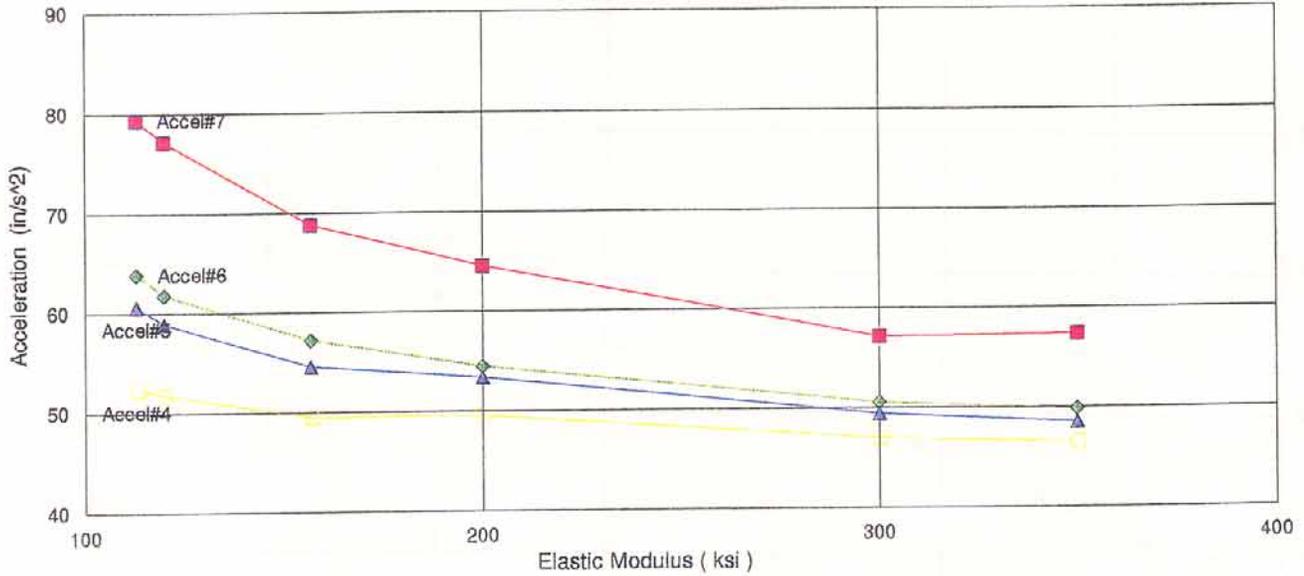
Uncracked Koyna Laboratory Study  
Sensitivity to Variation in Elastic Modulus  
Mesh#3

Material Properties

E = ( 113, 120, 157, 200, 300, 350 ksi )  
Material Density = 138.2 pcf

Damping = 3.5% critical  
Rayleigh Damping Factors  
Alpha = 1.954769; Beta = .000248

**Peak Accelerations**  
Elastic Modulus Varied



Peak Accelerations ( inch / sec ^ 2 )

	113	120	157	200	300	350	LAB
Accel#7	79.31	77.11	68.75	64.53	57.14	57.39	53.26
Accel#6	63.80	61.74	57.19	54.46	50.50	49.85	51.72
Accel#5	60.60	58.90	54.54	53.34	49.42	48.51	49.26
Accel#4	52.28	51.69	49.47	49.50	46.97	46.47	47.72

Figure g2

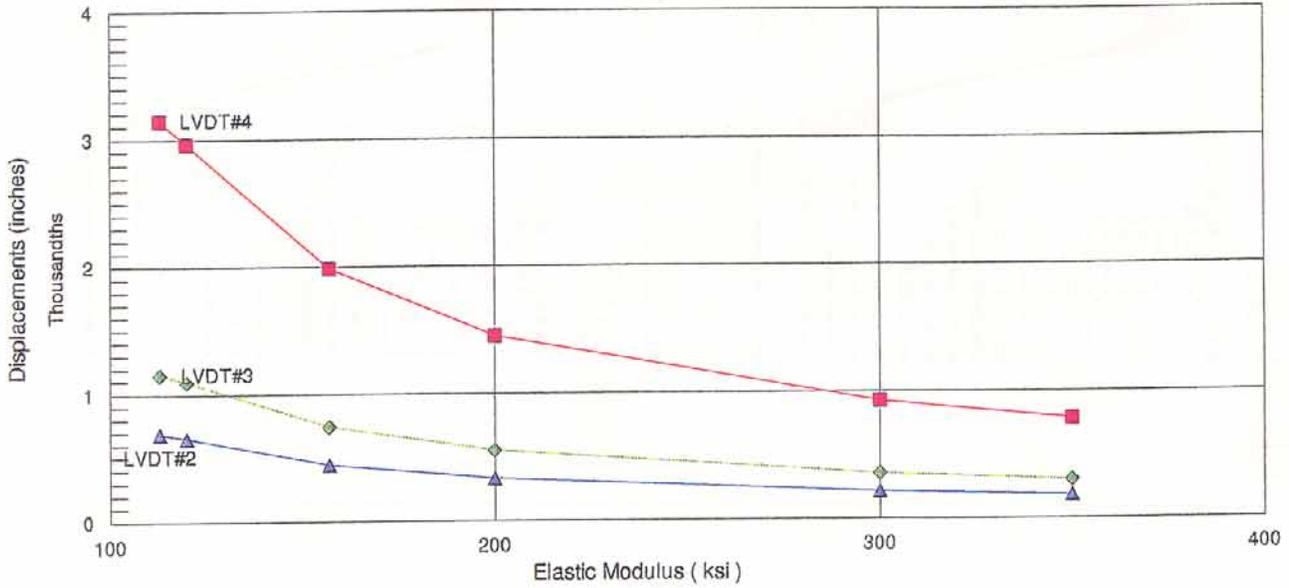
Uncracked Koyna Laboratory Study  
Sensitivity to Variation in Elastic Modulus  
Mesh#3

Material Properties

E = (113, 120, 157, 200, 300, 350 ksi )  
Material Density = 138.2 pcf

Damping = 3.5% critical  
Rayleigh Damping Factors  
Alpha = 1.954769; Beta = .000248

**Peak Displacements**  
Elastic Modulus Varied



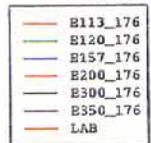
Peak Displacements ( inches )

	113	120	157	200	300	350	LAB
LVDT#4	3.1E-03	3.0E-03	2.0E-03	1.5E-03	9.2E-04	7.8E-04	7.2E-04
LVDT#3	1.2E-03	1.1E-03	7.4E-04	5.5E-04	3.6E-04	3.0E-04	3.1E-04
LVDT#2	6.9E-04	6.5E-04	4.4E-04	3.3E-04	2.2E-04	1.8E-04	2.1E-04

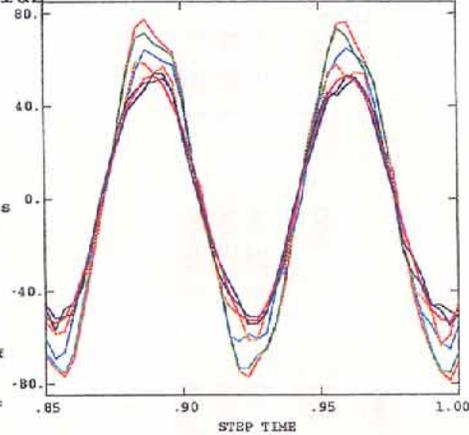
Figure g3

# ABAQUS

Elastic Modulus Varied



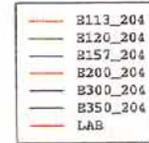
Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model  
Acceleration  
at ACCEL#7  
Modal Damping, 3.5%  
Material Density = 138 pcf  
Filename:SHAKEA  
Total Time = 279.75 to 280 sec



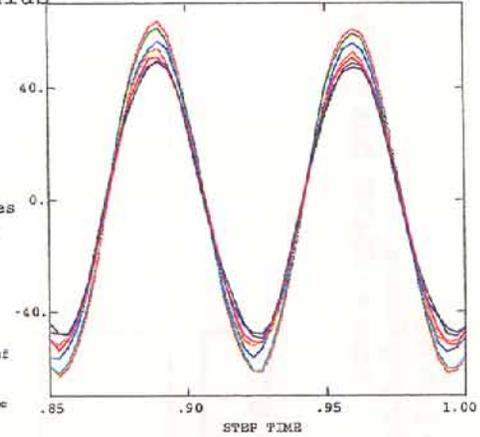
ABAQUS Modal Dynamic Analyses (E113 to E300) vs Laboratory Measurements (LAB)

# ABAQUS

Elastic Modulus Varied



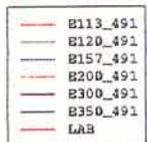
Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model  
Acceleration  
at ACCEL#6  
Modal Damping, 3.5%  
Material Density = 138 pcf  
Filename:SHAKEA  
Total Time = 279.75 to 280 sec



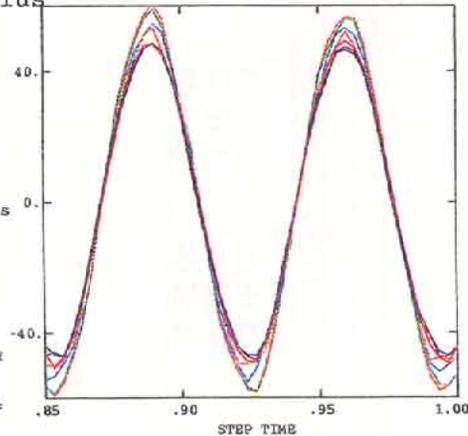
ABAQUS Modal Dynamic Analyses (E113 to E350) vs Laboratory Measurements (LAB)

# ABAQUS

Elastic Modulus Varied



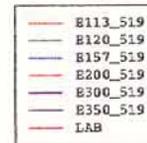
Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model  
Acceleration  
at ACCEL#5  
Modal Damping, 3.5%  
Material Density = 138 pcf  
Filename:SHAKEA  
Total Time = 279.75 to 280 sec



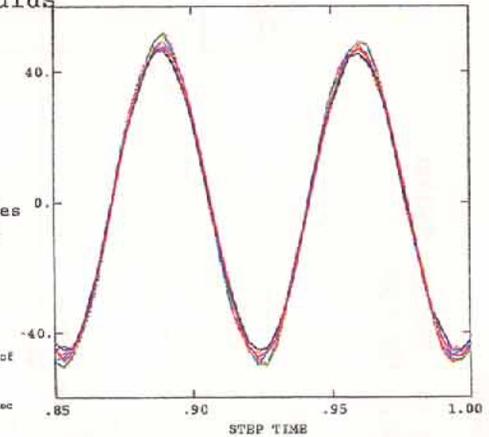
ABAQUS Modal Dynamic Analyses (E113 to E350) vs Laboratory Measurements (LAB)

# ABAQUS

Elastic Modulus Varied



Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model  
Acceleration  
at ACCEL#4  
Modal Damping, 3.5%  
Material Density = 138 pcf  
Filename:SHAKEA  
Total Time = 279.75 to 280 sec



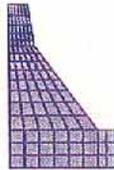
ABAQUS Modal Dynamic Analyses (E113 to E350) vs Laboratory Measurements (LAB)

# ABAQUS

Koyna Laboratory Model Study  
 Uncracked Model Study  
 Sensitivity Study  
 Variation of Elastic Modulus

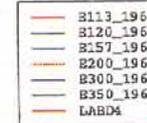
Comparison of Displacements  
 ABAQUS STANDARD  
 Modal Dynamic Analysis

Input Record SHAKEA  
 Modal Damping, 3.5%  
 Density = 138.2 pcf  
 Mesh # 3

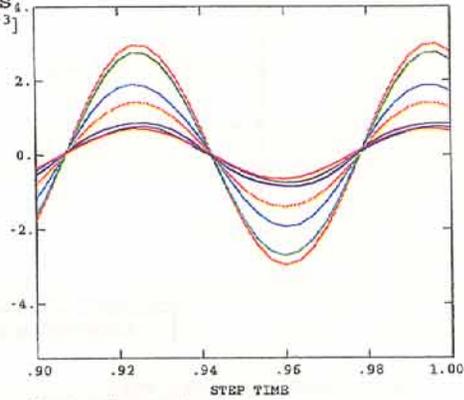


# ABAQUS

Elastic Modulus<sub>4</sub>  
 [ $\times 10^{-3}$ ]



Linear Elastic  
 Material Properties  
 STANDARD Analyses  
 Uncracked Model  
 Displacement  
 at LVDT#4

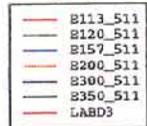


Total Time = 279.70 to 280 sec

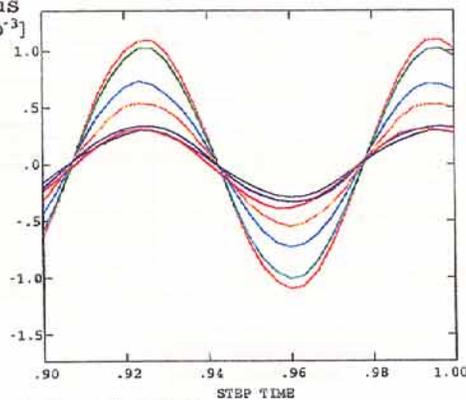
ABAQUS Modal Dynamic Analyses & Laboratory Measurements

# ABAQUS

Elastic Modulus  
 [ $\times 10^{-3}$ ]



Linear Elastic  
 Material Properties  
 STANDARD Analyses  
 Uncracked Model  
 Displacement  
 at LVDT#3

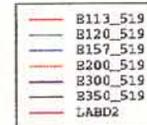


Total Time = 279.50 to 280 sec

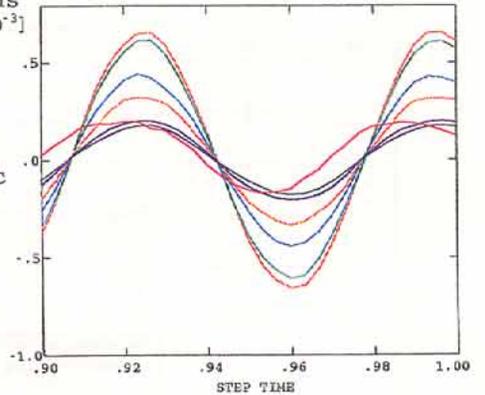
ABAQUS Modal Dynamic Analyses & Laboratory Measurements

# ABAQUS

Elastic Modulus  
 [ $\times 10^{-3}$ ]



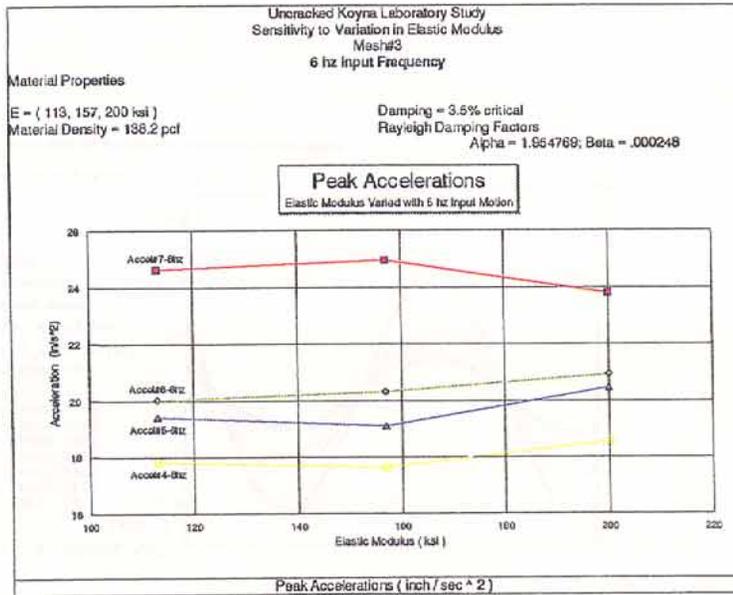
Linear Elastic  
 Material Properties  
 STANDARD Analyses  
 Uncracked Model  
 Acceleration  
 at LVDT#2



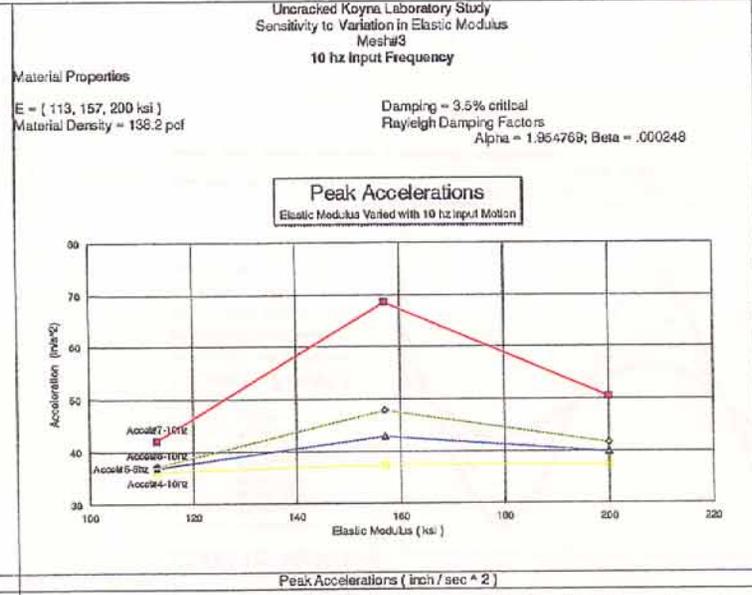
Total Time = 279.50 to 280 sec

ABAQUS Modal Dynamic Analyses & Laboratory Measurements

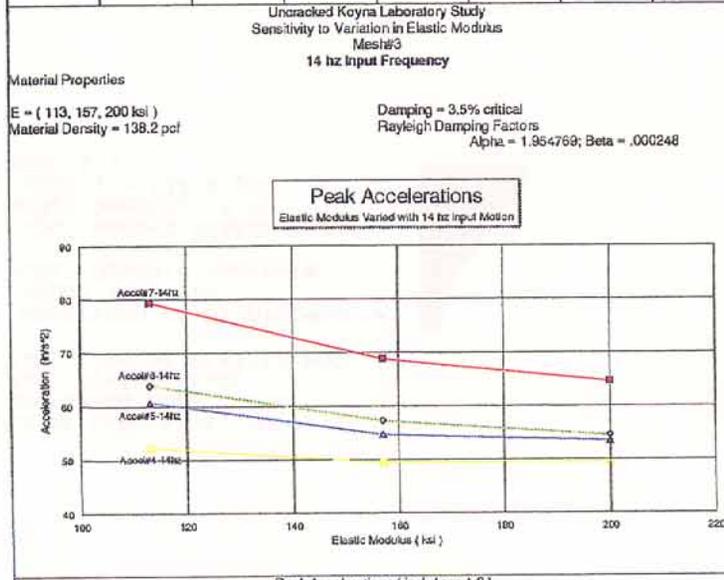
Figure 95



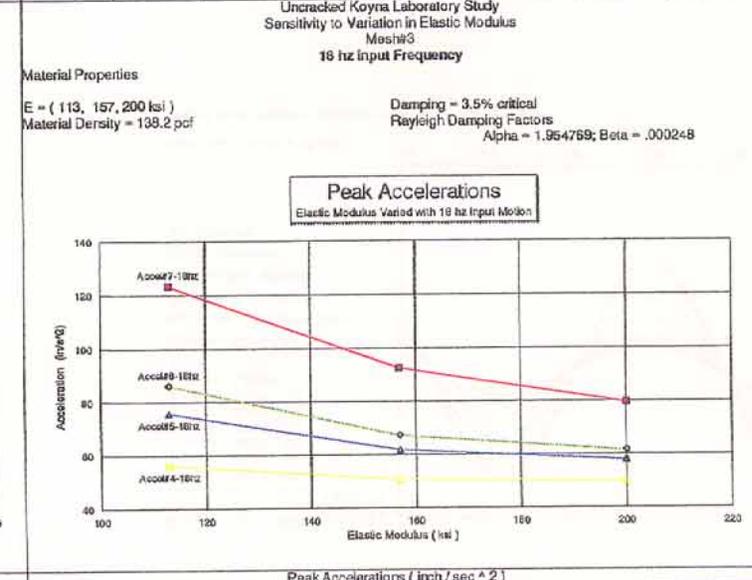
10 Hz Input Motion	113	157	200	Lab	10 Hz
Accel#7-6Hz	24.62	24.96	23.79	Accel#7-6Hz	17.55
Accel#6-6Hz	20.02	20.31	20.93	Accel#6-6Hz	17.86
Accel#5-6Hz	19.40	19.09	20.45	Accel#5-6Hz	16.93
Accel#4-6Hz	17.84	17.65	18.56	Accel#4-6Hz	17.24



10 Hz Input Motion	113	157	200	Lab	10 Hz
Accel#7-10Hz	42.15	68.45	50.39	Accel#7-10Hz	37.87
Accel#6-10Hz	37.18	47.84	41.61	Accel#6-10Hz	36.94
Accel#5-10Hz	36.79	42.87	39.70	Accel#5-10Hz	36.4
Accel#4-10Hz	36.27	37.47	37.50	Accel#4-10Hz	36.02

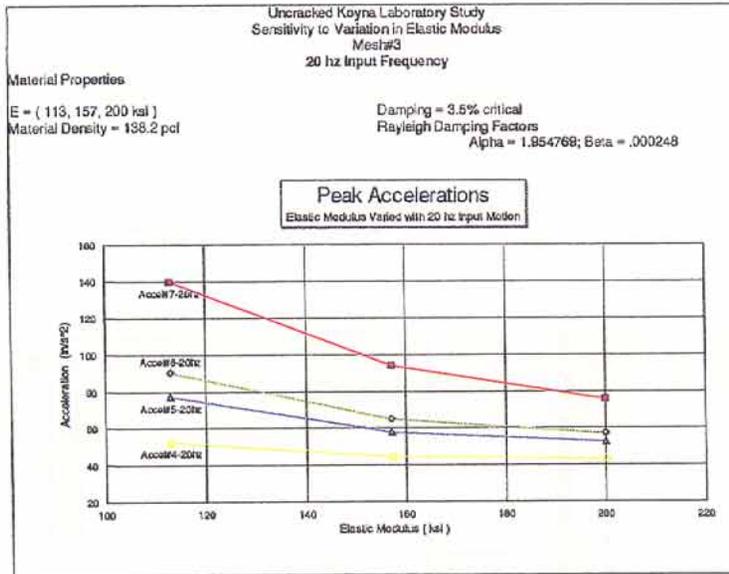


14 Hz Input Motion	113	157	200	Lab	14 Hz
Accel#7-14Hz	79.31	68.75	64.53	Accel#7-14Hz	53.26
Accel#6-14Hz	63.80	57.19	54.46	Accel#6-14Hz	50.72
Accel#5-14Hz	60.60	54.54	53.34	Accel#5-14Hz	49.26
Accel#4-14Hz	52.28	49.47	49.5	Accel#4-14Hz	47.72



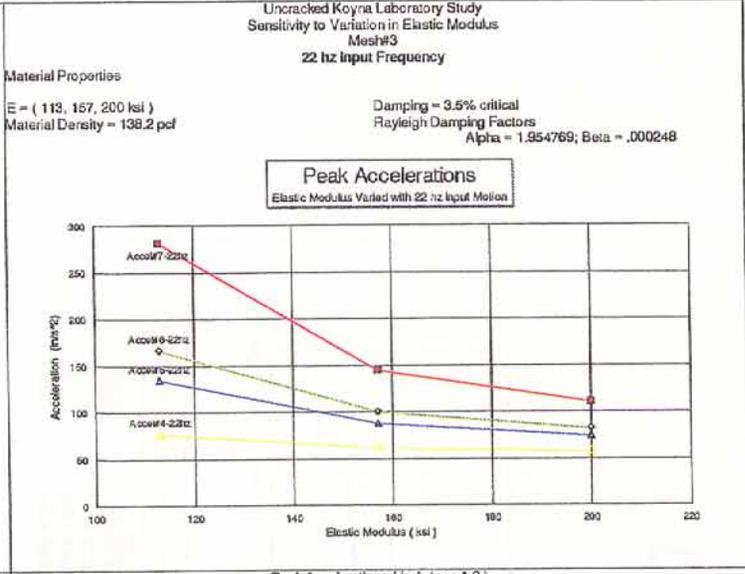
18 Hz Input Motion	113	157	200	Lab	18 Hz
Accel#7-18Hz	123.2	92.43	78.49	Accel#7-18Hz	28.94
Accel#6-18Hz	85.88	67.23	61.48	Accel#6-18Hz	32.62
Accel#5-18Hz	75.55	61.65	57.8	Accel#5-18Hz	35.71
Accel#4-18Hz	56.15	50.82	49.95	Accel#4-18Hz	40.02

Figure 96



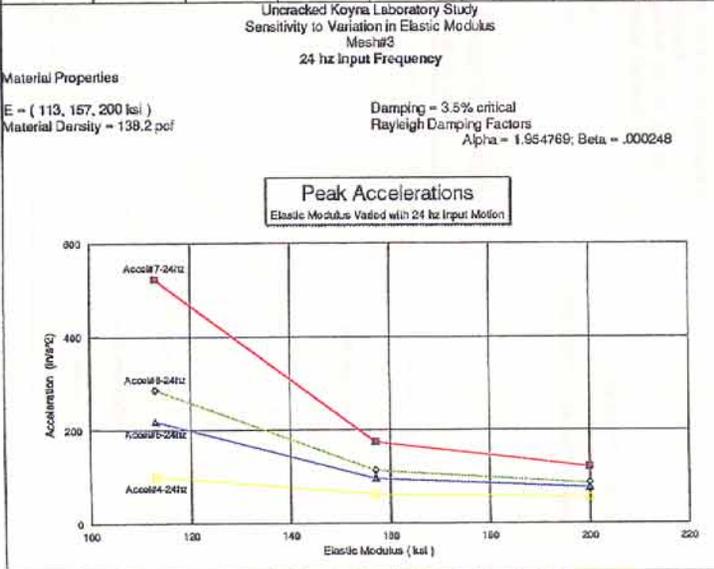
Peak Accelerations ( inch / sec ^ 2 )

20 hz Input Motion	113	157	200	Lab	20 hz
Accel#7-20hz	139.80	94.03	75.55	Accel#7-20hz	85.26
Accel#6-20hz	90.25	65.09	57.14	Accel#6-20hz	57.57
Accel#5-20hz	77.07	57.65	52.66	Accel#5-20hz	51.1
Accel#4-20hz	52.48	44.84	43.31	Accel#4-20hz	44.84



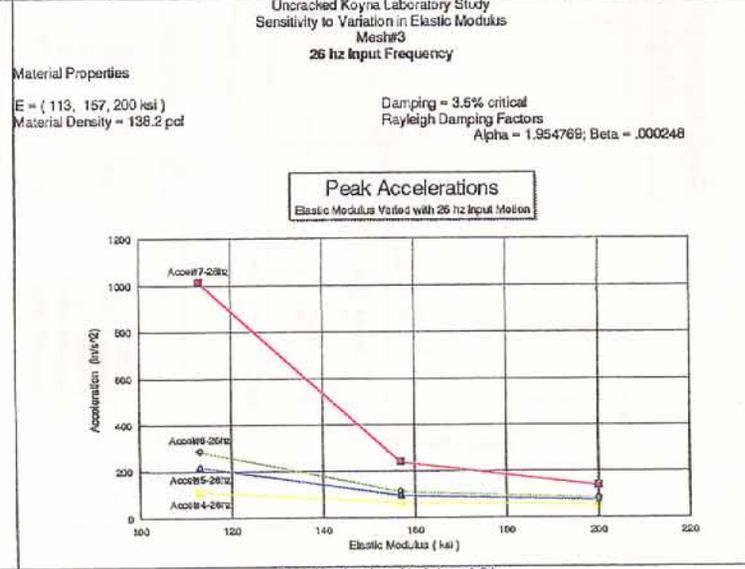
Peak Accelerations ( inch / sec ^ 2 )

22 hz Input Motion	113	157	200	Lab	22 hz
Accel#7-22hz	281.60	144.20	110.20	Accel#7-22hz	65.57
Accel#6-22hz	166.30	100.10	82.04	Accel#6-22hz	60.03
Accel#5-22hz	134.40	87.09	73.59	Accel#5-22hz	55.72
Accel#4-22hz	77.24	61.90	57.66	Accel#4-22hz	52.33



Peak Accelerations ( inch / sec ^ 2 )

24 hz Input Motion	113	157	200	Lab	24 hz
Accel#7-24hz	523.00	174.50	121.4	Accel#7-24hz	97.59
Accel#6-24hz	285.00	112.60	85.59	Accel#6-24hz	79.42
Accel#5-24hz	217.00	95.42	75.81	Accel#5-24hz	68.96
Accel#4-24hz	100.50	62.95	56.31	Accel#4-24hz	57.88



Peak Accelerations ( inch / sec ^ 2 )

26 hz Input Motion	113	157	200	Lab	26 hz
Accel#7-26hz	1013	238.6	137.9	Accel#7-26hz	97.59
Accel#6-26hz	285.3	112.6	85.59	Accel#6-26hz	79.42
Accel#5-26hz	217.9	95.42	75.81	Accel#5-26hz	68.96
Accel#4-26hz	111.4	65.02	54.3	Accel#4-26hz	57.88

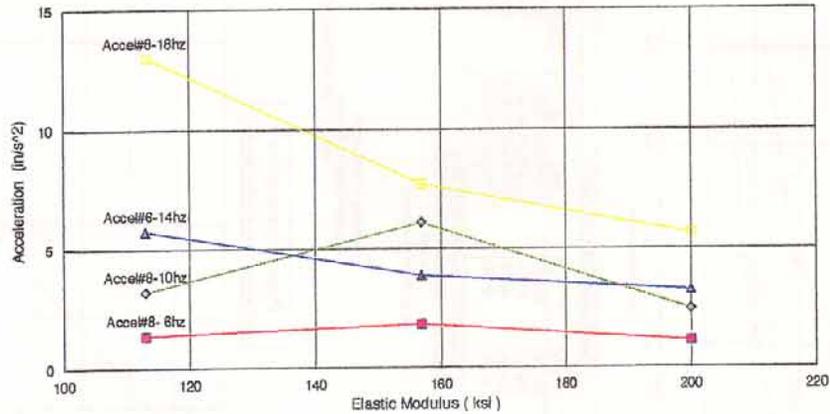
Figure 97

Uncracked Koyna Laboratory Study  
Sensitivity to Variation in Elastic Modulus  
Mesh#3  
6, 10, 14, 18 hz Input Frequency  
Vertical Accelerations

Material Properties  
E = ( 113, 157, 200 ksi )  
Material Density = 138.2 pcf

Damping = 3.5% critical  
Rayleigh Damping Factors  
Alpha = 1.954769; Beta = .000248

Peak Vertical Accelerations  
6, 10, 14, 18 hz Input Motions



Peak Accelerations ( inch / sec ^ 2 )

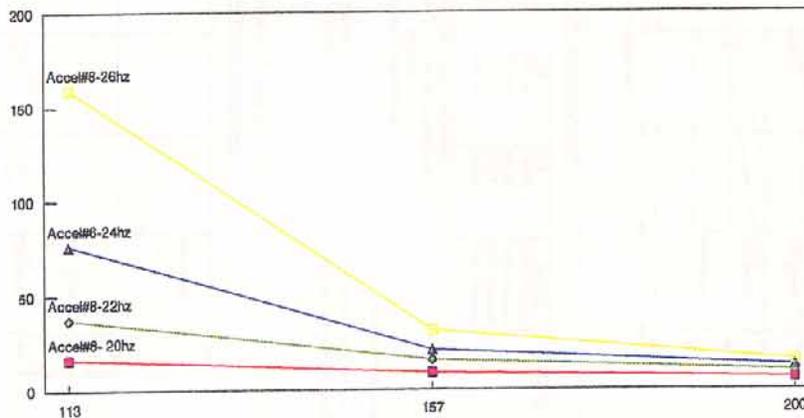
Motion	113	157	200	Lab	
Accel#8- 6hz	1.356	1.791	1.096	Accel#8-6hz	3.694
Accel#8- 10hz	3.18	6.07	2.45	Accel#8-10hz	6.773
Accel#6- 14hz	5.73	3.87	3.23	Accel#6-14hz	11.08
Accel#8- 18hz	12.97	7.66	5.82	Accel#8-18hz	76.96

Uncracked Koyna Laboratory Study  
Sensitivity to Variation in Elastic Modulus  
Mesh#3  
20, 22, 24, 26 hz Input Frequency  
Vertical Accelerations

Material Properties  
E = ( 113, 157, 200 ksi )  
Material Density = 138.2 pcf

Damping = 3.5% critical  
Rayleigh Damping Factors  
Alpha = 1.954769; Beta = .000248

Peak Vertical Accelerations  
20, 22, 24, 26 hz Input Motions



Peak Accelerations ( inch / sec ^ 2 )

Motion	113	157	200	Lab	
Accel#8- 20hz	16.38	8.579	5.977	Accel#8-6hz	33.86
Accel#8- 22hz	37.06	15.86	10.00	Accel#8-10hz	18.47
Accel#6- 24hz	76.13	21.01	12.52	Accel#6-14hz	18.78
Accel#8- 26hz	158.70	31.27	15.83	Accel#8-18hz	10.78

Figure g8

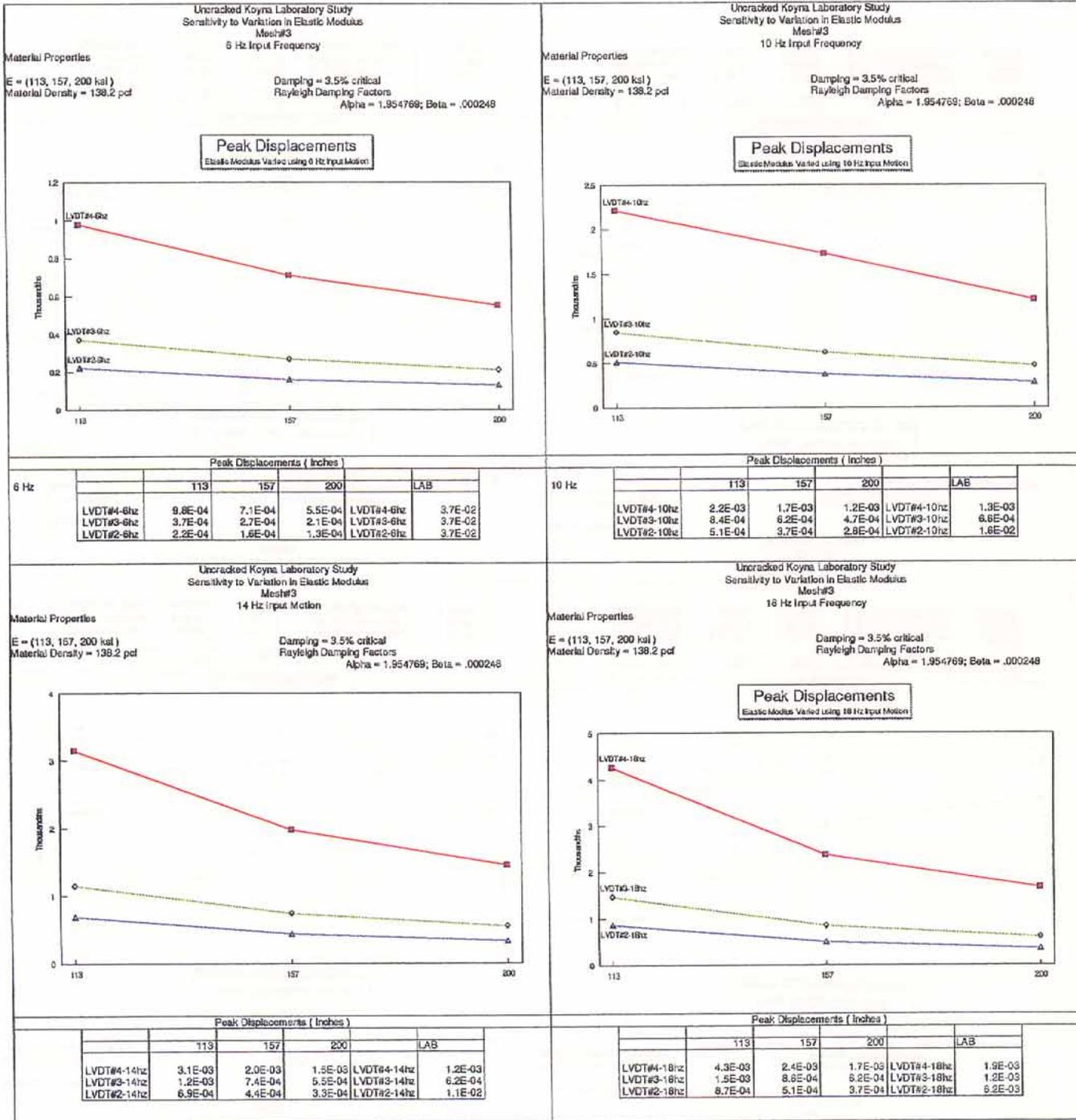
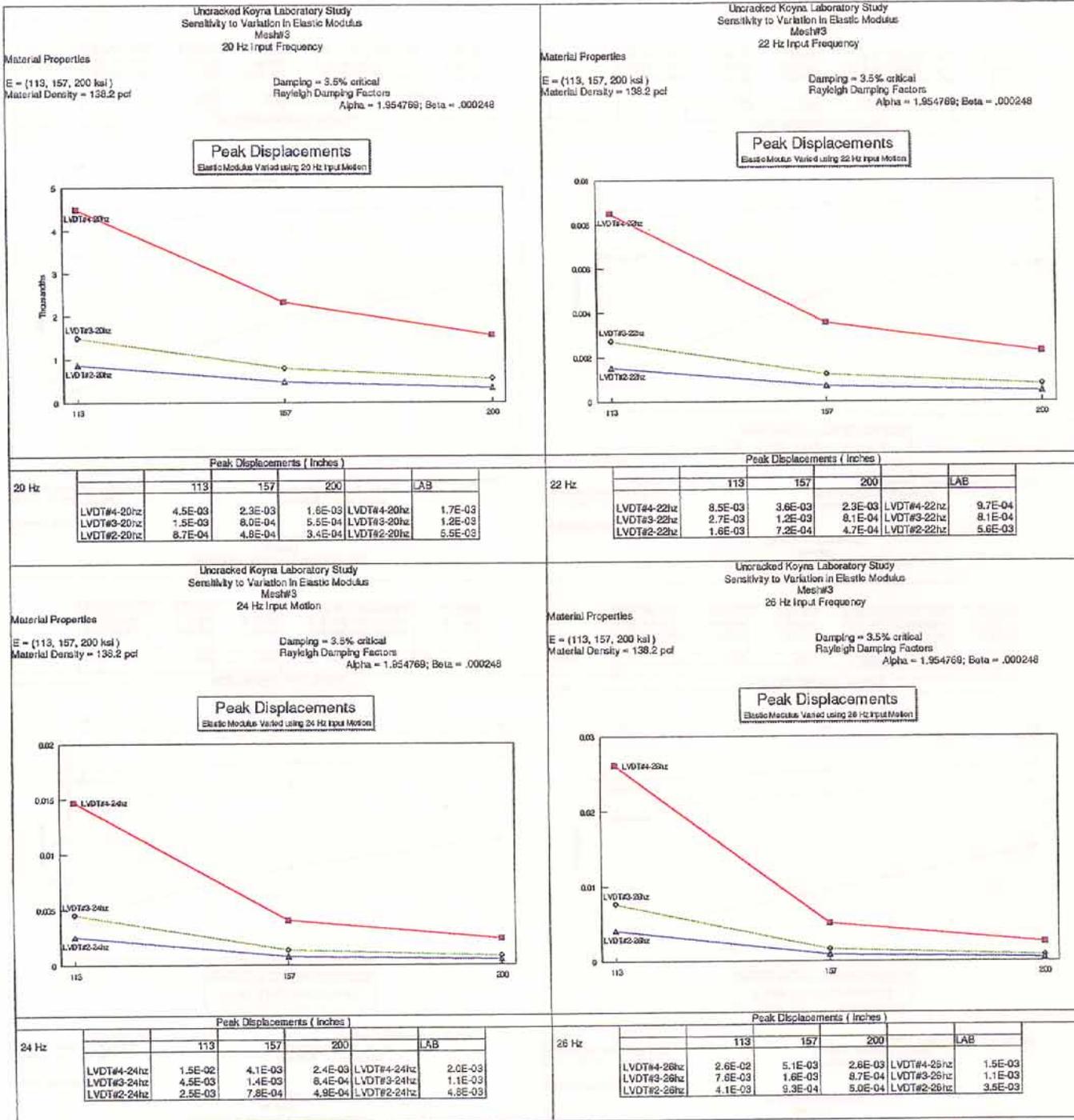
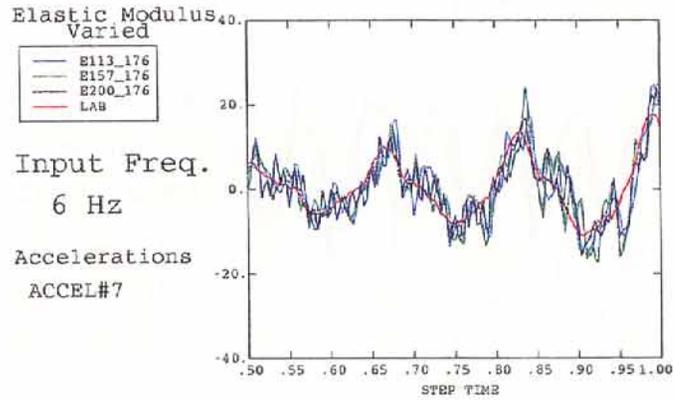


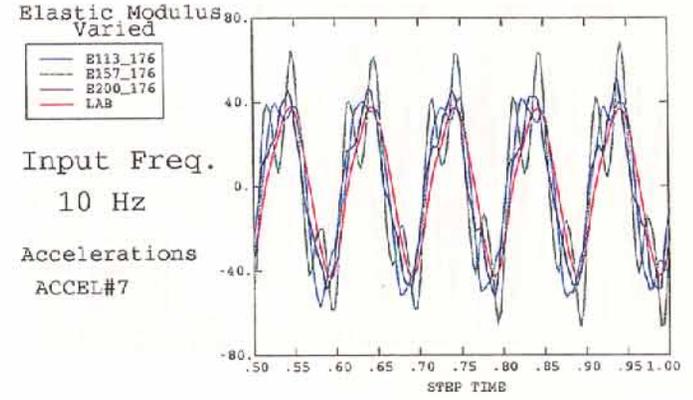
Figure g10



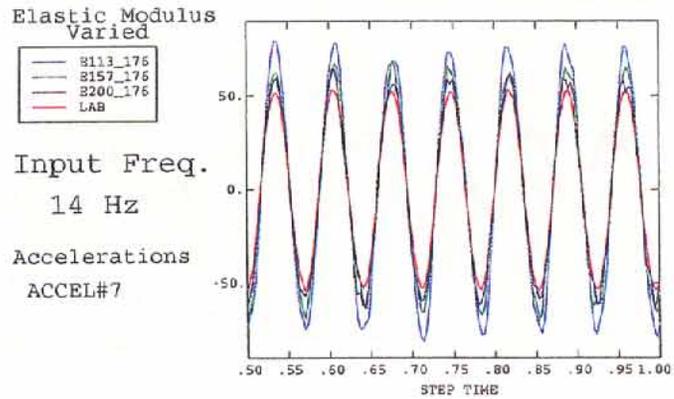
# ABAQUS



# ABAQUS



# ABAQUS



# ABAQUS

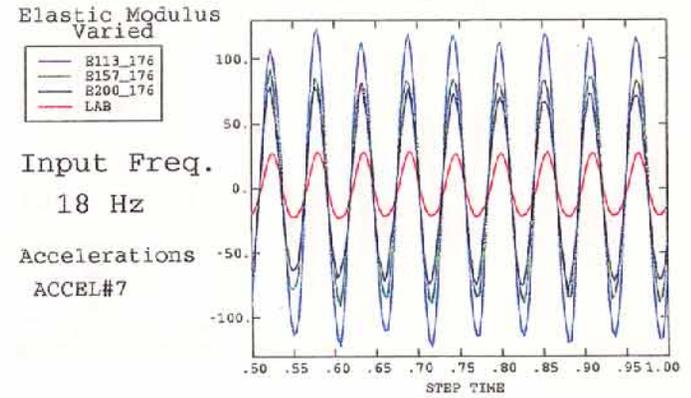
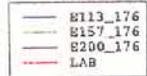


Figure g11

# ABAQUS

Elastic Modulus Varied [ $\times 10^3$ ]

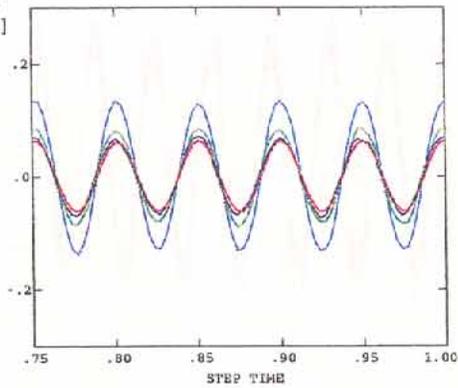


Input Freq.

20 Hz

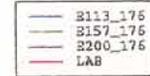
Accelerations

ACCEL#7



# ABAQUS

Elastic Modulus Varied [ $\times 10^3$ ]

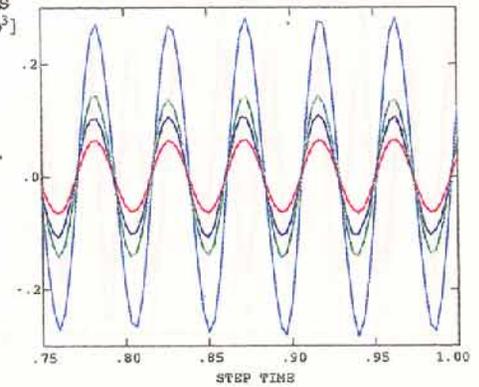


Input Freq.

22 Hz

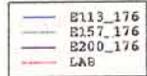
Accelerations

ACCEL#7



# ABAQUS

Elastic Modulus Varied [ $\times 10^3$ ]

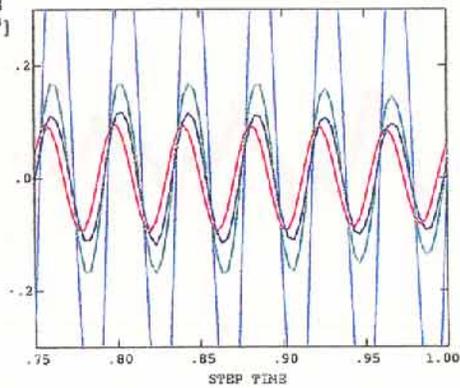


Input Freq.

24 Hz

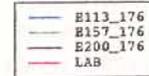
Accelerations

ACCEL#7



# ABAQUS

Elastic Modulus Varied [ $\times 10^3$ ]



Input Freq.

26 Hz

Accelerations

ACCEL#7

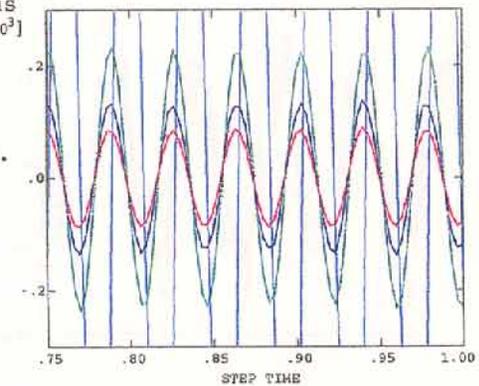
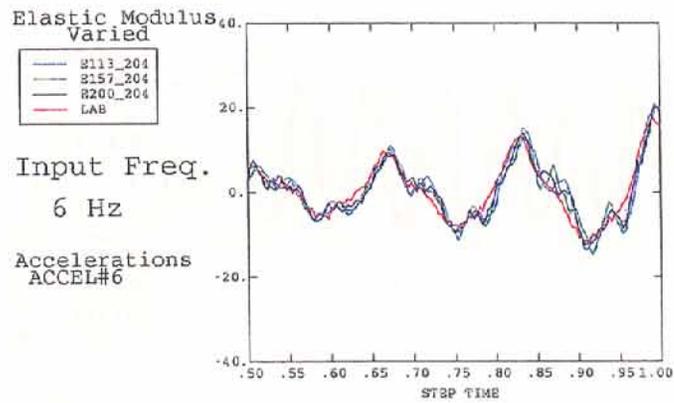
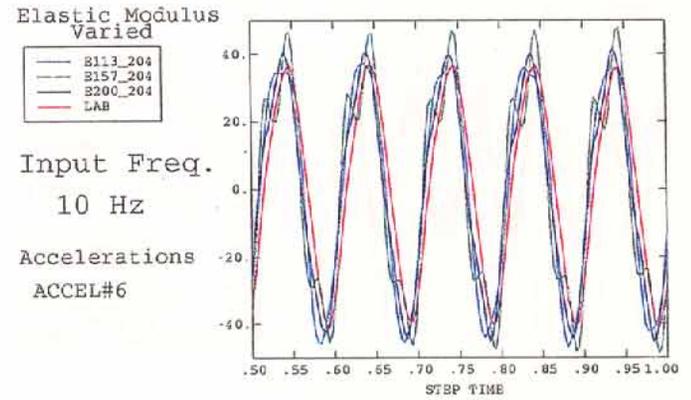


Figure g12

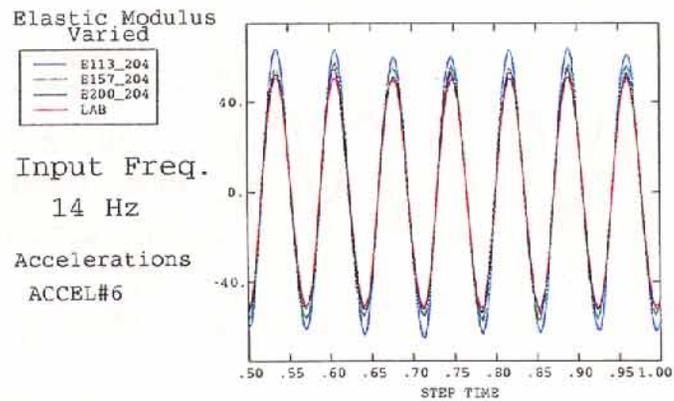
# ABAQUS



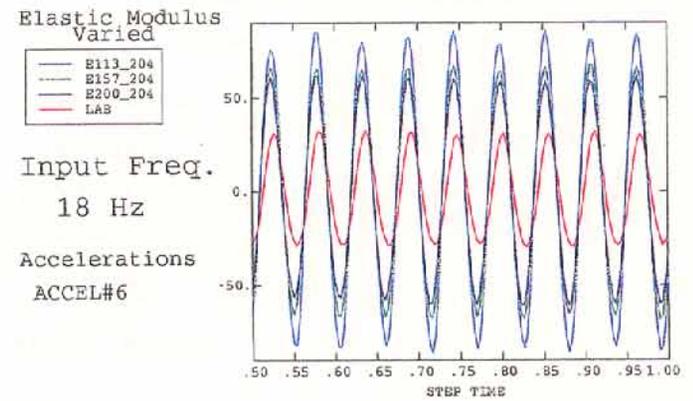
# ABAQUS



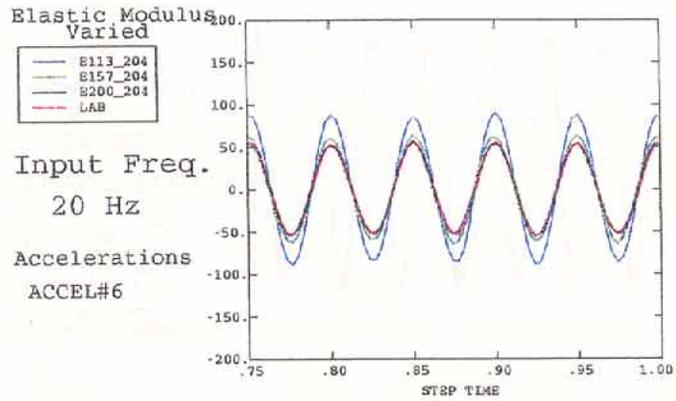
# ABAQUS



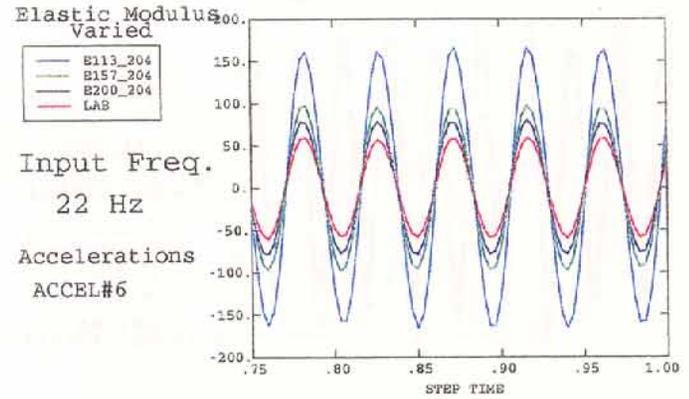
# ABAQUS



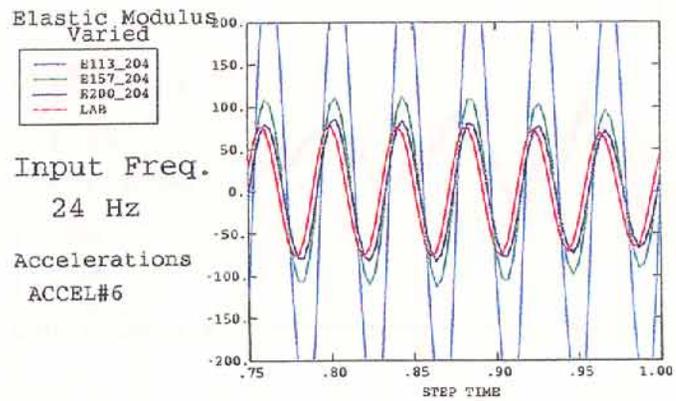
# ABAQUS



# ABAQUS



# ABAQUS



# ABAQUS

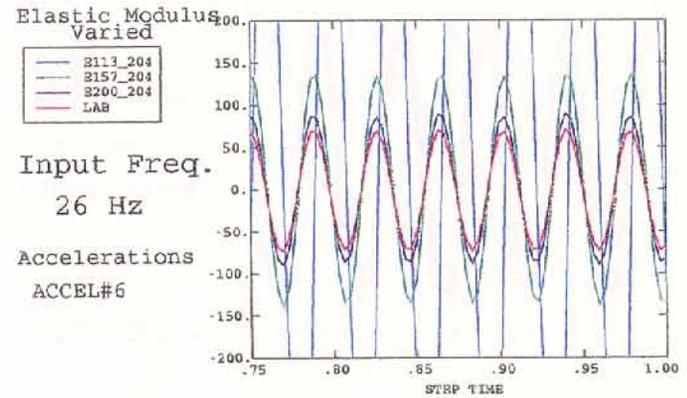
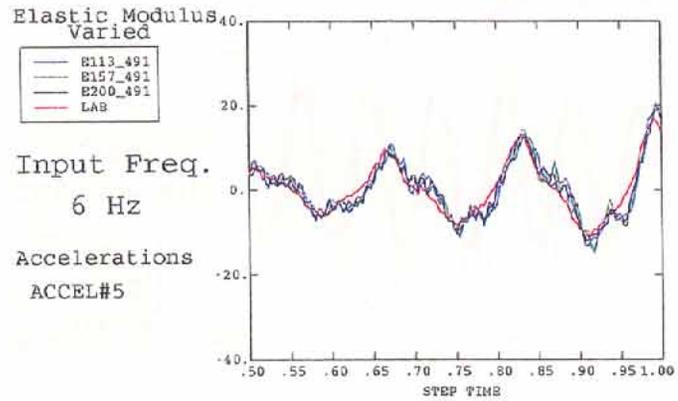
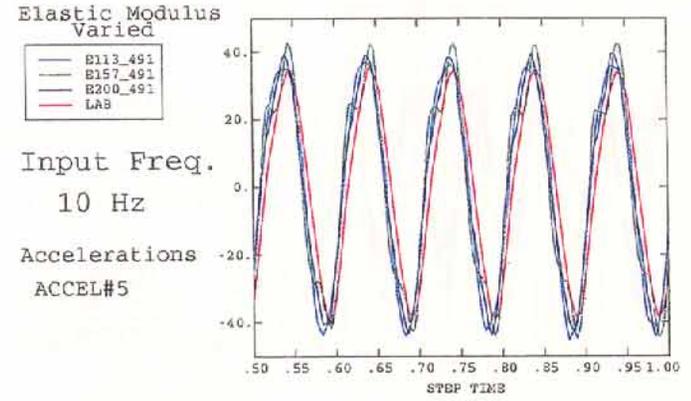


Figure g14

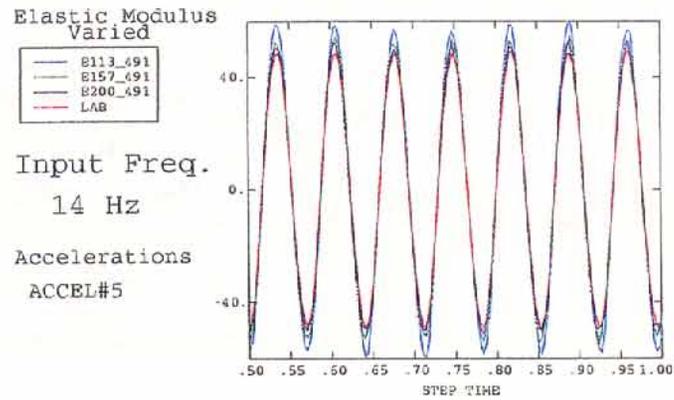
# ABAQUS



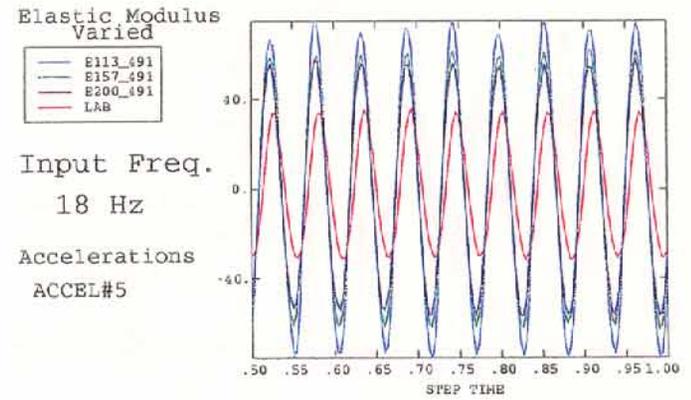
# ABAQUS



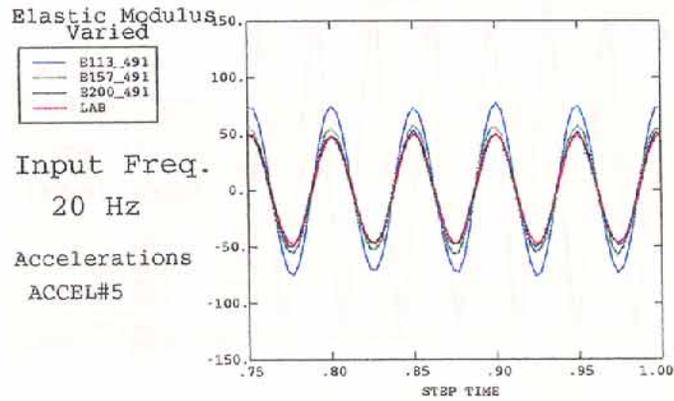
# ABAQUS



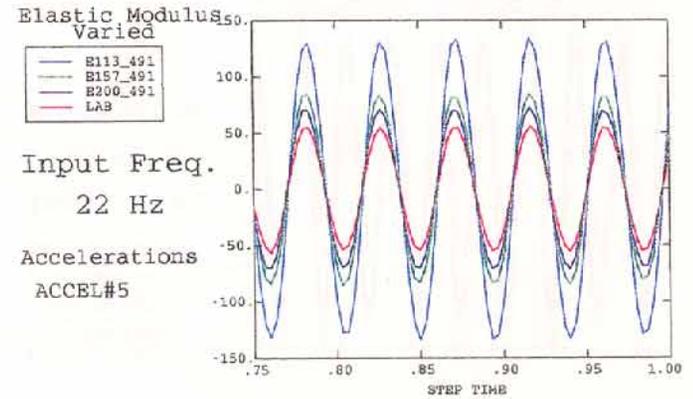
# ABAQUS



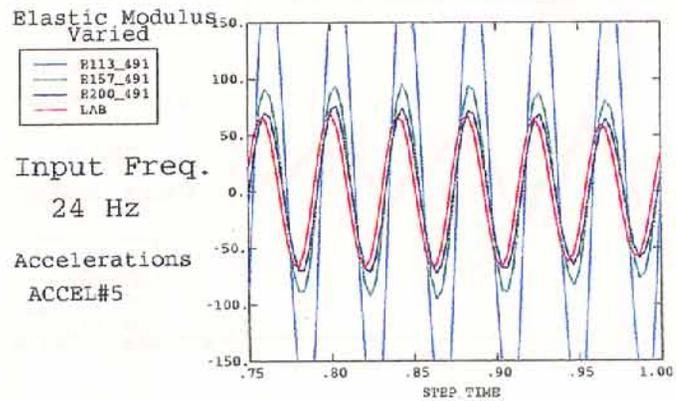
# ABAQUS



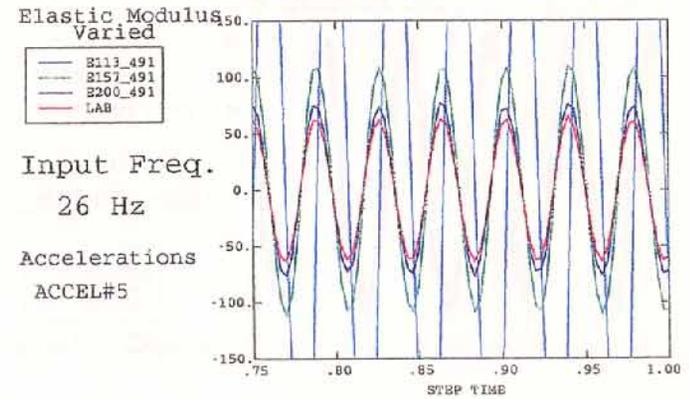
# ABAQUS



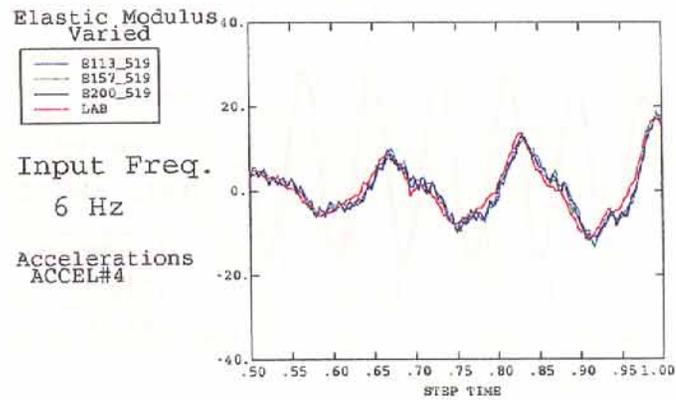
# ABAQUS



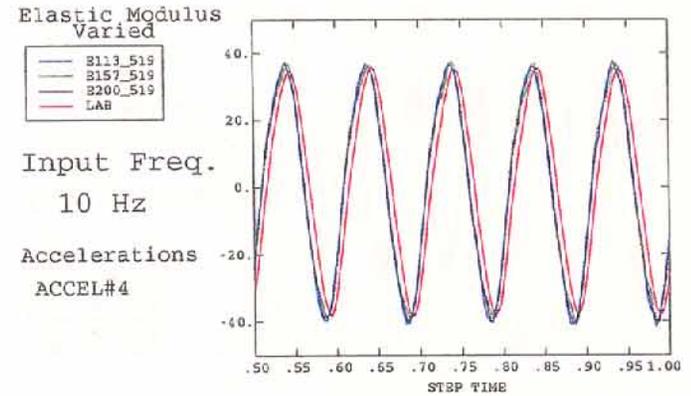
# ABAQUS



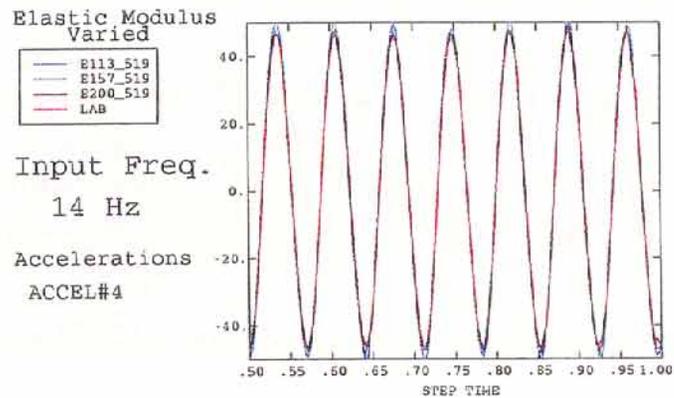
# ABAQUS



# ABAQUS



# ABAQUS



# ABAQUS

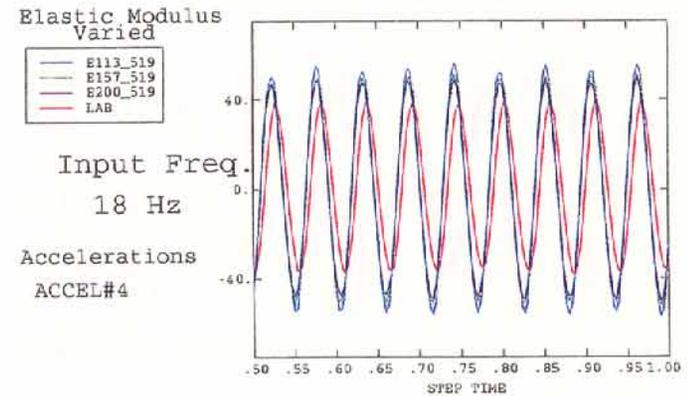
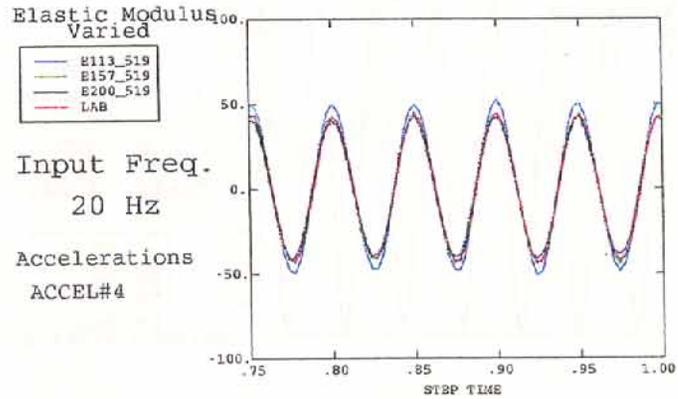
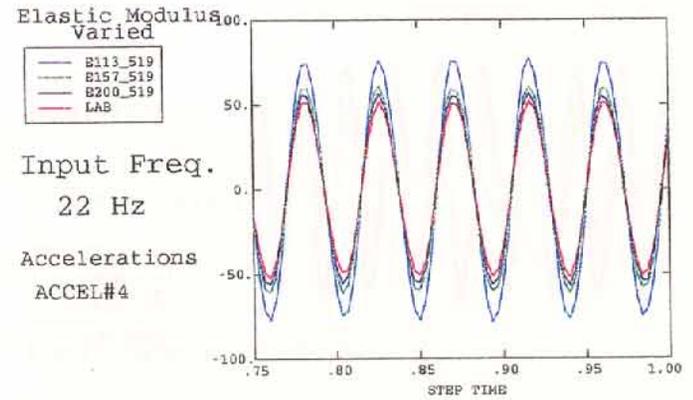


Figure g17

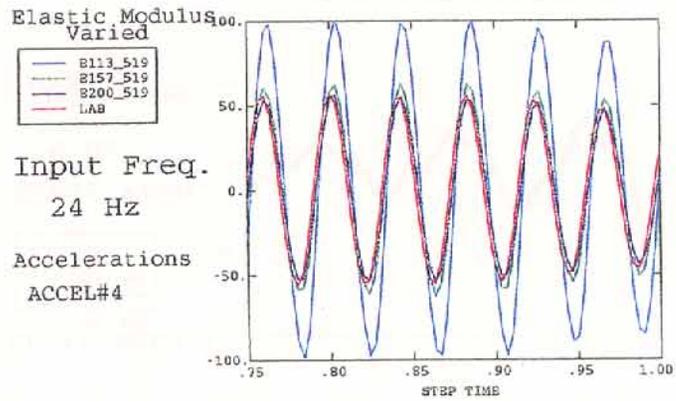
# ABAQUS



# ABAQUS



# ABAQUS



# ABAQUS

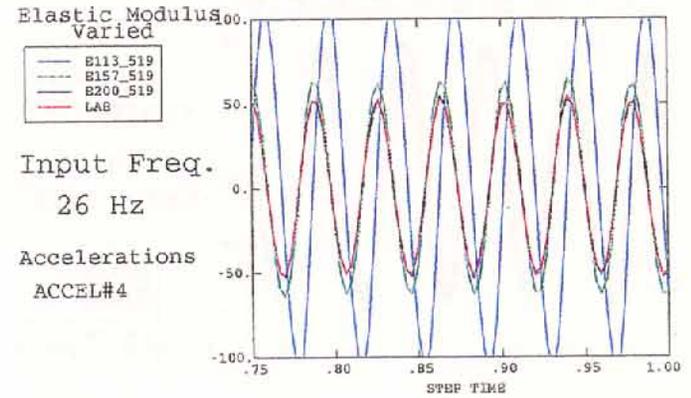
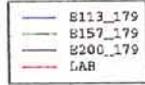


Figure g18

# ABAQUS

Elastic Modulus Varied

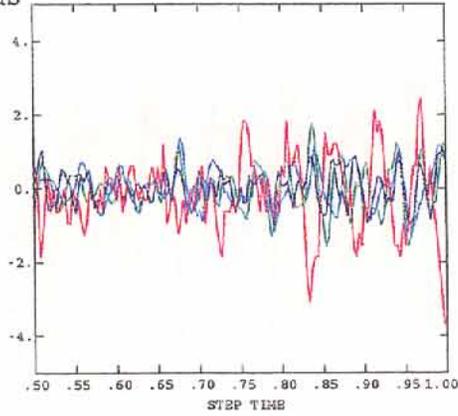


Input Freq.

6 Hz

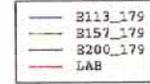
Accelerations

ACCEL#8



# ABAQUS

Elastic Modulus Varied

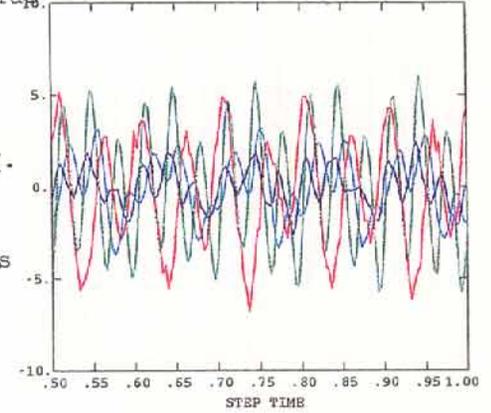


Input Freq.

10 Hz

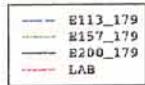
Accelerations

ACCEL#8



# ABAQUS

Elastic Modulus Varied

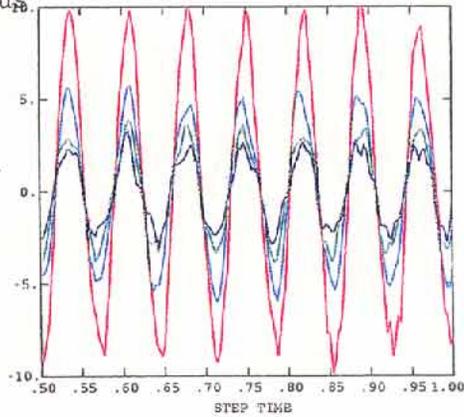


Input Freq.

14 Hz

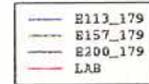
Accelerations

ACCEL#8



# ABAQUS

Elastic Modulus Varied

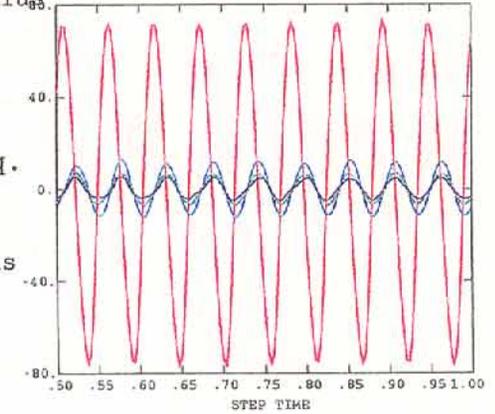


Input Freq.

18 Hz

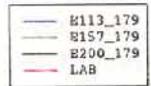
Accelerations

ACCEL#8



# ABAQUS

Elastic Modulus Varied

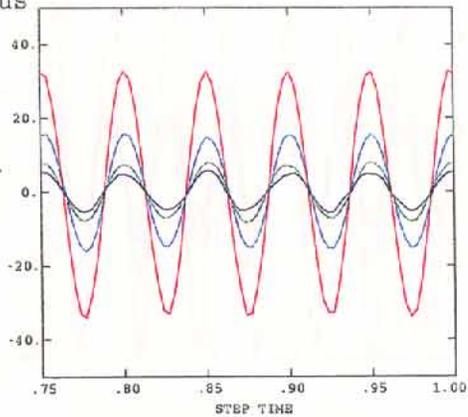


Input Freq.

20 Hz

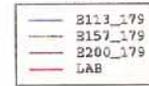
Accelerations

ACCEL#8



# ABAQUS

Elastic Modulus Varied

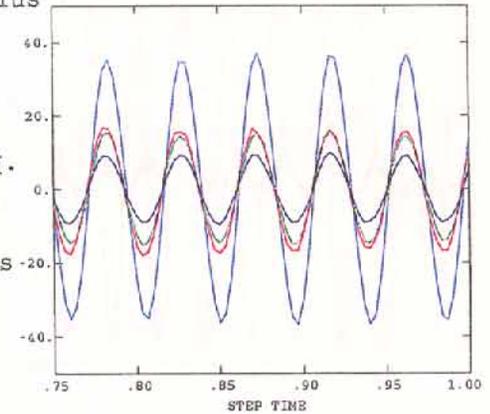


Input Freq.

22 Hz

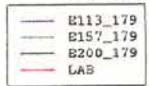
Accelerations

ACCEL#8



# ABAQUS

Elastic Modulus Varied

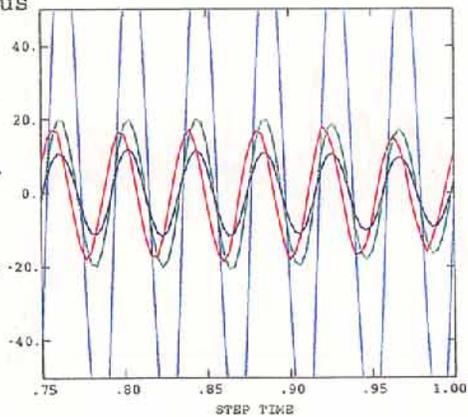


Input Freq.

24 Hz

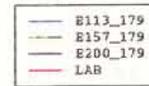
Accelerations

ACCEL#8



# ABAQUS

Elastic Modulus Varied



Input Freq.

26 Hz

Accelerations

ACCEL#8

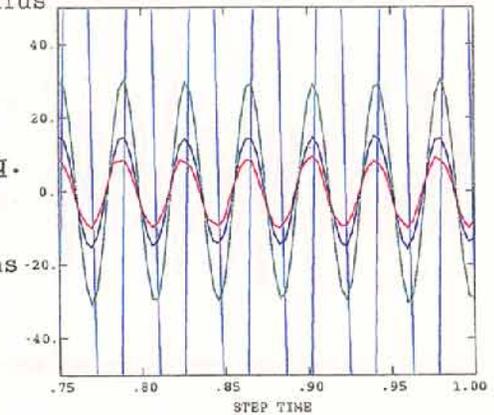


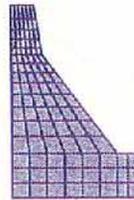
Figure g20

# ABAQUS

Koyna Laboratory Model Study  
 Uncracked Model Study  
 Sensitivity Study  
 Variation of Elastic Modulus

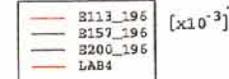
At Diff. Input Frequencies  
 Comparison of Displacements  
 Dynamic Analysis

Input Record SHAKEA  
 Mesh # 3



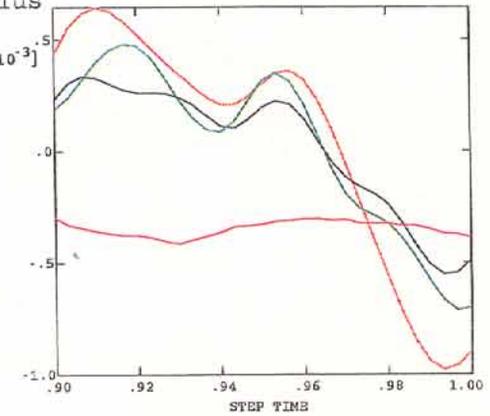
# ABAQUS

Elastic Modulus  
 Varied



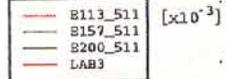
Input Freq.  
 6 hz

Displacement  
 at LVDT#4



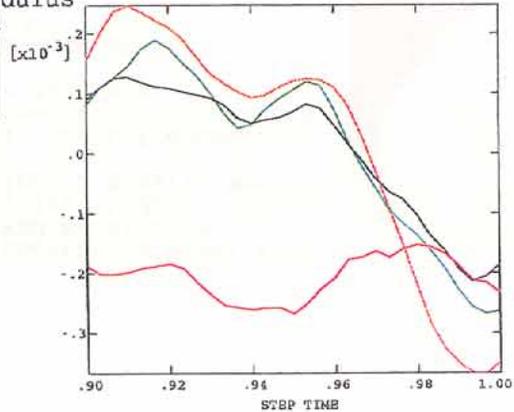
# ABAQUS

Elastic Modulus  
 Varied



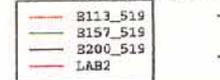
Input Freq.  
 6 hz

Displacement  
 at LVDT#3



# ABAQUS

Elastic Modulus  
 Varied



Input Freq.  
 6 hz

Displacement  
 at LVDT#2

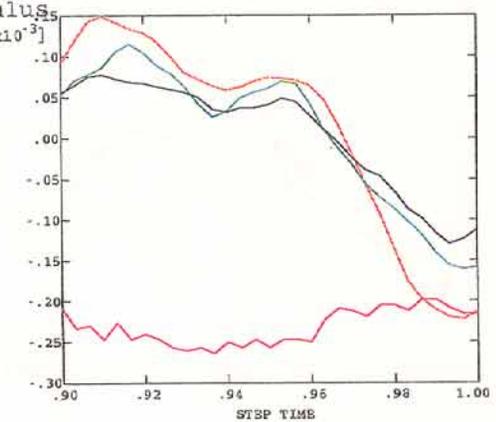


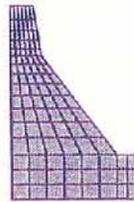
Figure g21

# ABAQUS

Koyna Laboratory Model Study  
Uncracked Model Study  
Sensitivity Study  
Variation of Elastic Modulus

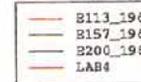
At Diff. Input Frequencies  
Comparison of Displacements  
Dynamic Analysis

Input Record SHAKEA  
Mesh # 3



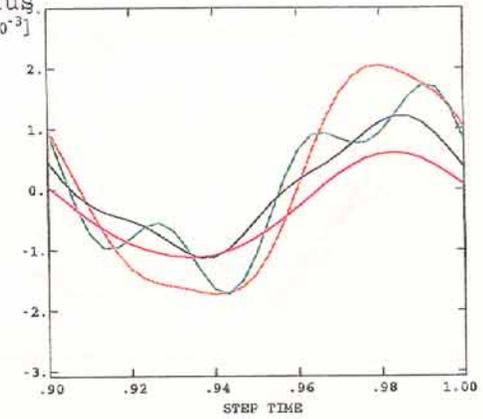
# ABAQUS

Elastic Modulus  
Varied [ $\times 10^{-3}$ ]



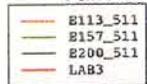
Input Freq.  
10 hz

Displacement  
at LVDT#4



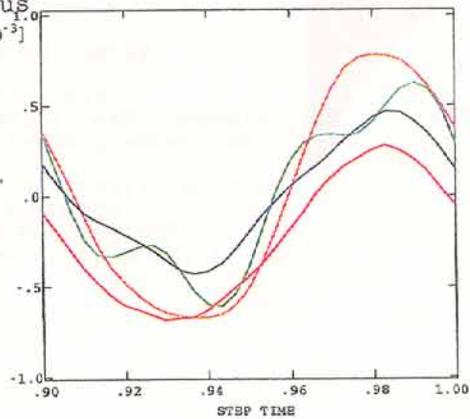
# ABAQUS

Elastic Modulus  
Varied [ $\times 10^{-3}$ ]



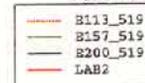
Input Freq.  
10 hz

Displacement  
at LVDT#3



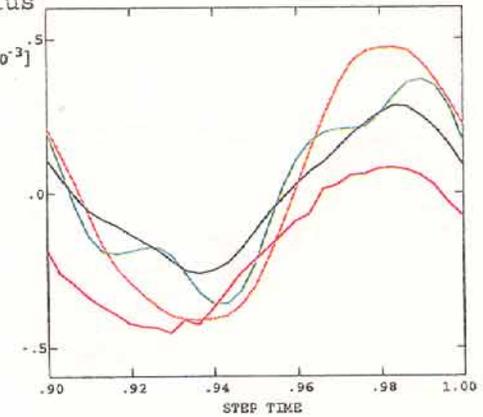
# ABAQUS

Elastic Modulus  
Varied [ $\times 10^{-3}$ ]



Input Freq.  
10 hz

Displacement  
at LVDT#2

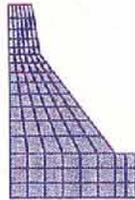


# ABAQUS

Koyna Laboratory Model Study  
 Uncracked Model Study  
 Sensitivity Study  
 Variation of Elastic Modulus

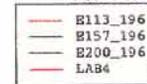
At Diff. Input Frequencies  
 Comparison of Displacements  
 Dynamic Analysis

Input Record SHAKEA  
 Mesh # 3



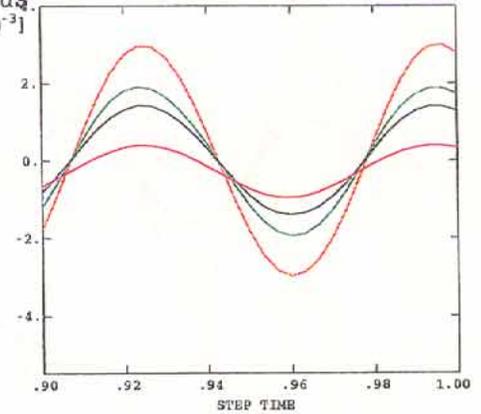
# ABAQUS

Elastic Modulus  
 Varied [ $\times 10^{-3}$ ]



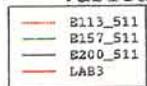
Input Freq.  
 14 hz

Displacement  
 at LVDT#4



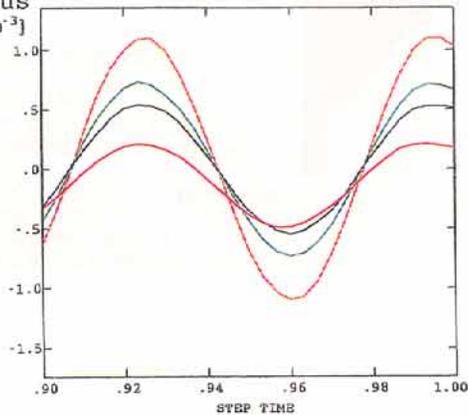
# ABAQUS

Elastic Modulus  
 Varied [ $\times 10^{-3}$ ]



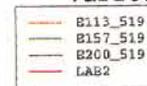
Input Freq.  
 14 hz

Displacement  
 at LVDT#3



# ABAQUS

Elastic Modulus  
 Varied [ $\times 10^{-3}$ ]



Input Freq.  
 14 hz

Displacement  
 at LVDT#2

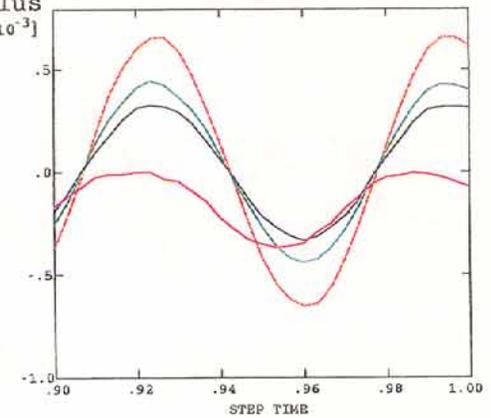


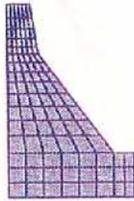
Figure g23

# ABAQUS

Koyna Laboratory Model Study  
Uncracked Model Study  
Sensitivity Study  
Variation of Elastic Modulus

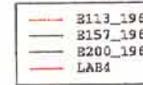
At Diff. Input Frequencies  
Comparison of Displacements  
Dynamic Analysis

Input Record SHAKEA  
Mesh # 3



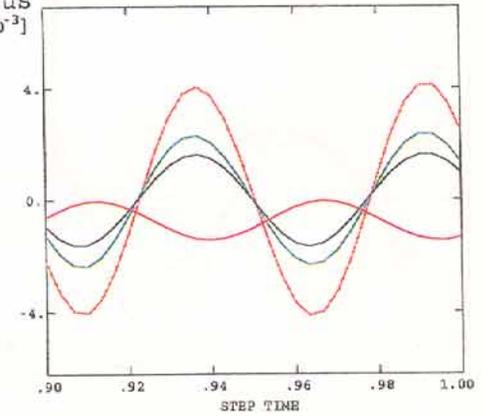
# ABAQUS

Elastic Modulus  
Varied [ $\times 10^3$ ]



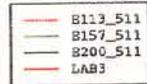
Input Freq.  
18 hz

Displacement  
at LVDT#4



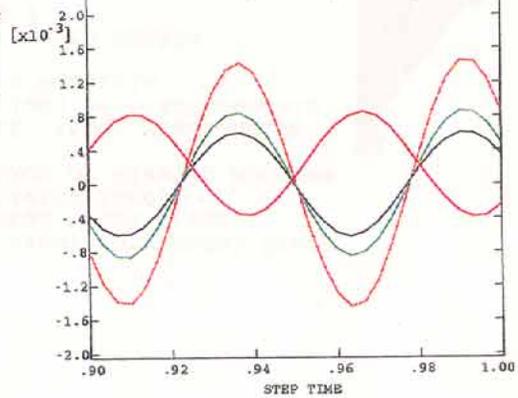
# ABAQUS

Elastic Modulus  
Varied



Input Freq.  
18 hz

Displacement  
at LVDT#3



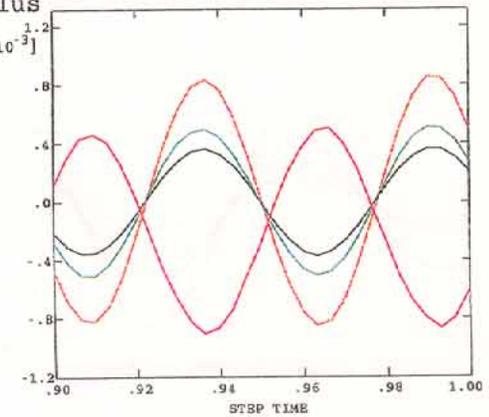
# ABAQUS

Elastic Modulus  
Varied [ $\times 10^3$ ]



Input Freq.  
18 hz

Displacement  
at LVDT#2

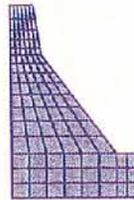


# ABAQUS

Koyna Laboratory Model Study  
 Uncracked Model Study  
 Sensitivity Study  
 Variation of Elastic Modulus

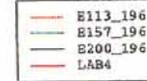
At Diff. Input Frequencies  
 Comparison of Displacements  
 Dynamic Analysis

Input Record SHAKEA  
 Mesh # 3



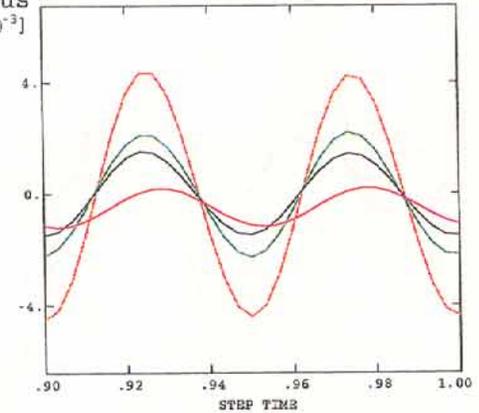
# ABAQUS

Elastic Modulus  
 Varied [ $\times 10^{-3}$ ]



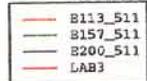
Input Freq.  
 20 hz

Displacement  
 at LVDT#4



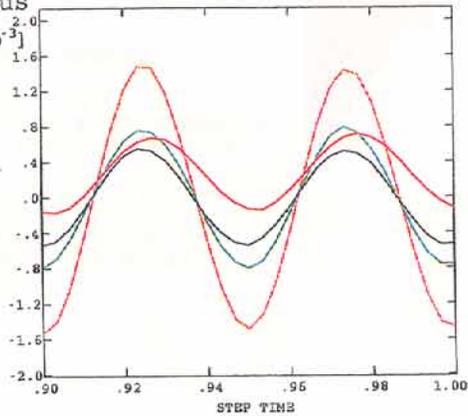
# ABAQUS

Elastic Modulus  
 Varied [ $\times 10^{-3}$ ]



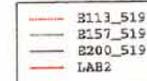
Input Freq.  
 20 hz

Displacement  
 at LVDT#3



# ABAQUS

Elastic Modulus<sub>2</sub>  
 Varied [ $\times 10^{-3}$ ]



Input Freq.  
 20 hz

Displacement  
 at LVDT#2

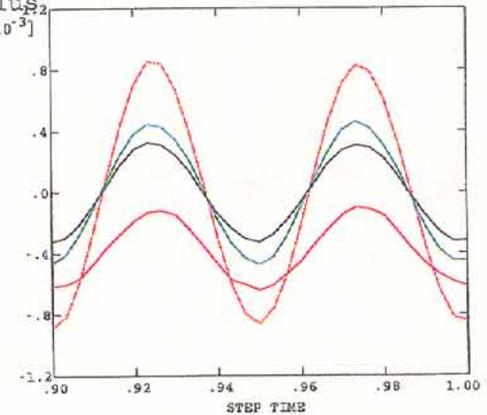


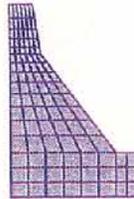
Figure g25

# ABAQUS

Koyna Laboratory Model Study  
 Uncracked Model Study  
 Sensitivity Study  
 Variation of Elastic Modulus

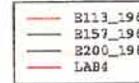
At Diff. Input Frequencies  
 Comparison of Displacements  
 Dynamic Analysis

Input Record SHAKEA  
 Mesh # 3



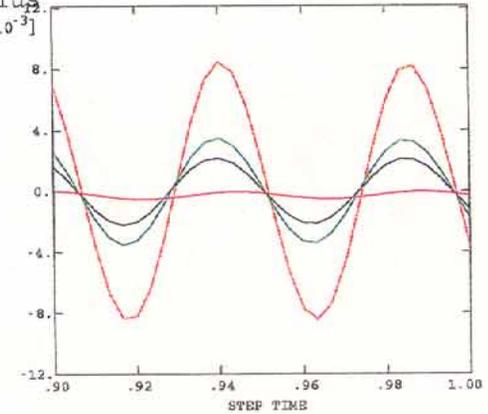
# ABAQUS

Elastic Modulus  
 Varied [ $\times 10^{-3}$ ]



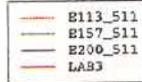
Input Freq.  
 22 hz

Displacement  
 at LVDT#4



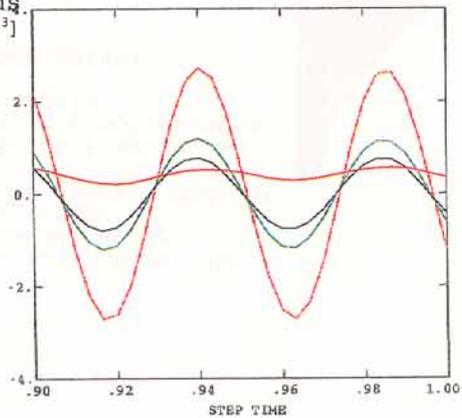
# ABAQUS

Elastic Modulus  
 Varied [ $\times 10^{-3}$ ]



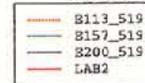
Input Freq.  
 22 hz

Displacement  
 at LVDT#3



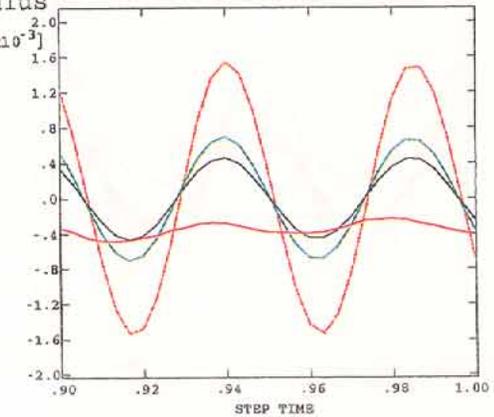
# ABAQUS

Elastic Modulus  
 Varied [ $\times 10^{-3}$ ]



Input Freq.  
 22 hz

Displacement  
 at LVDT#2

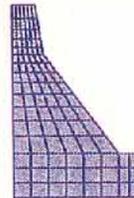


# ABAQUS

Koyna Laboratory Model Study  
 Uncracked Model Study  
 Sensitivity Study  
 Variation of Elastic Modulus

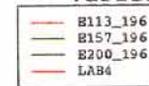
At Diff. Input Frequencies  
 Comparison of Displacements  
 Dynamic Analysis

Input Record SHAKEA  
 Mesh # 3



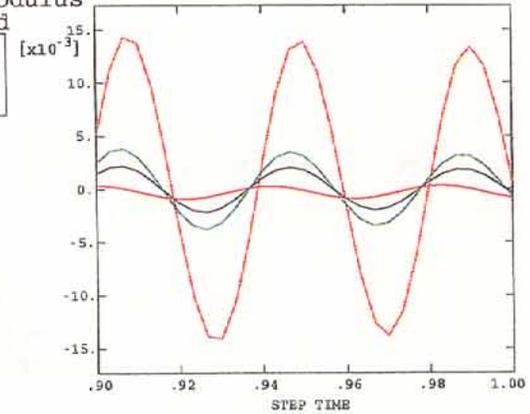
# ABAQUS

Elastic Modulus  
 Varied



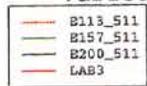
Input Freq.  
 24 hz

Displacement  
 at LVDT#4



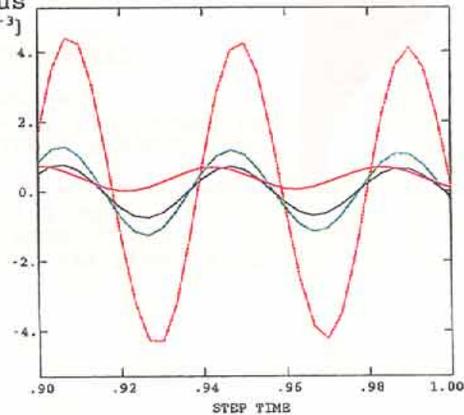
# ABAQUS

Elastic Modulus  
 Varied [ $\times 10^{-3}$ ]



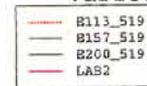
Input Freq.  
 24 hz

Displacement  
 at LVDT#3



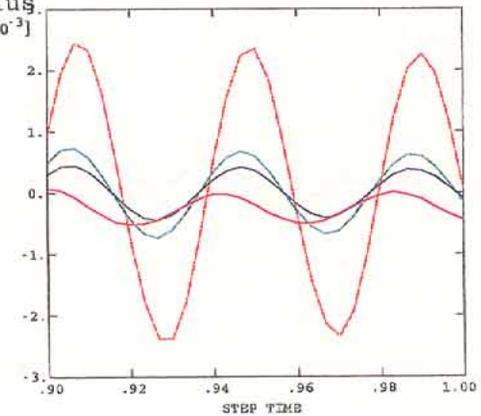
# ABAQUS

Elastic Modulus  
 Varied [ $\times 10^{-3}$ ]



Input Freq.  
 24 hz

Displacement  
 at LVDT#2

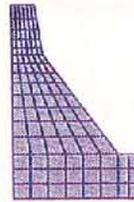


# ABAQUS

Koyna Laboratory Model Study  
 Uncracked Model Study  
 Sensitivity Study  
 Variation of Elastic Modulus

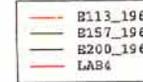
At Diff. Input Frequencies  
 Comparison of Displacements  
 Dynamic Analysis

Input Record SHAKEA  
 Mesh # 3



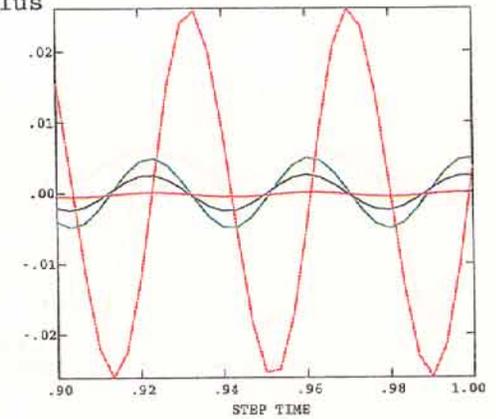
# ABAQUS

Elastic Modulus  
 Varied



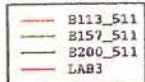
Input Freq.  
 26 hz

Displacement  
 at LVDT#4



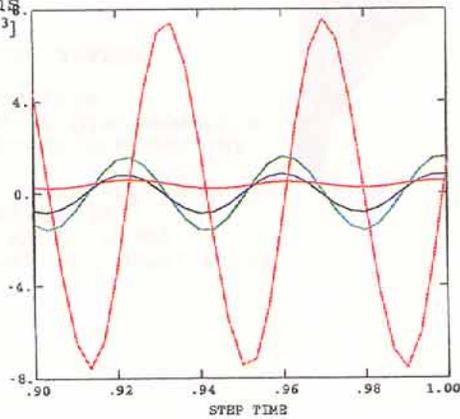
# ABAQUS

Elastic Modulus  
 Varied [ $\times 10^3$ ]



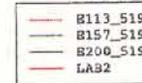
Input Freq.  
 26 hz

Displacement  
 at LVDT#3



# ABAQUS

Elastic Modulus  
 Varied [ $\times 10^3$ ]



Input Freq.  
 25 hz

Displacement  
 at LVDT#2

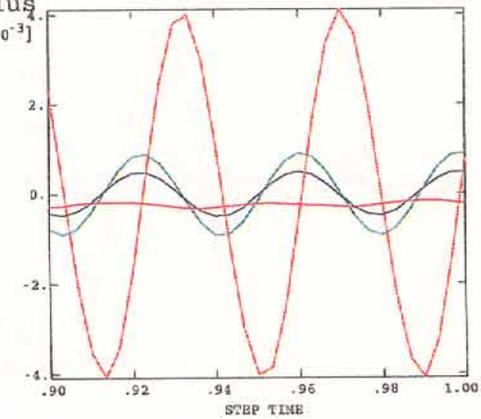


Figure g28

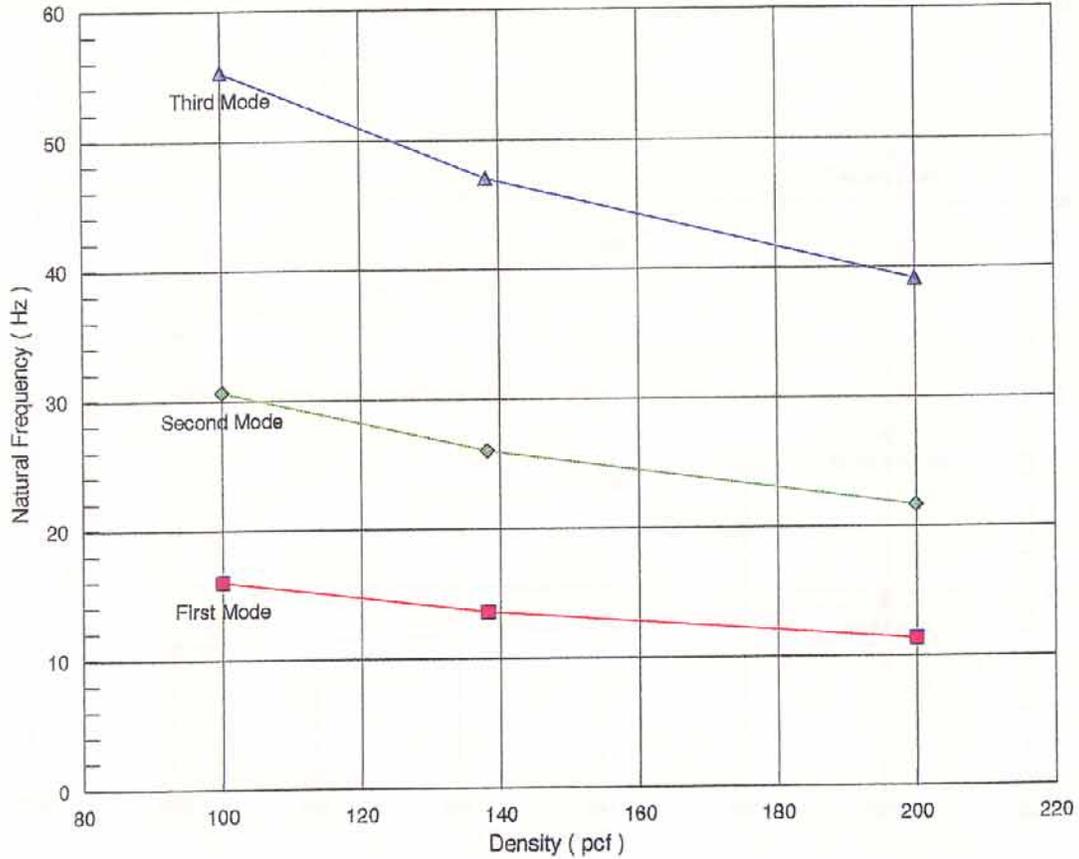
Uncracked Koyna Laboratory Study  
Sensitivity to Variation in Material Density  
Mesh#3

Material Properties

Elastic Modulus = 113 ksi  
Material Density = (100, 138, 200 pcf)

Damping = 3.5% critical  
Rayleigh Damping Factors  
Alpha = 1.954769; Beta = .000248

Natural Frequency  
Material Density Varied



E = 113 ksi

Natural Frequencies (Hz)

Mode	100	138.2	200	LAB
1	16.0	13.6	11.3	18.0
2	30.6	26.0	21.6	24.0
3	55.3	47.0	39.1	30.0
4	65.8	55.9	46.5	
5	68.7	58.4	48.5	
6	70.8	60.2	50.1	
7	75.2	64.0	53.2	
8	76.2	64.8	53.9	
9	76.9	65.4	54.4	
10	78.4	66.7	55.4	

Figure g29

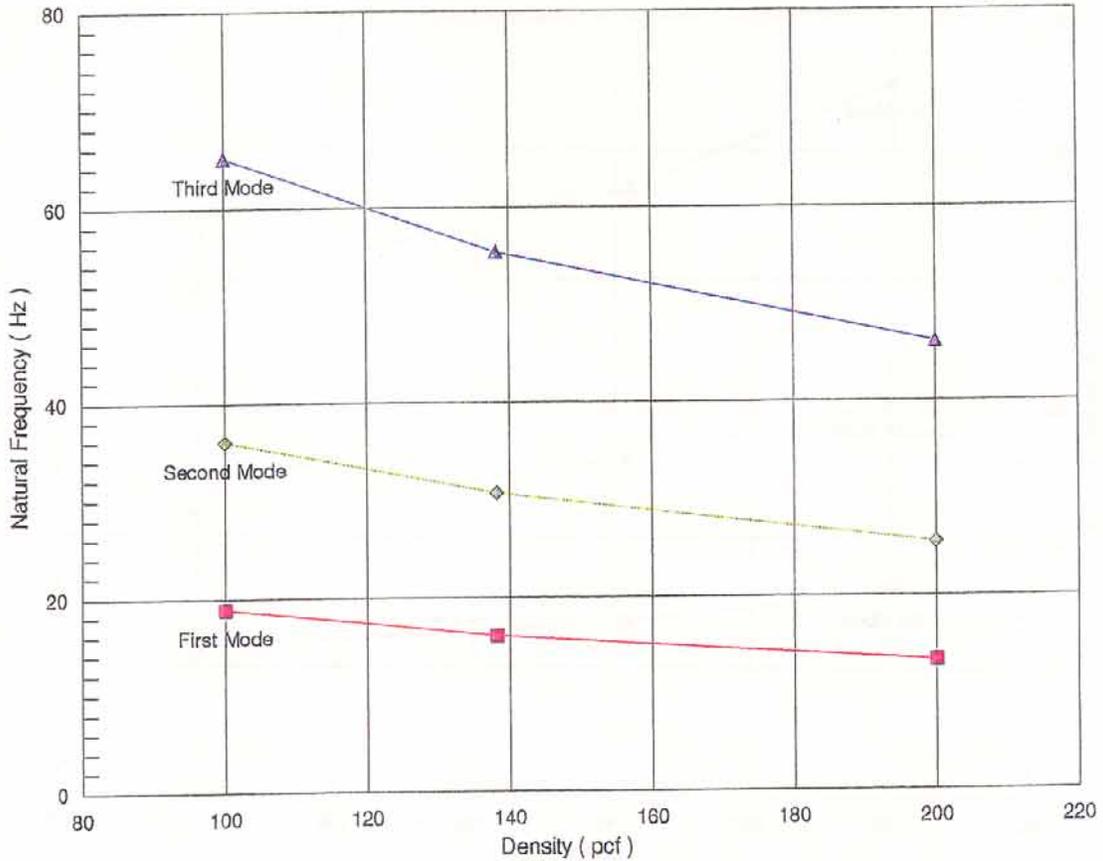
Uncracked Koyna Laboratory Study  
Sensitivity to Variation in Material Density  
Mesh#3

Material Properties

Elastic Modulus = 157 ksi  
Material Density = (100, 138, 200 pcf)

Damping = 3.5% critical  
Rayleigh Damping Factors

**Natural Frequencies**  
Material Density Varied



E = 157 ksi

Natural Frequencies (Hz)

Mode	100	138.2	200	LAB
1	18.8	16.0	13.3	18.0
2	36.0	30.6	25.5	22.0
3	65.1	55.4	46.1	30.0
4	77.5	65.9	54.8	
5	80.9	68.8	57.2	
6	83.5	71.0	59.0	
7	88.7	75.4	62.7	
8	89.8	76.4	63.5	
9	90.6	77.1	64.1	
10	92.4	78.6	65.3	

Figure g30

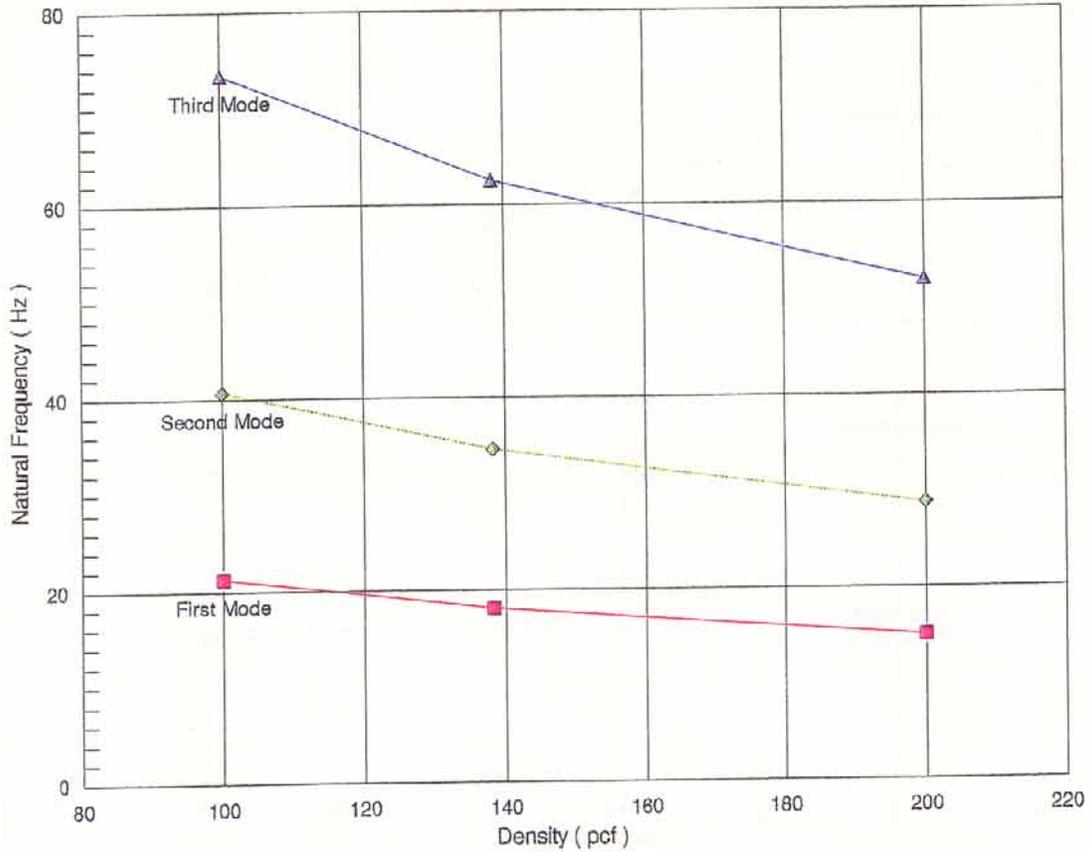
Uncracked Koyna Laboratory Study  
Sensitivity to Variation in Material Density  
Mesh#3

Material Properties

Elastic Modulus = 200 ksi  
Material Density = (100, 138, 200 pcf)

Damping = 3.5% critical  
Rayleigh Damping Factors  
Alpha = 1.954769; Beta = .000248

**Natural Frequencies**  
Material Density Varied



E = 200 ksi

Natural Frequencies (Hz)

Mode	100	138.2	200	LAB
1	21.3	18.1	15.0	18.0
2	40.7	34.6	28.7	24.0
3	73.5	62.5	52.0	30.0
4	87.5	74.4	61.9	
5	91.3	77.7	64.6	
6	94.2	80.1	66.6	
7	100.1	85.1	70.8	
8	101.3	86.2	71.6	
9	102.3	87.0	72.3	
10	104.3	88.7	73.7	

Figure g31

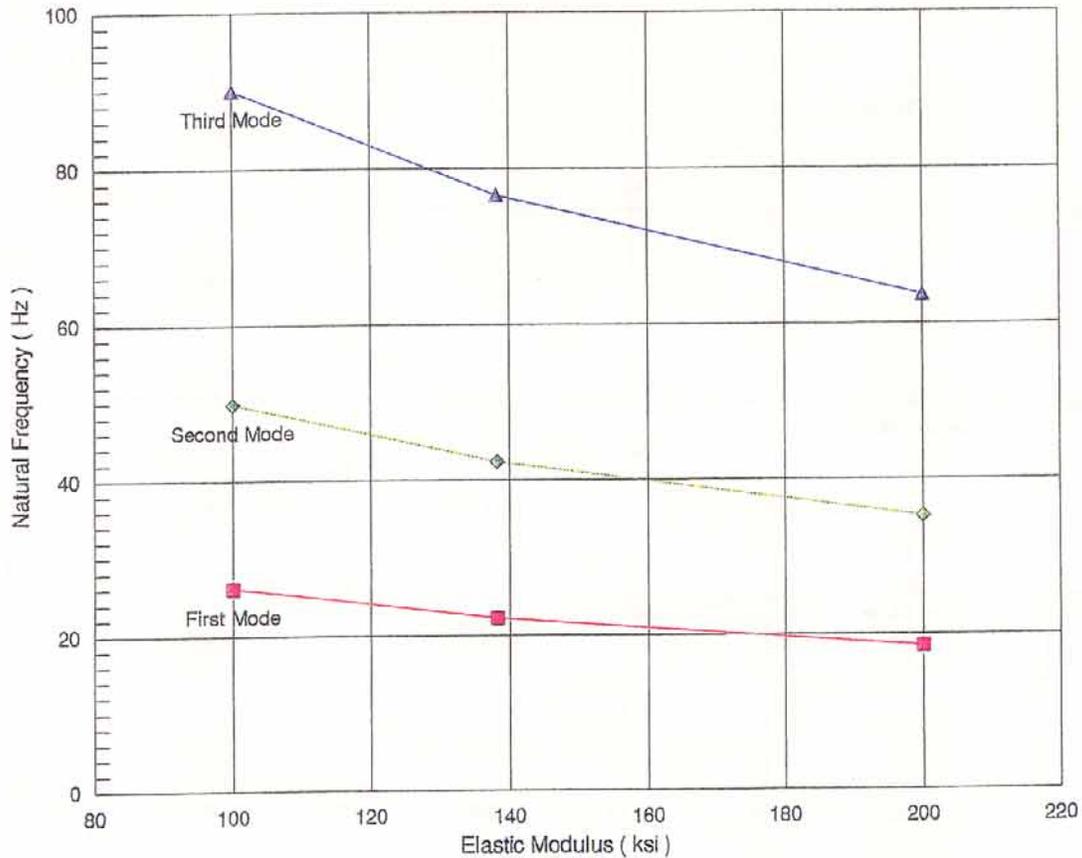
Uncracked Koyna Laboratory Study  
Sensitivity to Variation in Material Density  
Mesh#3

Material Properties

Elastic Modulus = 300 ksi  
Material Density = (100, 138, 200 pcf)

Damping = 3.5% critical  
Rayleigh Damping Factors  
Alpha = 1.954769; Beta = .000248

**Natural Frequency**  
Material Density Varied



E = 300 ksi

Natural Frequencies (Hz)

Mode	100	138.2	200	LAB
1	26.0	22.2	18.4	18.0
2	49.8	42.4	35.2	24.0
3	90.0	76.6	63.7	30.0
4	107.2	91.1	75.8	
5	111.9	95.2	79.1	
6	115.4	98.1	81.6	
7	122.5	104.2	86.7	
8	124.1	105.6	87.7	
9	125.3	106.6	88.6	
10	127.7	108.7	90.3	

Figure g32

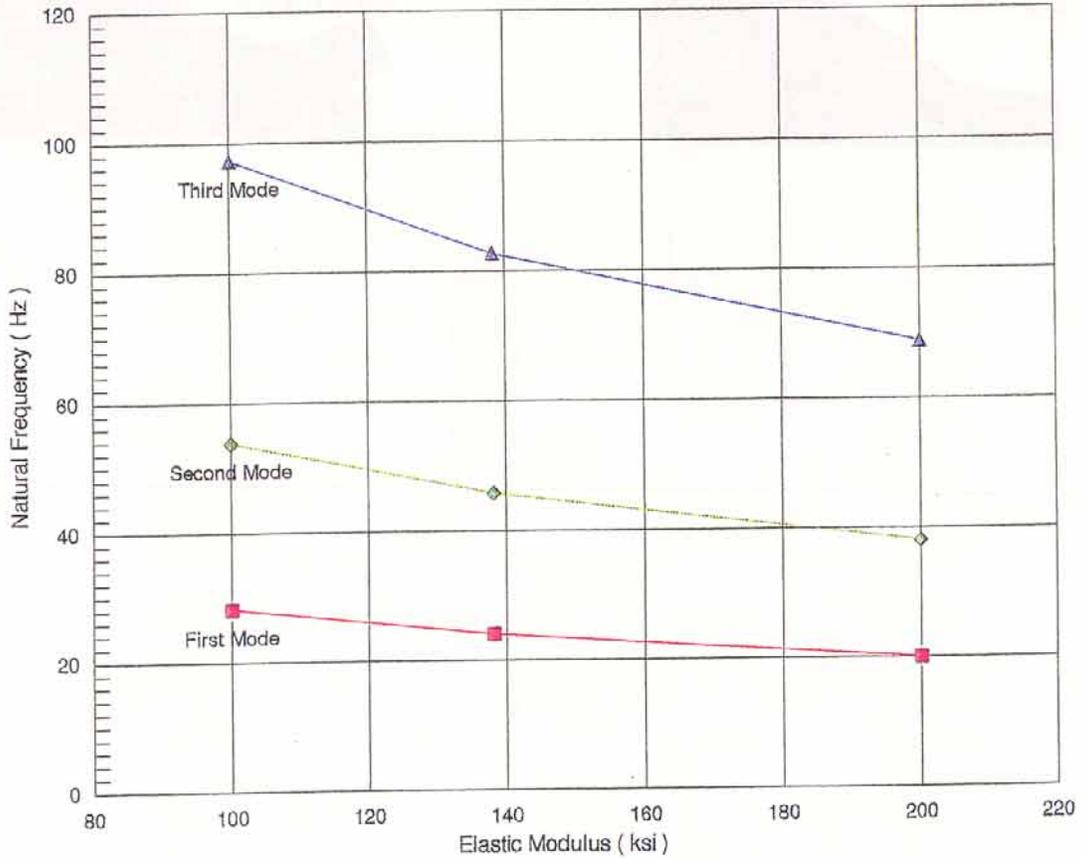
Uncracked Koyna Laboratory Study  
Sensitivity to Variation in Material Density  
Mesh#3

Material Properties

Elastic Modulus = 350 ksi  
Material Density = (100, 138, 200 pcf)

Damping = 3.5% critical  
Rayleigh Damping Factors  
Alpha = 1.954769; Beta = .000248

Natural Frequency  
Material Density Varied



E = 350 ksi

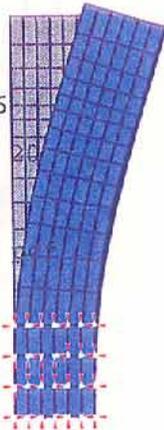
Natural Frequencies (Hz)

Mode	100	138.2	200	LAB
1	28.1	24.0	19.9	18.0
2	53.8	45.7	38.0	24.0
3	97.2	82.7	68.8	30.0
4	115.7	98.4	81.8	
5	120.8	102.8	85.4	
6	124.6	106.0	88.1	
7	132.4	112.6	93.6	
8	134.0	114.0	94.8	
9	135.3	115.1	95.7	
10	138.0	117.4	97.6	

Figure g33

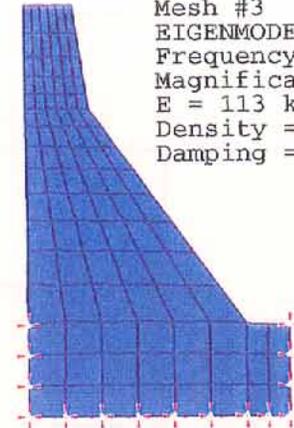
# ABAQUS

Mesh #3  
EIGENMODE 1  
Frequency = 13.6  
Magnification = 20  
E = 113 ksi  
Density = 138.2  
Damping = 3.5%



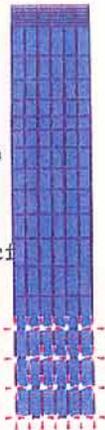
# ABAQUS

Mesh #3  
EIGENMODE 1  
Frequency = 13.6  
Magnification = 20  
E = 113 ksi  
Density = 138.2 pcf  
Damping = 3.5%



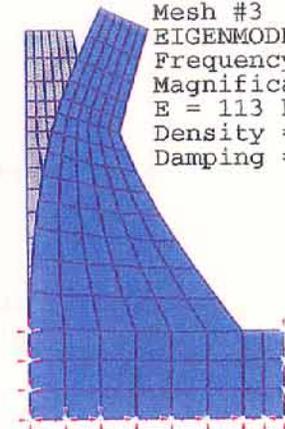
# ABAQUS

Mesh #3  
EIGENMODE 2  
Frequency = 26  
Magnification = 20  
E = 113 ksi  
Density = 138.2 pcf  
Damping = 3.5%



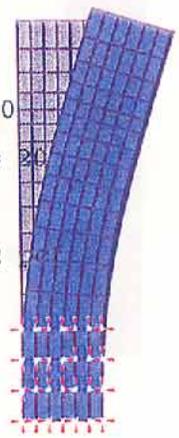
# ABAQUS

Mesh #3  
EIGENMODE 2  
Frequency = 26  
Magnification = 20  
E = 113 ksi  
Density = 138.2 pcf  
Damping = 3.5%



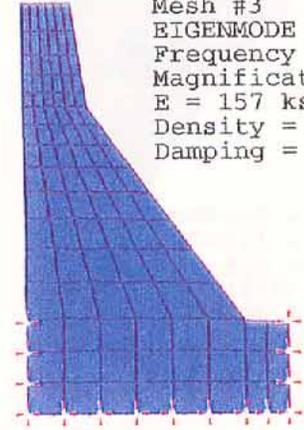
# ABAQUS

Mesh #3  
EIGENMODE 1  
Frequency = 16.0  
Magnification = 20  
E = 157 ksi  
Density = 138.2 pcf  
Damping = 3.5%



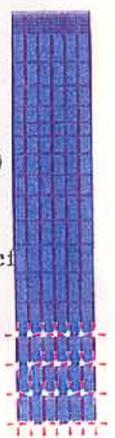
# ABAQUS

Mesh #3  
EIGENMODE 1  
Frequency = 16.0  
Magnification = 20  
E = 157 ksi  
Density = 138.2 pcf  
Damping = 3.5%



# ABAQUS

Mesh #3  
EIGENMODE 2  
Frequency = 30.6  
Magnification = 20  
E = 157 ksi  
Density = 138.2 pcf  
Damping = 3.5%



# ABAQUS

Mesh #3  
EIGENMODE 2  
Frequency = 30.6  
Magnification = 20  
E = 157 ksi  
Density = 138.2 pcf  
Damping = 3.5%

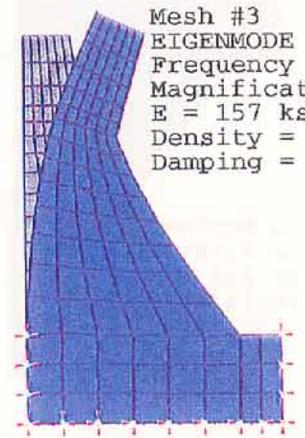
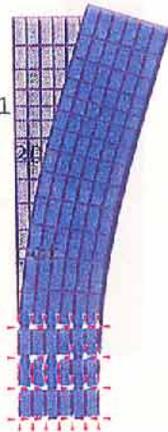


Figure g35

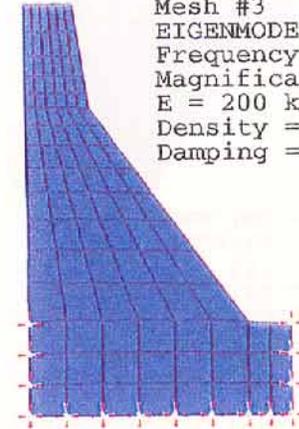
# ABAQUS

Mesh #3  
EIGENMODE 1  
Frequency = 18.1  
Magnification = 20  
E = 200 ksi  
Density = 138.2  
Damping = 3.5%



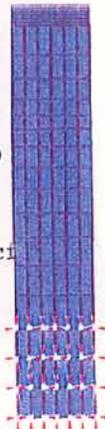
# ABAQUS

Mesh #3  
EIGENMODE 1  
Frequency = 18.1  
Magnification = 20  
E = 200 ksi  
Density = 138.2 pcf  
Damping = 3.5%



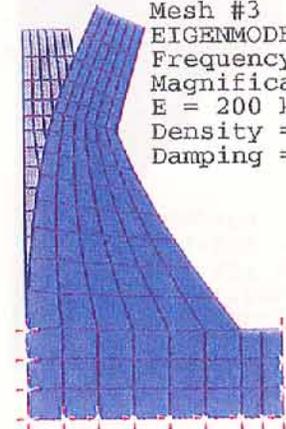
# ABAQUS

Mesh #3  
EIGENMODE 2  
Frequency = 34.6  
Magnification = 20  
E = 200 ksi  
Density = 138.2 pcf  
Damping = 3.5%



# ABAQUS

Mesh #3  
EIGENMODE 2  
Frequency = 34.6  
Magnification = 20  
E = 200 ksi  
Density = 138.2 pcf  
Damping = 3.5%



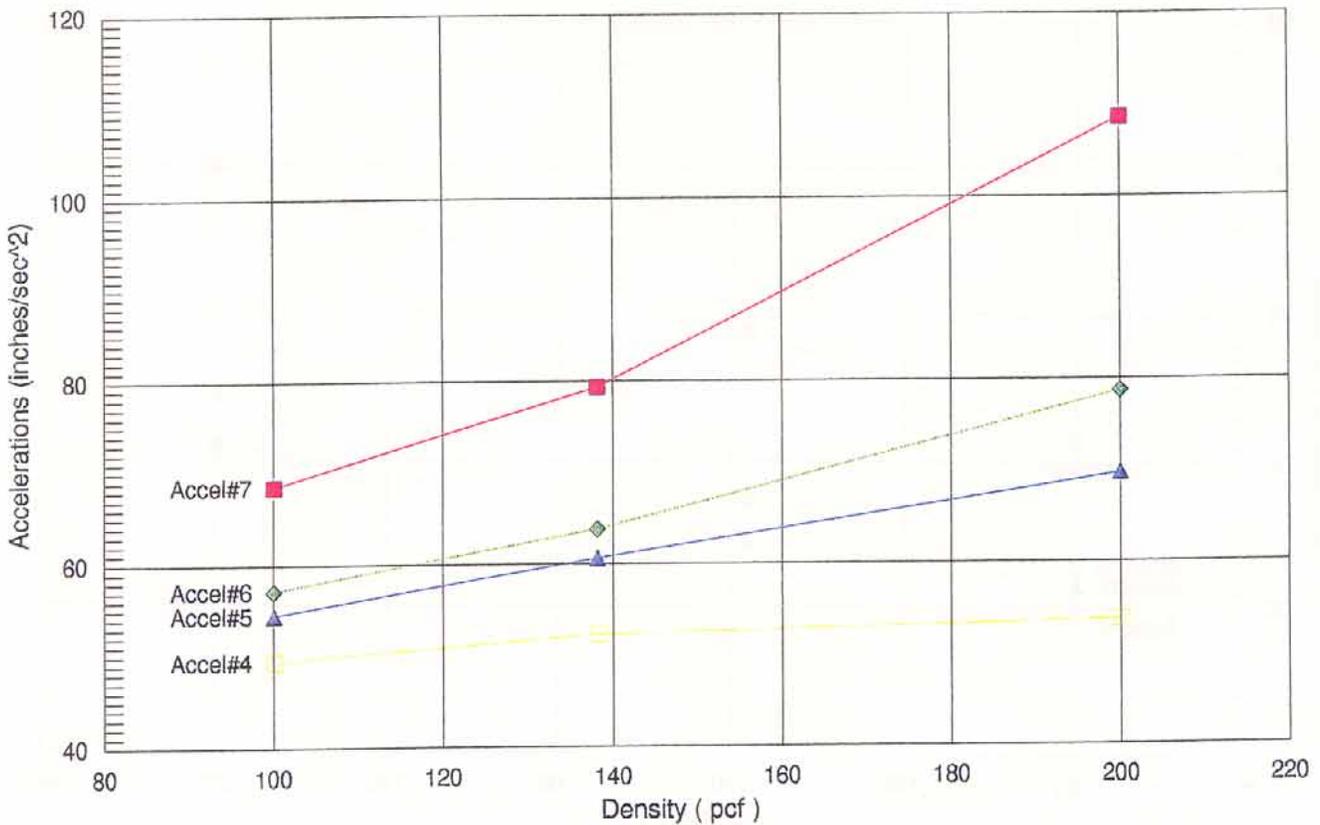
Uncracked Koyna Laboratory Study  
Sensitivity to Variation in Material Density  
Mesh#3

Material Properties

E = 113,000 psi  
Material Density = (100, 138, 200 pcf)

Damping = 3.5% critical  
Rayleigh Damping Factors  
Alpha = 1.954769; Beta = .000248

**Peak Accelerations**  
Material Density Varied



E = 113 ksi

Peak Accelerations ( inch / sec ^ 2 )

	100	138.2	200	LAB
Accel#7	68.51	79.31	108.60	53.26
Accel#6	57.18	63.80	78.68	51.72
Accel#5	54.49	60.60	69.67	49.26
Accel#4	49.40	52.28	53.65	47.72

Figure g37

Uncracked Koyna Laboratory Study  
Sensitivity to Variation in Material Density  
Mesh#3

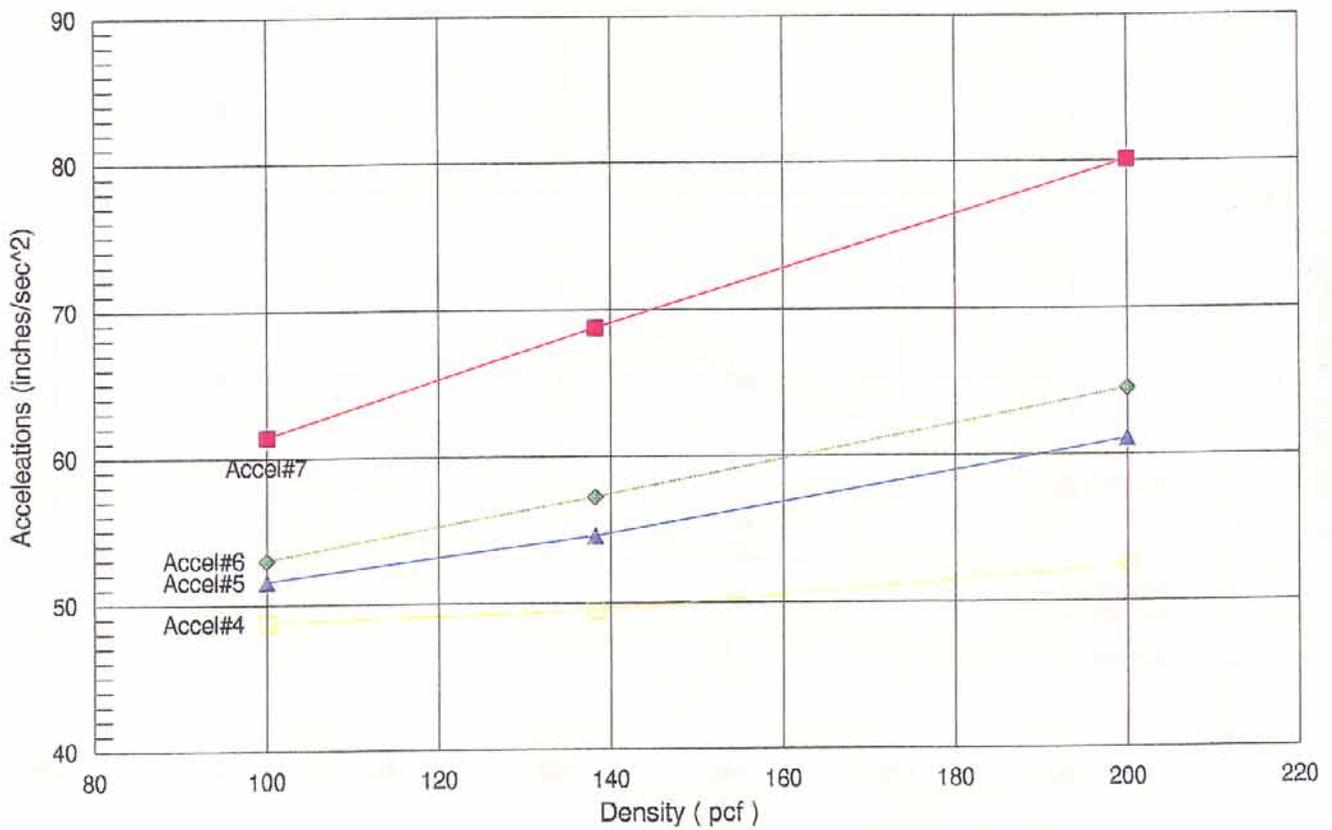
Material Properties

E = 157,000 psi  
Material Density = (100, 138, 200 pcf)

Damping = 3.5% critical

Rayleigh Damping Factors  
Alpha = 1.954769; Beta = .000248

**Peak Accelerations**  
Material Density Varied



E = 157 ksi

Peak Accelerations ( inch / sec ^ 2 )

	100	138.2	200	LAB
Accel#7	61.39	68.75	80.10	53.26
Accel#6	52.99	57.19	64.49	51.72
Accel#5	51.54	54.54	61.04	49.26
Accel#4	48.70	49.47	52.36	47.72

Figure g38

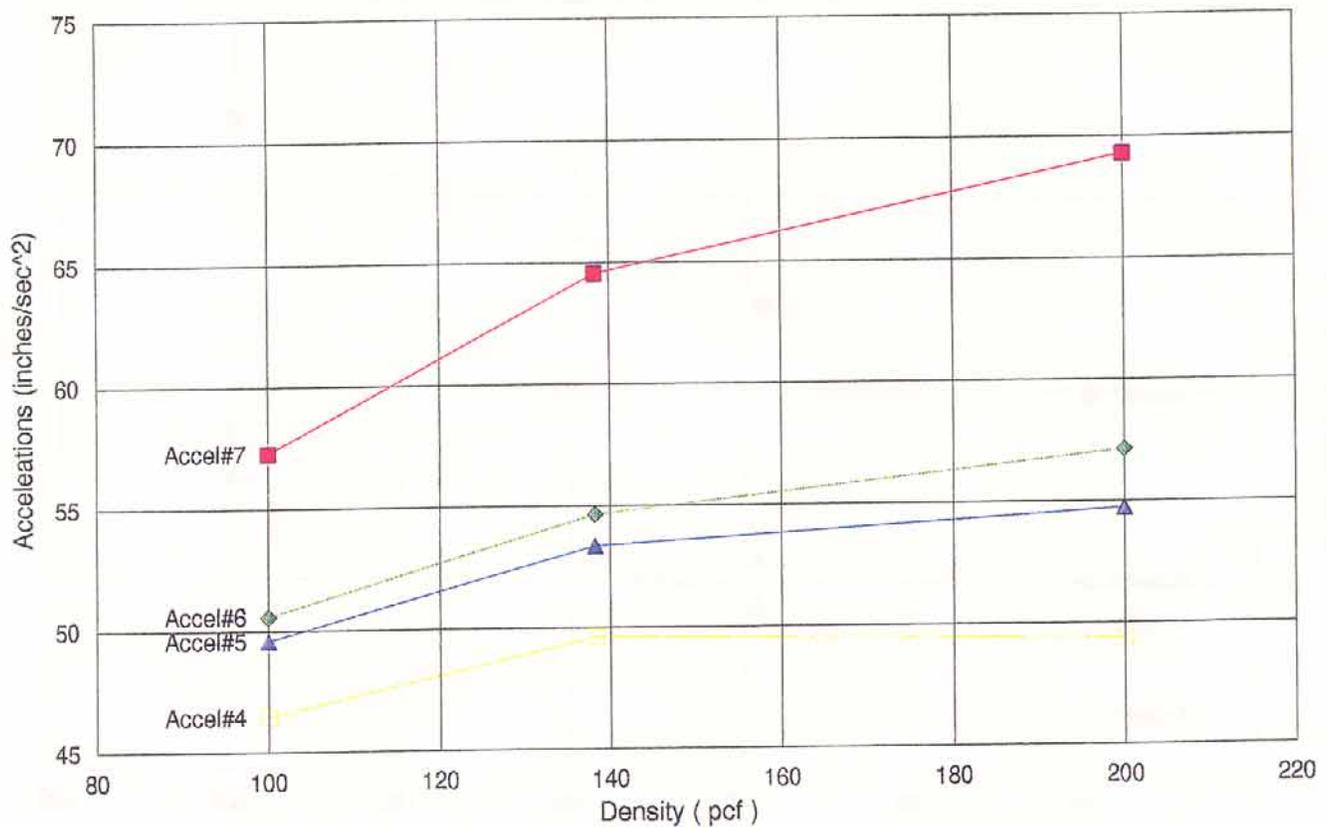
Uncracked Koyna Laboratory Study  
Sensitivity to Variation in Material Density  
Mesh#3

Material Properties

E = 200,000 psi  
Material Density = (100, 138, 200 pcf)

Damping = 3.5% critical  
Rayleigh Damping Factors  
Alpha = 1.954769; Beta = .000248

**Peak Accelerations**  
Material Density Varied



E = 200 ksi

Peak Accelerations ( inch / sec  <sup>2</sup>  )

	100	138.2	200	LAB
Accel#7	57.25	64.53	69.27	53.26
Accel#6	50.56	54.64	57.12	51.72
Accel#5	49.57	53.34	54.73	49.26
Accel#4	46.42	49.60	49.36	47.72

Figure g39

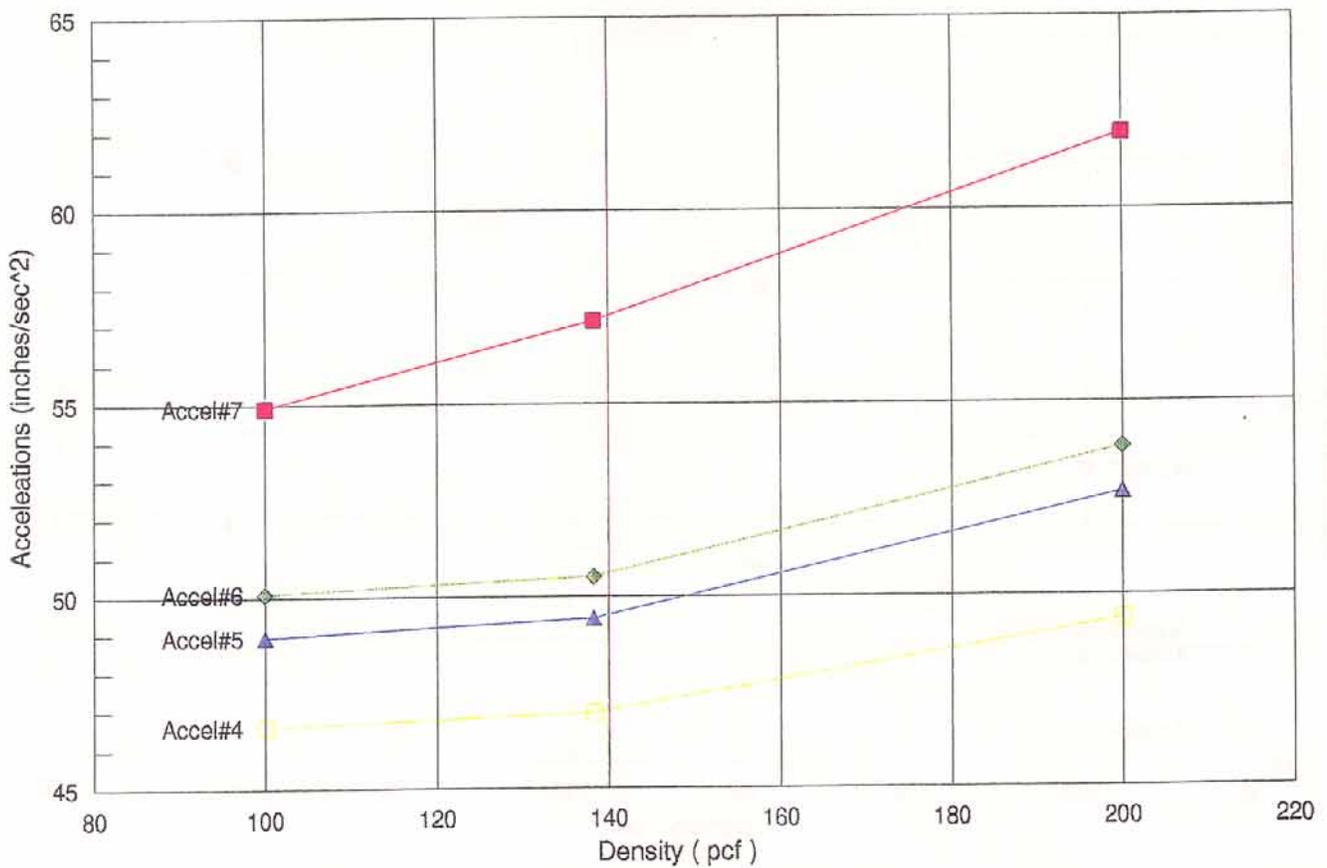
Uncracked Koyna Laboratory Study  
Sensitivity to Variation in Material Density  
Mesh#3

Material Properties

E = 300,000 psi  
Material Density = (100, 138, 200 pcf)

Damping = 3.5% critical  
Rayleigh Damping Factors  
Alpha = 1.954769; Beta = .000248

**Peak Accelerations**  
Material Density Varied



E = 300 ksi

Peak Accelerations ( inch / sec ^ 2 )

	100	138.2	200	<b>LAB</b>
Accel#7	54.90	57.14	61.96	53.26
Accel#6	50.07	50.50	53.82	51.72
Accel#5	48.93	49.42	52.65	49.26
Accel#4	46.59	46.97	49.36	47.72

Figure g40

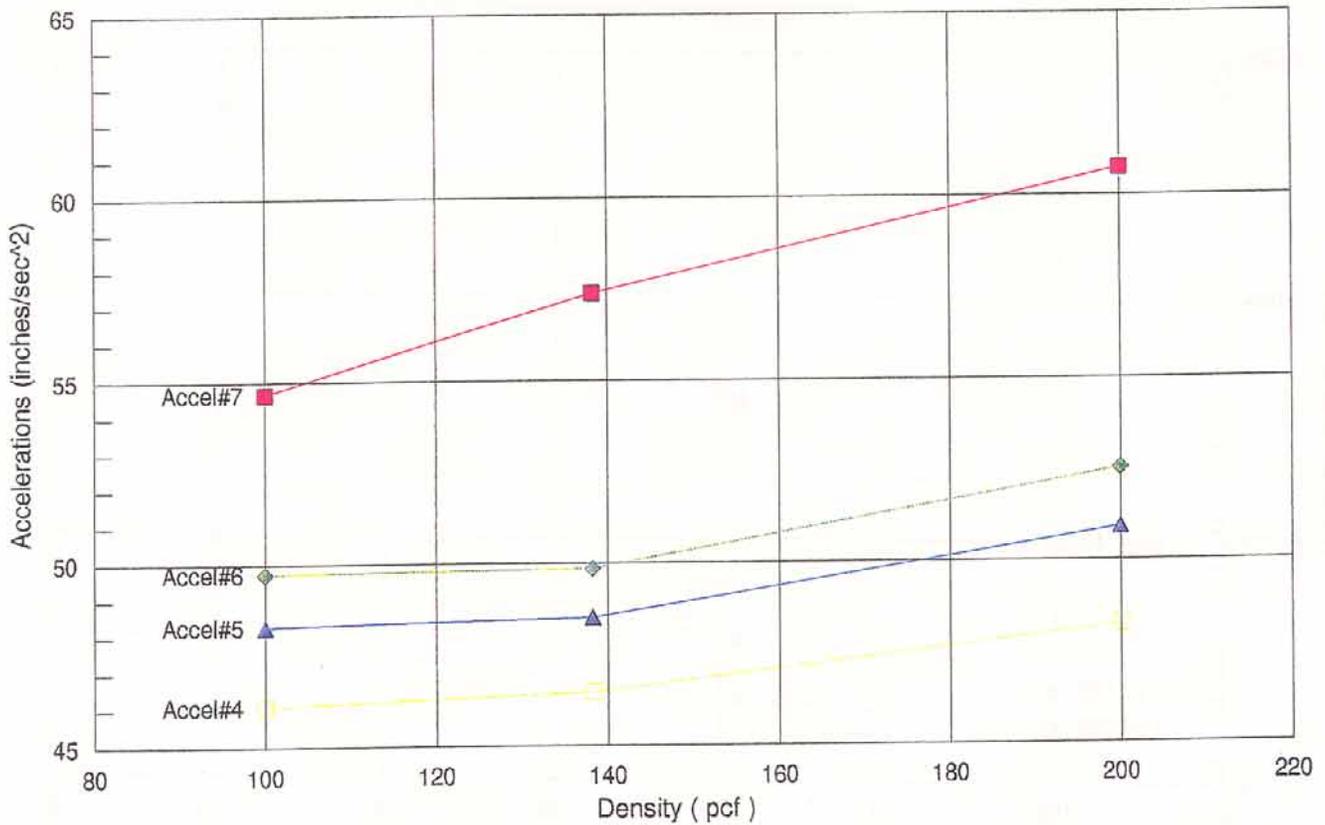
Uncracked Koyna Laboratory Study  
Sensitivity to Variation in Material Density  
Mesh#3

Material Properties

E = 350,000 psi  
Material Density = (100, 138, 200 pcf)

Damping = 3.5% critical  
Rayleigh Damping Factors  
Alpha = 1.954769; Beta = .000248

**Peak Accelerations**  
Material Density Varied



E = 350 ksi

Peak Accelerations ( inch / sec ^ 2 )

	100	138.2	200	LAB
Accel#7	54.66	57.39	60.74	53.26
Accel#6	49.73	49.85	52.52	51.72
Accel#5	48.29	48.51	50.91	49.26
Accel#4	46.09	46.47	48.24	47.72

Figure g41

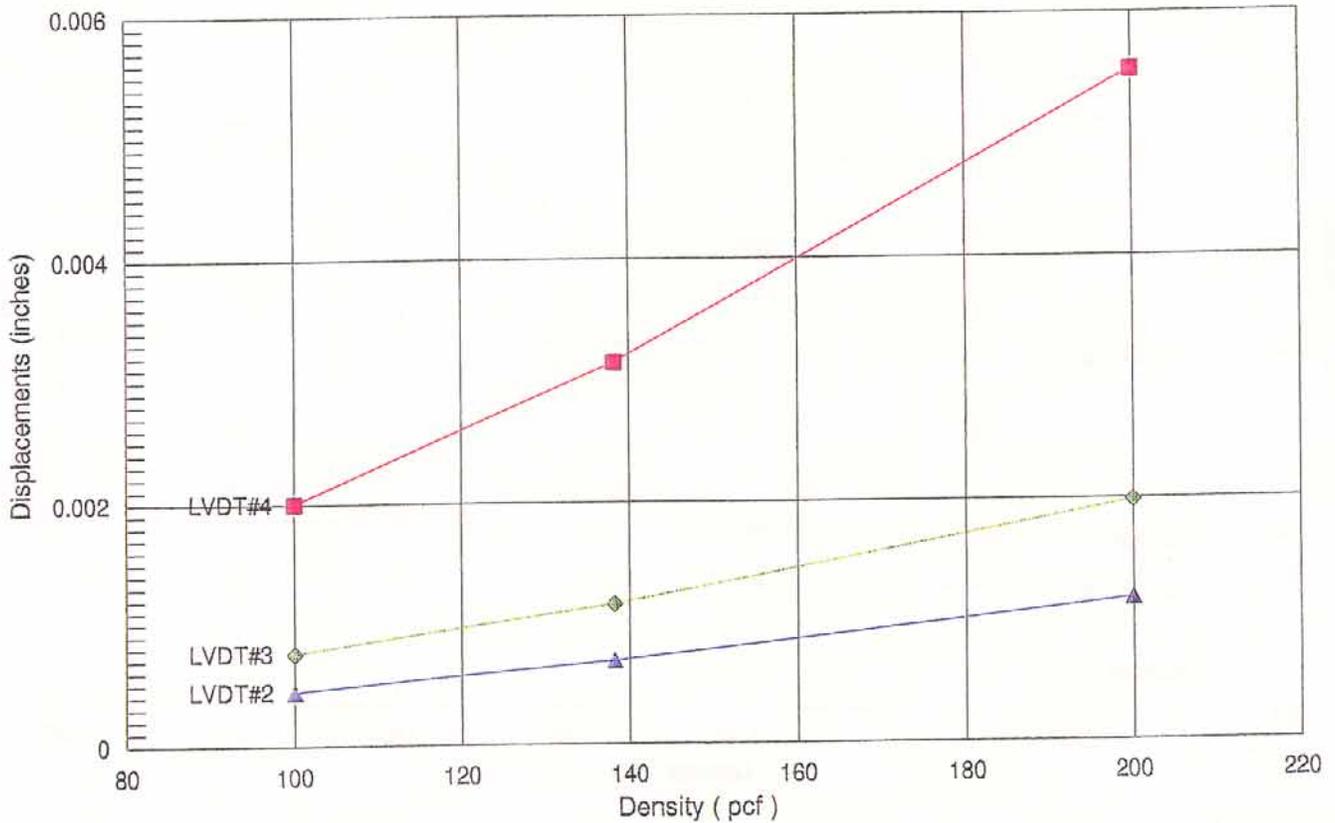
Uncracked Koyna Laboratory Study  
Sensitivity to Variation in Material Density  
Mesh#3

Material Properties

E = 113,000 psi  
Material Density = (100, 138, 200 pcf)

Damping = 3.5% critical  
Rayleigh Damping Factors  
Alpha = 1.954769; Beta = .000248

Peak Displacements  
Material Density Varied



E = 113 ksi

Peak Displacements ( inches )

	100	138.2	200	LAB
LVDT#4	2.0E-03	3.1E-03	5.5E-03	7.2E-04
LVDT#3	7.6E-04	1.2E-03	2.0E-03	3.1E-04
LVDT#2	4.5E-04	6.9E-04	1.2E-03	2.1E-04

Figure g42

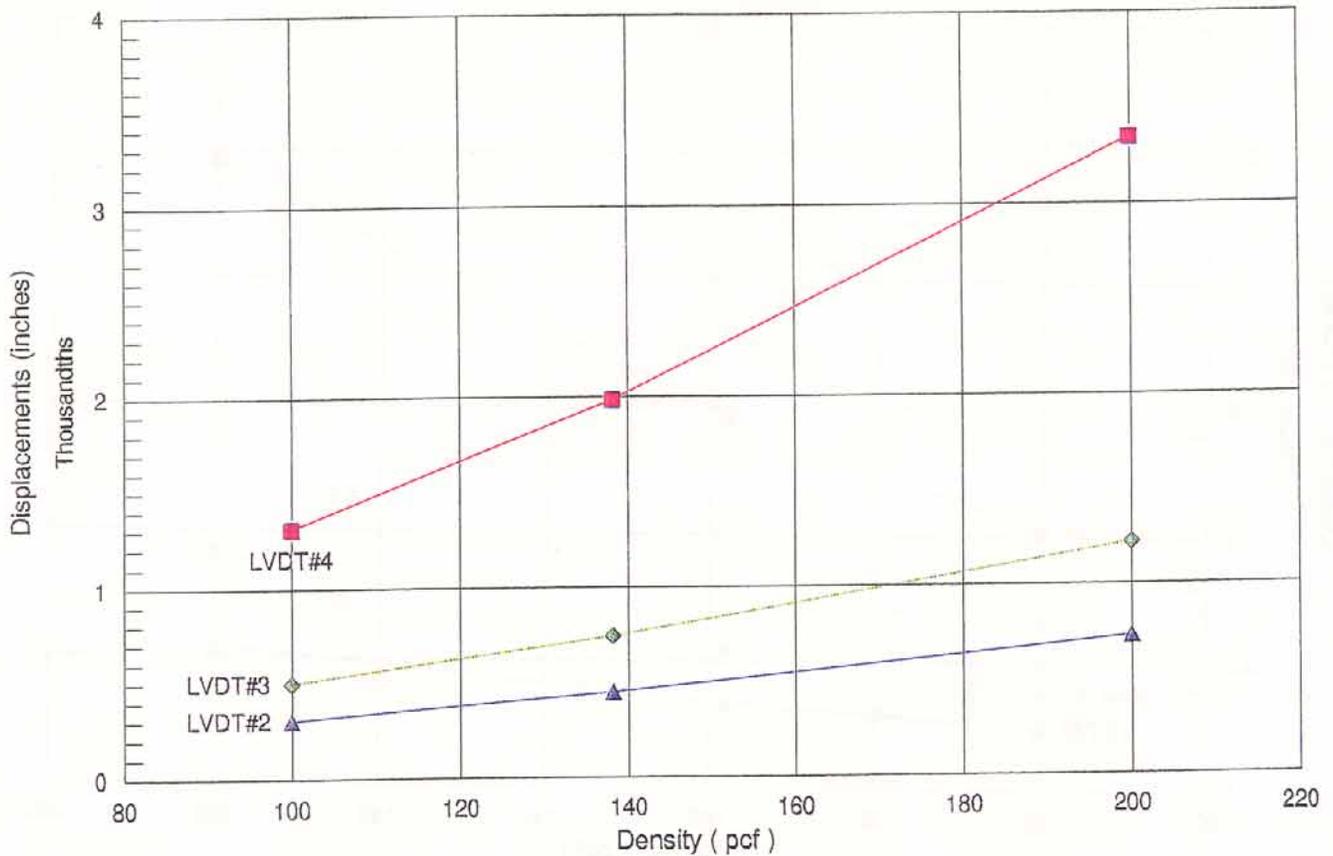
Uncracked Koyna Laboratory Study  
Sensitivity to Variation in Material Density  
Mesh#3

Material Properties

E = 157,000 psi  
Material Density = (100, 138, 200 pcf)

Damping = 3.5% critical  
Rayleigh Damping Factors  
Alpha = 1.954769; Beta = .000248

**Peak Displacements**  
Material Density Varied



E = 157 ksi

Peak Displacements ( inches )

	100	138.2	200	LAB
LVDT#4	1.3E-03	2.0E-03	3.3E-03	7.2E-04
LVDT#3	5.0E-04	7.4E-04	1.2E-03	3.1E-04
LVDT#2	3.0E-04	4.4E-04	7.2E-04	2.1E-04

Figure g43

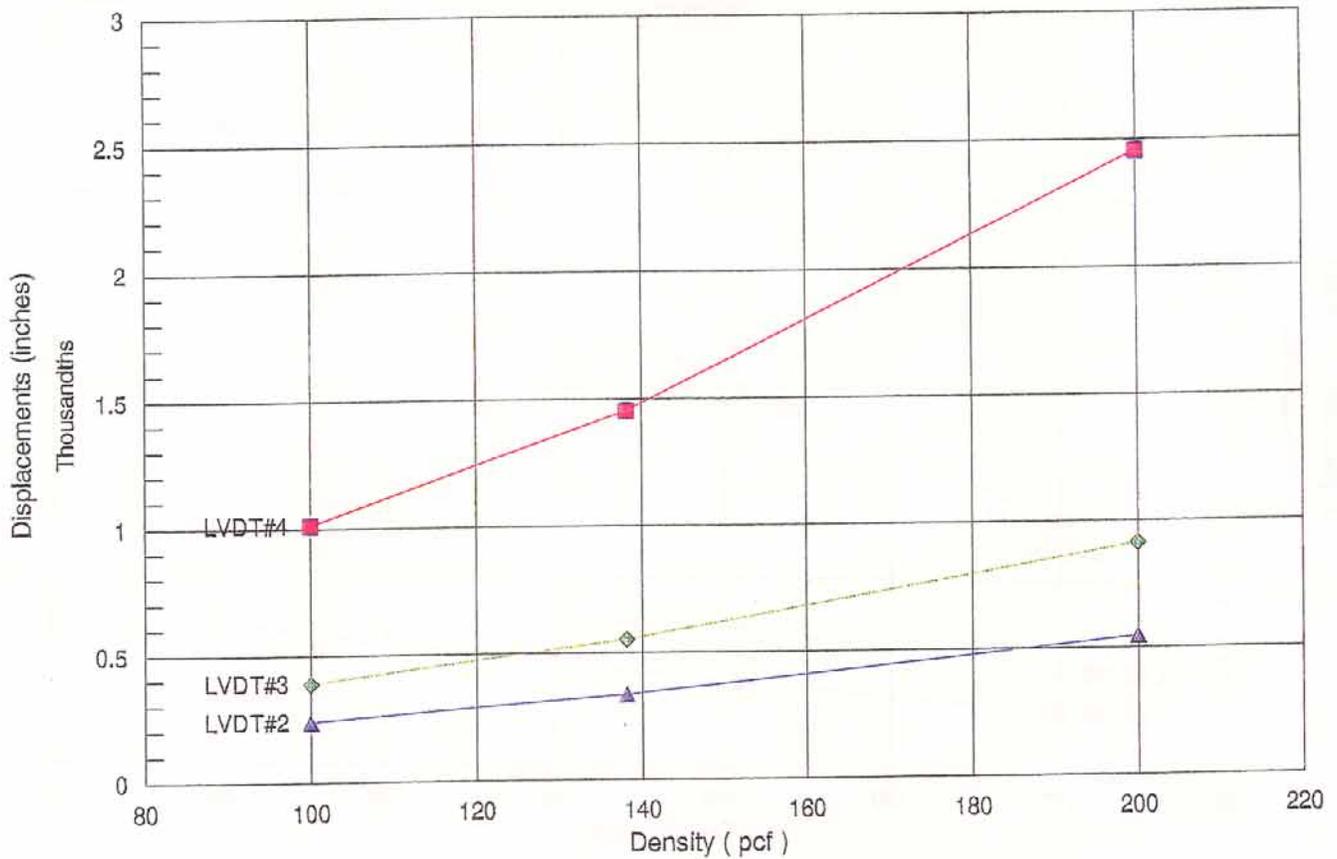
Uncracked Koyna Laboratory Study  
Sensitivity to Variation in Material Density  
Mesh#3

Material Properties

E = 200,000 psi  
Material Density = (100, 138, 200 pcf)

Damping = 3.5% critical  
Rayleigh Damping Factors  
Alpha = 1.954769; Beta = .000248

**Peak Displacements**  
Material Density Varied



E = 200 ksi

Peak Displacements ( inches )

	100	138.2	200	LAB
LVDT#4	1.0E-03	1.5E-03	2.5E-03	7.2E-04
LVDT#3	3.9E-04	5.5E-04	9.1E-04	3.1E-04
LVDT#2	2.4E-04	3.3E-04	5.5E-04	2.1E-04

Figure g44

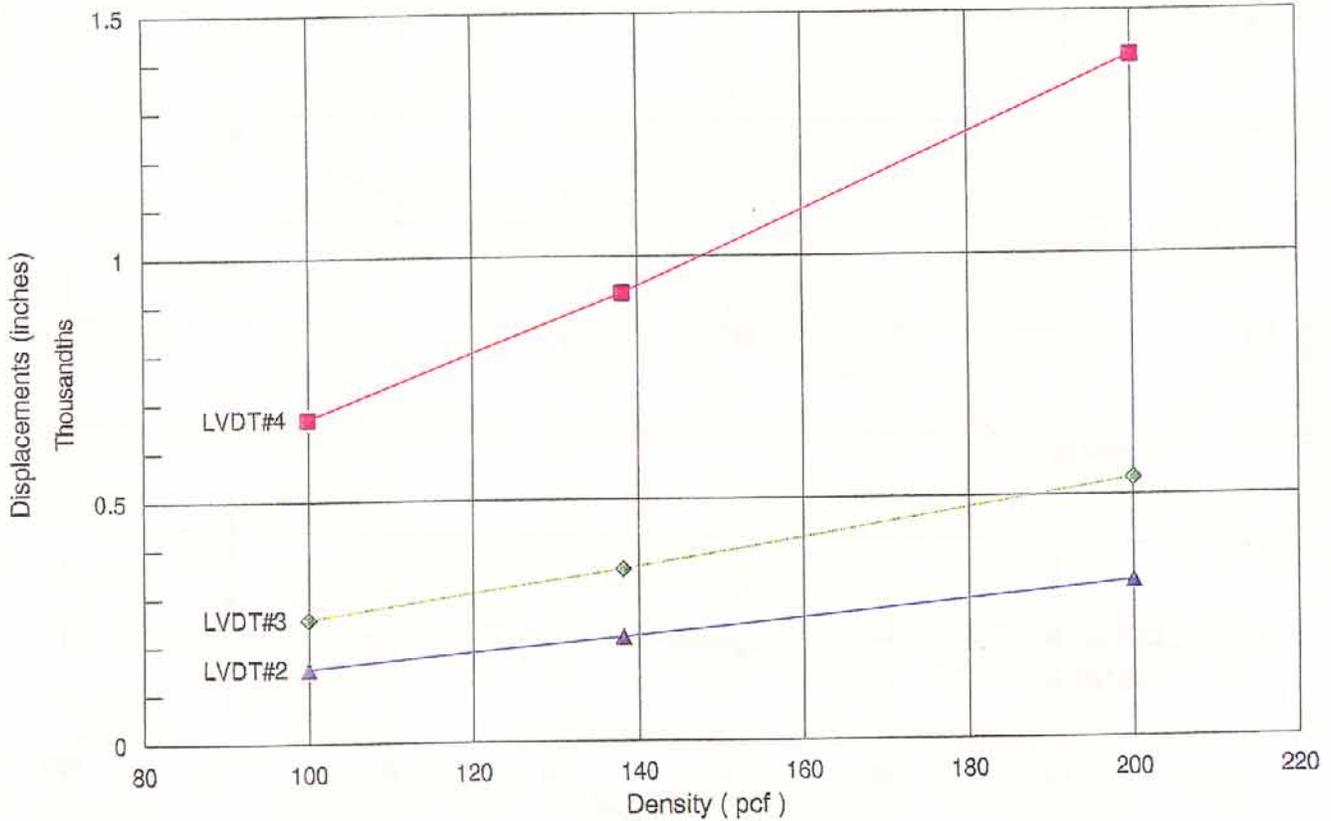
Uncracked Koyna Laboratory Study  
Sensitivity to Variation in Material Density  
Mesh#3

Material Properties

E = 300,000 psi  
Material Density = (100, 138, 200 pcf)

Damping = 3.5% critical  
Rayleigh Damping Factors  
Alpha = 1.954769; Beta = .000248

Peak Displacements  
Material Density Varied



E = 300 ksi

Peak Displacements ( inches )

	100	138.2	200	LAB
LVDT#4	6.7E-04	9.2E-04	1.4E-03	7.2E-04
LVDT#3	2.6E-04	3.6E-04	5.3E-04	3.1E-04
LVDT#2	1.5E-04	2.2E-04	3.2E-04	2.1E-04

Figure g45

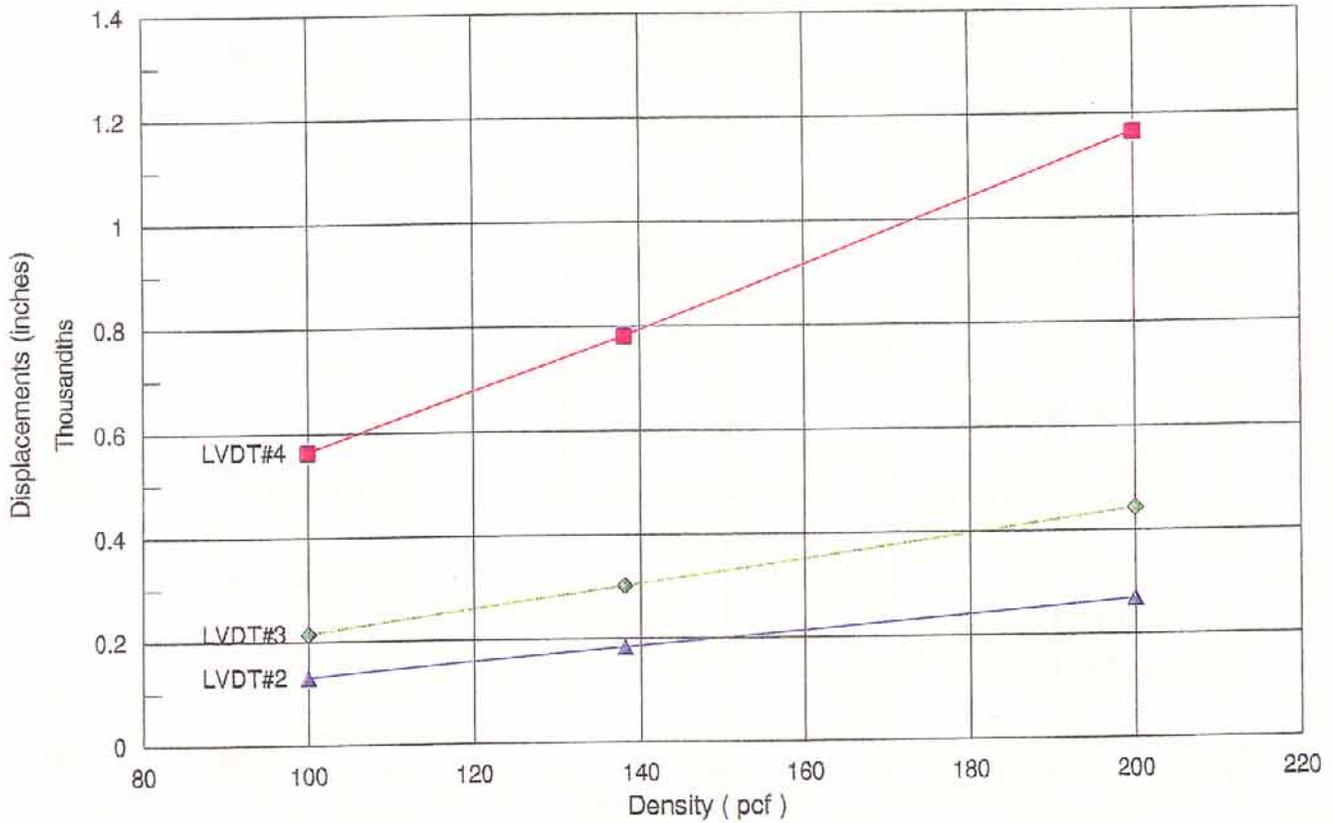
Uncracked Koyna Laboratory Study  
Sensitivity to Variation in Material Density  
Mesh#3

Material Properties

E = 350,000 psi  
Material Density = (100, 138, 200 pcf)

Damping = 3.5% critical  
Rayleigh Damping Factors  
Alpha = 1.954769; Beta = .000248

Peak Displacements  
Material Density Varied



E = 350 ksi

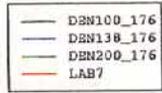
Peak Displacements ( inches )

	100	138.2	200	LAB
LVDT#4	5.6E-04	7.8E-04	1.2E-03	7.2E-04
LVDT#3	2.2E-04	3.0E-04	4.4E-04	3.1E-04
LVDT#2	1.3E-04	1.8E-04	2.7E-04	2.1E-04

Figure g46

# ABAQUS

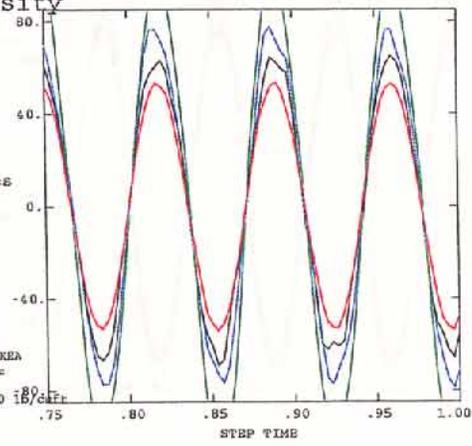
Material Density Varied



Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model  
Acceleration  
at ACCEL#7  
E = 113 ksi

3.5% Critical Damping  
Input Freq=14 Hz File:SHAKEA  
Total Time : 279.75 to 280 sec

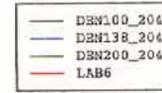
Densities 100, 138, & 200 lb/cu in



ABAQUS Modal Dynamic Analyses vs Laboratory Measurements (LAB)

# ABAQUS

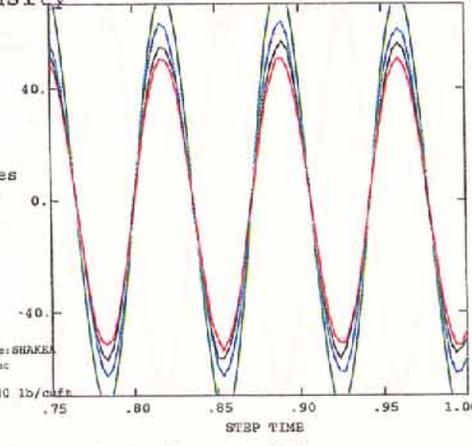
Material Density Varied



Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model  
Acceleration  
at ACCEL#6  
E = 113 ksi

3.5% Critical Damping  
Input Freq=14 Hz Filename:SHAKEA  
Total Time : 279.75 to 280 sec

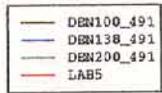
Densities 100, 138, & 200 lb/cu in



ABAQUS Modal Dynamic Analyses vs Laboratory Measurements (LAB)

# ABAQUS

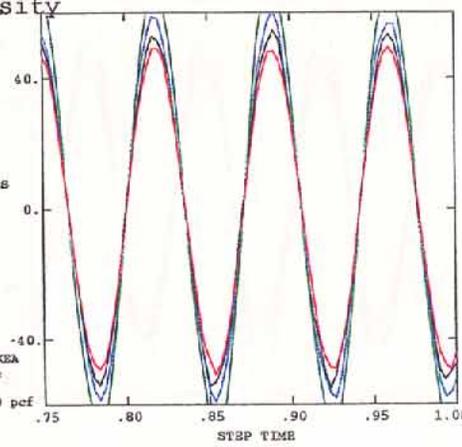
Material Density Varied



Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model  
Acceleration  
at ACCEL#5  
E = 113 ksi

3.5% Critical Damping  
Input Freq=14 Hz File:SHAKEA  
Total Time : 279.75 to 280 sec

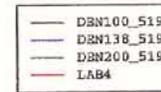
Densities 100, 138, & 200 pcf



ABAQUS Modal Dynamic Analyses vs Laboratory Measurements (LAB)

# ABAQUS

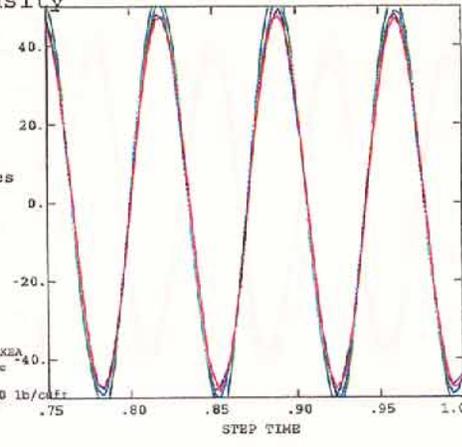
Material Density Varied



Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model  
Acceleration  
at ACCEL#4  
E = 113 ksi

3.5% Critical Damping  
Input Freq=14 Hz File:SHAKEA  
Total Time : 279.75 to 280 sec

Densities 100, 138, & 200 lb/cu ft

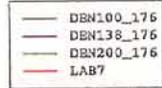


ABAQUS Modal Dynamic Analyses vs Laboratory Measurements (LAB)

Figure g47

# ABAQUS

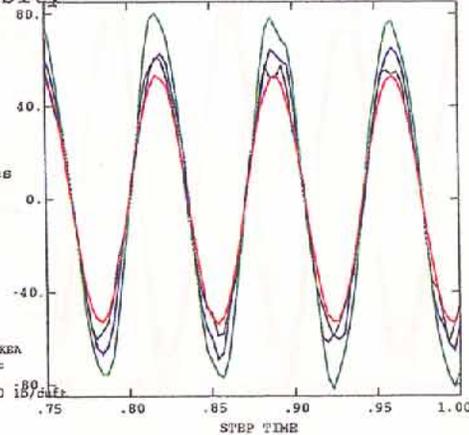
Material Density Varied



Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model  
Acceleration  
at ACCEL#7  
E = 157 ksi

3.5% Critical Damping  
Input Freq=14 Hz File:SHAKEA  
Total Time = 279.75 to 280 sec

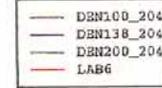
Densitys 100, 138, & 200 lb/cu ft



ABAQUS Modal Dynamic Analyses vs Laboratory Measurements (LAB)

# ABAQUS

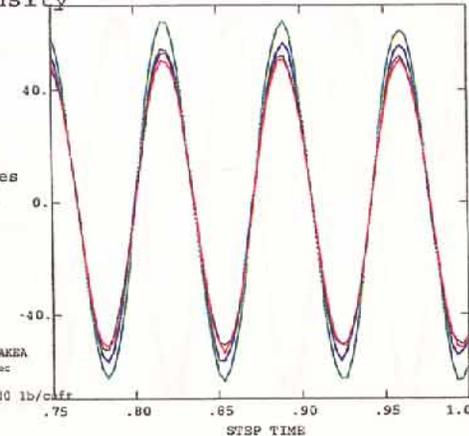
Material Density Varied



Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model  
Acceleration  
at ACCEL#6  
E = 157 ksi

3.5% Critical Damping  
Input Freq=14 Hz File:SHAKEA  
Total Time = 279.75 to 280 sec

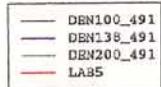
Densitys 100, 138, & 200 lb/cu ft



ABAQUS Modal Dynamic Analyses vs Laboratory Measurements (LAB)

# ABAQUS

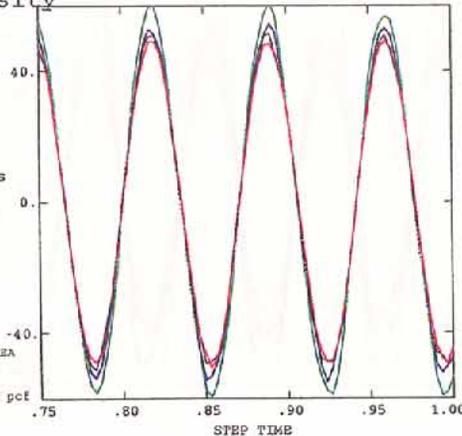
Material Density Varied



Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model  
Acceleration  
at ACCEL#5  
E = 157 psi

3.5% Critical Damping  
Input Freq=14 Hz File:SHAKEA  
Total Time = 279.75 to 280 sec

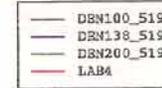
Densitys 100, 138, & 200 pcf



ABAQUS Modal Dynamic Analyses vs Laboratory Measurements (LAB)

# ABAQUS

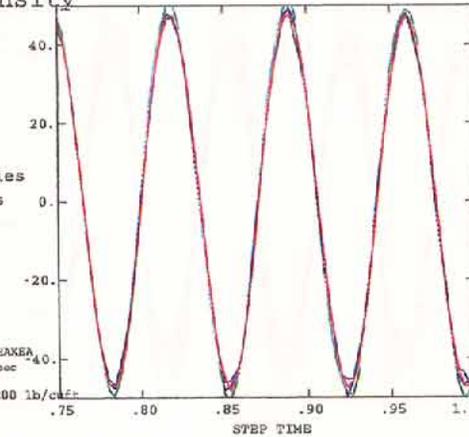
Material Density Varied



Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model  
Acceleration  
at ACCEL#4  
E = 157 ksi

3.5% Critical Damping  
Input Freq=14 Hz File:SHAKEA  
Total Time = 279.75 to 280 sec

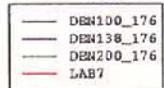
Densitys 100, 138, & 200 lb/cu ft



ABAQUS Modal Dynamic Analyses vs Laboratory Measurements (LAB)

# ABAQUS

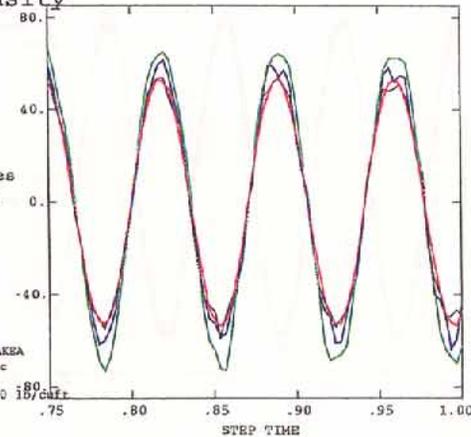
Material Density Varied



Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model  
Acceleration  
at ACCEL#7  
E = 200 ksi

3.5% Critical Damping  
Input Freq=14 Hz File:SHAKEA  
Total Time = 279.75 to 280 sec

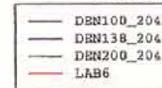
Densitys 100, 138, & 200 lb/cu ft



ABAQUS Modal Dynamic Analyses vs Laboratory Measurements (LAB)

# ABAQUS

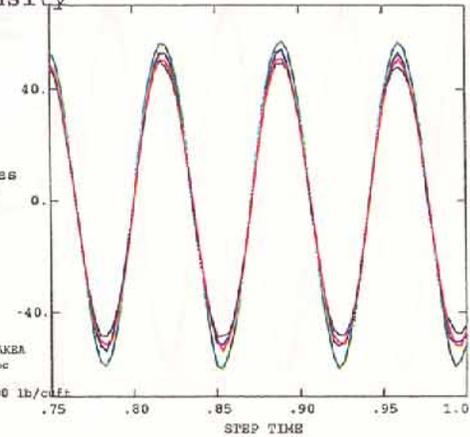
Material Density Varied



Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model  
Acceleration  
at ACCEL#6  
E = 200 ksi

3.5% Critical Damping  
Input Freq=14 Hz File:SHAKEA  
Total Time = 279.75 to 280 sec

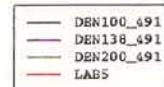
Densitys 100, 138, & 200 lb/cu ft



ABAQUS Modal Dynamic Analyses vs Laboratory Measurements (LAB)

# ABAQUS

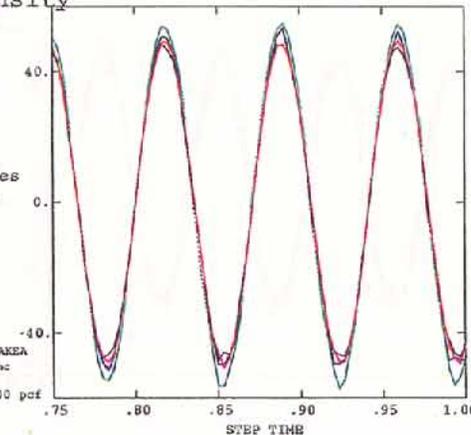
Material Density Varied



Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model  
Acceleration  
at ACCEL#5  
E = 200 ksi

3.5% Critical Damping  
Input Freq=14 Hz File:SHAKEA  
Total Time = 279.75 to 280 sec

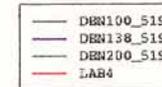
Densitys 100, 138, & 200 pcf



ABAQUS Modal Dynamic Analyses vs Laboratory Measurements (LAB)

# ABAQUS

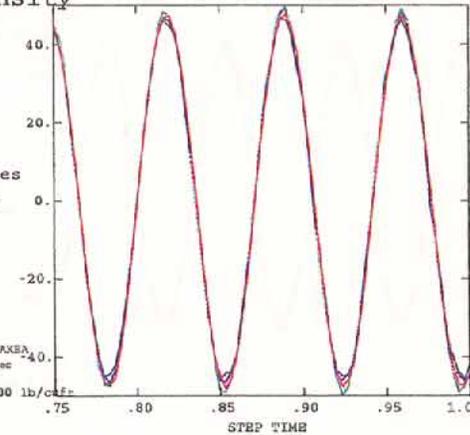
Material Density Varied



Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model  
Acceleration  
at ACCEL#4  
E = 200 ksi

3.5% Critical Damping  
Input Freq=14 Hz File:SHAKEA  
Total Time = 279.75 to 280 sec

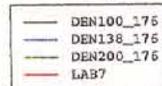
Densitys 100, 138, & 200 lb/cu ft



ABAQUS Modal Dynamic Analyses vs Laboratory Measurements (LAB)

# ABAQUS

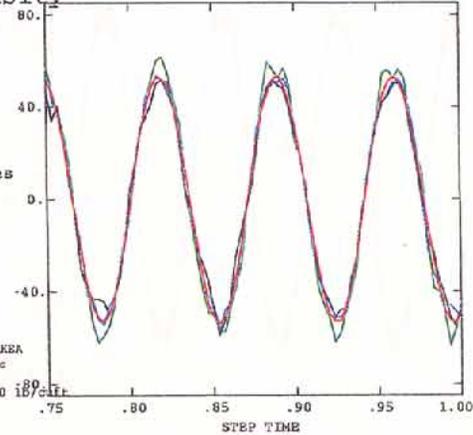
Material Density Varied



Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model  
Acceleration  
at ACCEL#7  
E = 300 ksi

3.5% Critical Damping  
Input Freq=14 Hz File:SHAKEA  
Total Time = 279.75 to 280 sec

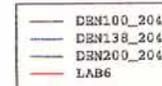
Densities 100, 138, & 200 lb/cuft



ABAQUS Modal Dynamic Analyses vs Laboratory Measurements (LAB)

# ABAQUS

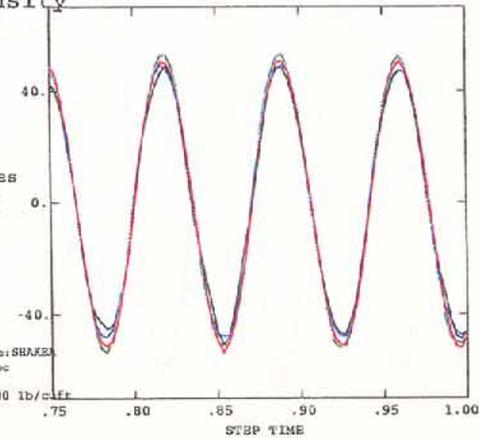
Material Density Varied



Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model  
Acceleration  
at ACCEL#6  
E = 300 ksi

3.5% Critical Damping  
Input Freq=14 Hz Filename:SHAKEA  
Total Time = 279.75 to 280 sec

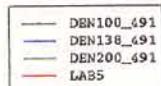
Densities 100, 138, & 200 lb/cuft



ABAQUS Modal Dynamic Analyses vs Laboratory Measurements (LAB)

# ABAQUS

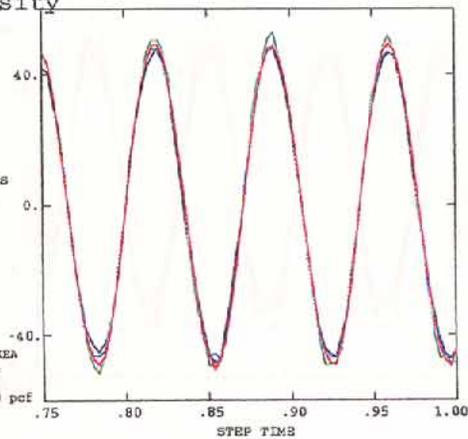
Material Density Varied



Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model  
Acceleration  
at ACCEL#5  
E = 300 ksi

3.5% Critical Damping  
Input Freq=14 Hz File:SHAKEA  
Total Time = 279.75 to 280 sec

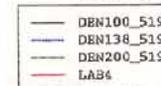
Densities 100, 138, & 200 pcf



ABAQUS Modal Dynamic Analyses vs Laboratory Measurements (LAB)

# ABAQUS

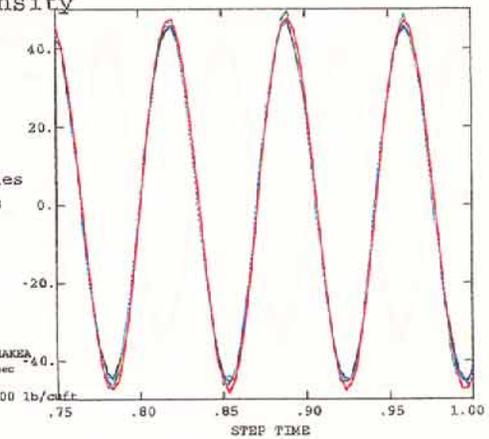
Material Density Varied



Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model  
Acceleration  
at ACCEL#4  
E = 300 ksi

3.5% Critical Damping  
Input Freq=14 Hz File:SHAKEA  
Total Time = 279.75 to 280 sec

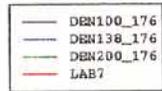
Densities 100, 138, & 200 lb/cuft



ABAQUS Modal Dynamic Analyses vs Laboratory Measurements (LAB)

# ABAQUS

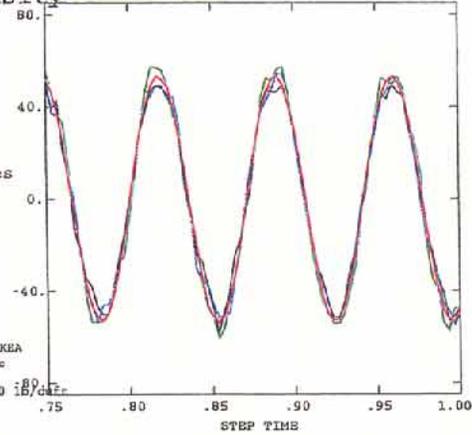
Material Density Varied



Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model  
Acceleration  
at ACCEL#7  
E = 350 ksi

3.5% Critical Damping  
Input Freq=14 Hz File:SHAKEA  
Total Time : 279.75 to 280 sec

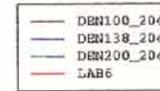
Densities 100, 138, & 200 lb/cu ft



ABAQUS Modal Dynamic Analyses vs Laboratory Measurements (LAB)

# ABAQUS

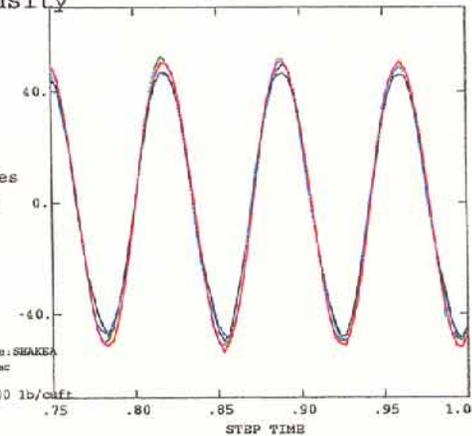
Material Density Varied



Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model  
Acceleration  
at ACCEL#6  
E = 350 ksi

3.5% Critical Damping  
Input Freq=14 Hz Filename:SHAKEA  
Total Time : 279.75 to 280 sec

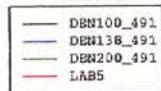
Densities 100, 138, & 200 lb/cu ft



ABAQUS Modal Dynamic Analyses vs Laboratory Measurements (LAB)

# ABAQUS

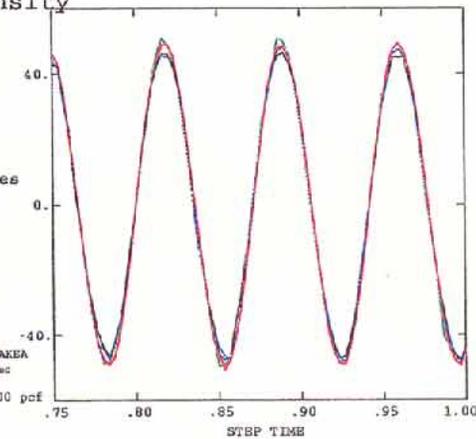
Material Density Varied



Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model  
Acceleration  
at ACCEL#5  
E = 350 ksi

3.5% Critical Damping  
Input Freq=14 Hz File:SHAKEA  
Total Time : 279.75 to 280 sec

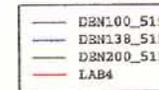
Densities 100, 138, & 200 pcf



ABAQUS Modal Dynamic Analyses vs Laboratory Measurements (LAB)

# ABAQUS

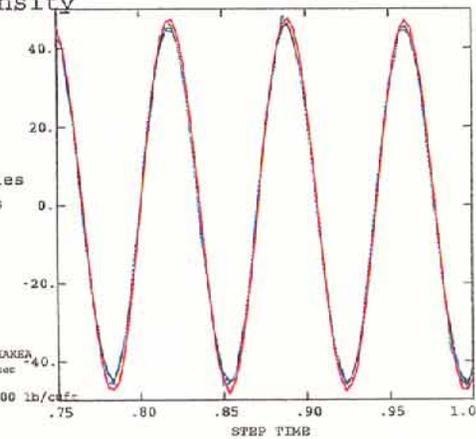
Material Density Varied



Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model  
Acceleration  
at ACCEL#4  
E = 350 ksi

3.5% Critical Damping  
Input Freq=14 Hz File:SHAKEA  
Total Time : 279.75 to 280 sec

Densities 100, 138, & 200 lb/cu ft



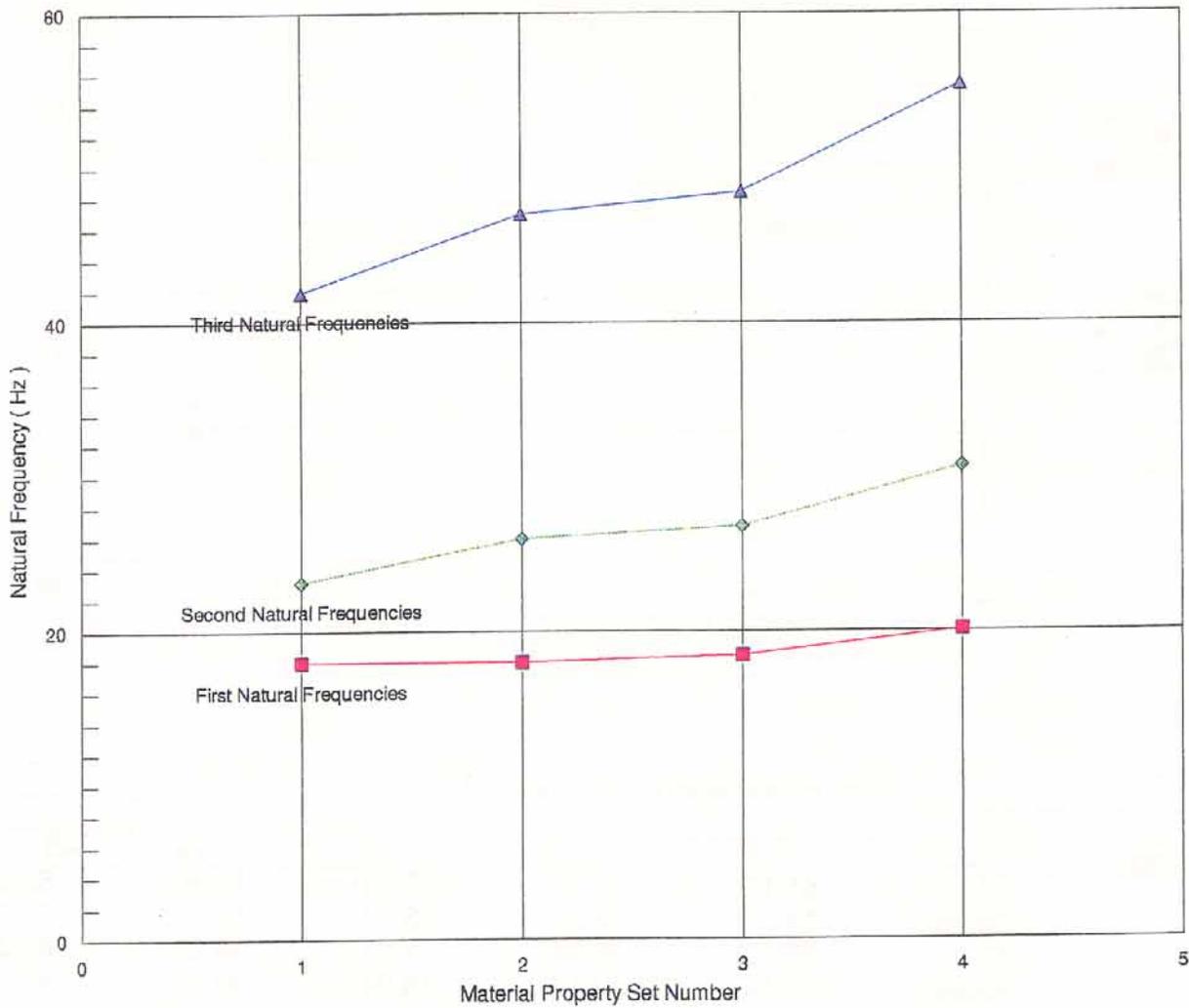
ABAQUS Modal Dynamic Analyses vs Laboratory Measurements (LAB)

Uncracked Koyna Laboratory Study  
Sensitivity to Variation in Percent Critical Damping  
Mesh#3

Material Property Sets

Linear Elastic Material Property Set #1 : Elastic Modulus = 190 ksi; Material Density = 133 pcf  
 Linear Elastic Material Property Set #2 : Elastic Modulus = 200 ksi; Material Density = 140 pcf  
 Linear Elastic Material Property Set #3 : Elastic Modulus = 210 ksi; Material Density = 140 pcf  
 Linear Elastic Material Property Set #4 : Elastic Modulus = 250 ksi; Material Density = 140 pcf

**Natural Frequencies**  
For Material Property Sets #1-#4



Natural Frequencies (Hz)

Material Property Set #	1	2	3	4	LAB
Mode 1	18.0	18.0	18.4	20.1	18.0
Mode 2	23.2	26.0	26.8	30.6	24.0
Mode 3	41.9	47.0	48.4	55.4	30.0

Figure h1

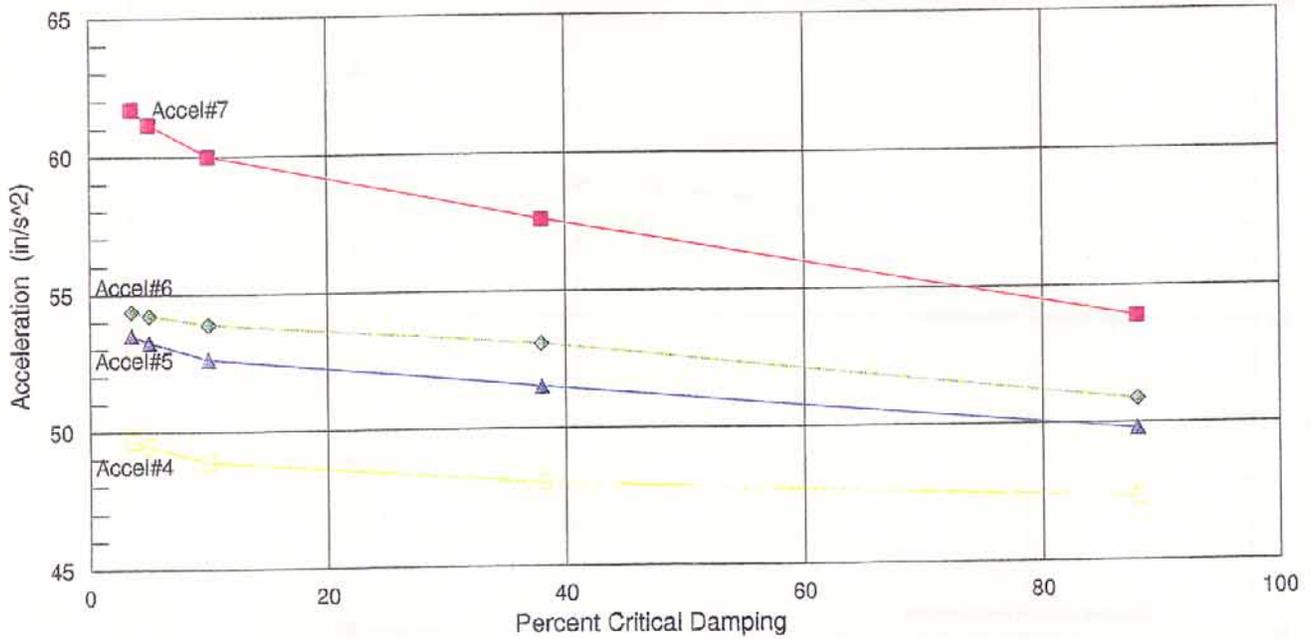
Uncracked Koyna Laboratory Study  
Sensitivity to Variation in Percent Critical Damping

Mesh#3

Modal Damping = ( 3.5%, 5%, 10%, 38% & 88% ) critical

Linear Elastic Material Property Set #1 : Elastic Modulus = 190 ksi; Material Density = 133 pcf

**Peak Accelerations**  
Percent Critical Damping Varied



Peak Accelerations ( inch / sec ^ 2 )

Percent Damping	3.5	5	10	38	88	LAB
Accel#7	61.73	61.17	59.99	57.60	53.90	53.26
Accel#6	54.39	54.23	53.88	53.07	50.87	51.72
Accel#5	53.52	53.25	52.61	51.53	49.80	49.26
Accel#4	49.66	49.44	48.87	48.04	47.32	47.72
CPU seconds	278.83	278.65	278.89	268.59	267.18	

Figure h2

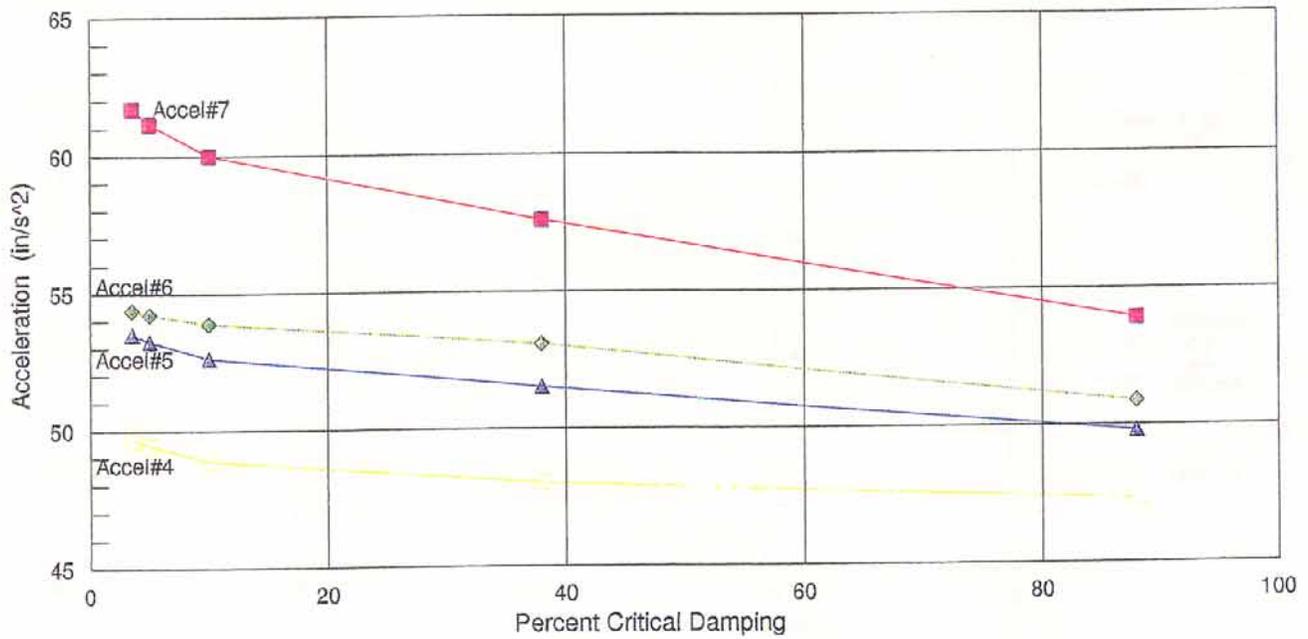
Uncracked Koyna Laboratory Study  
Sensitivity to Variation in Percent Critical Damping

Mesh#3

Modal Damping = ( 3.5%, 5%, 10%, 38%, & 88% ) critical

Linear Elastic Material Property Set #2 : Elastic Modulus = 200 ksi; Material Density = 140 pcf

**Peak Accelerations**  
Percent Critical Damping Varied



Peak Accelerations ( inch / sec ^ 2 )

Percent Damping	3.5	5	10	38	88	LAB
Accel#7	61.73	61.17	59.99	57.60	53.90	53.26
Accel#6	54.39	54.23	53.88	53.07	50.87	51.72
Accel#5	53.52	53.25	52.61	51.53	49.80	49.26
Accel#4	49.66	49.44	48.87	48.04	47.34	47.72

Figure h3

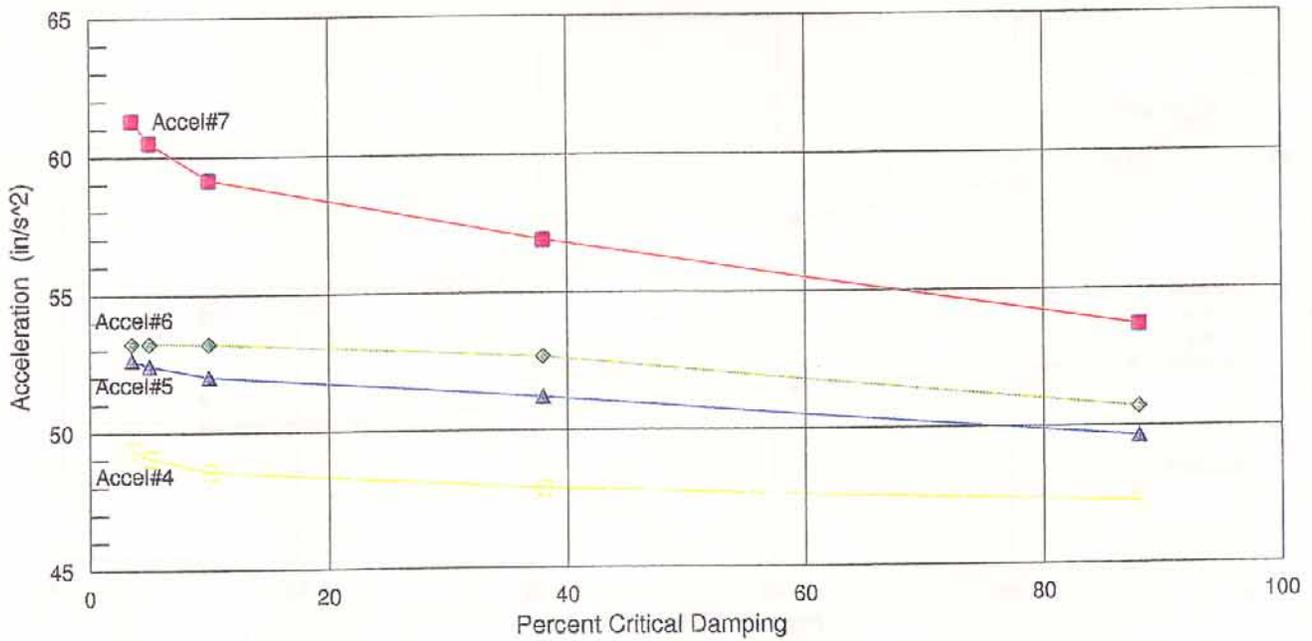
Uncracked Koyna Laboratory Study  
Sensitivity to Variation in Percent Critical Damping

Mesh#3

Modal Damping = (3.5%,5%,10%,38%,&88%) critical

Linear Elastic Material Property Set #3 : Elastic Modulus = 210 ksi; Material Density = 140 pcf

**Peak Accelerations**  
Percent Critical Damping Varied



Peak Accelerations ( inch / sec ^ 2 )

Percent Damping	3.5	5	10	38	88	LAB
Accel#7	61.31	60.51	59.15	56.91	53.68	53.26
Accel#6	53.22	53.23	53.21	52.67	50.70	51.72
Accel#5	52.65	52.43	52.02	51.21	49.65	49.26
Accel#4	49.36	49.06	48.57	47.90	47.27	47.72

Figure h4

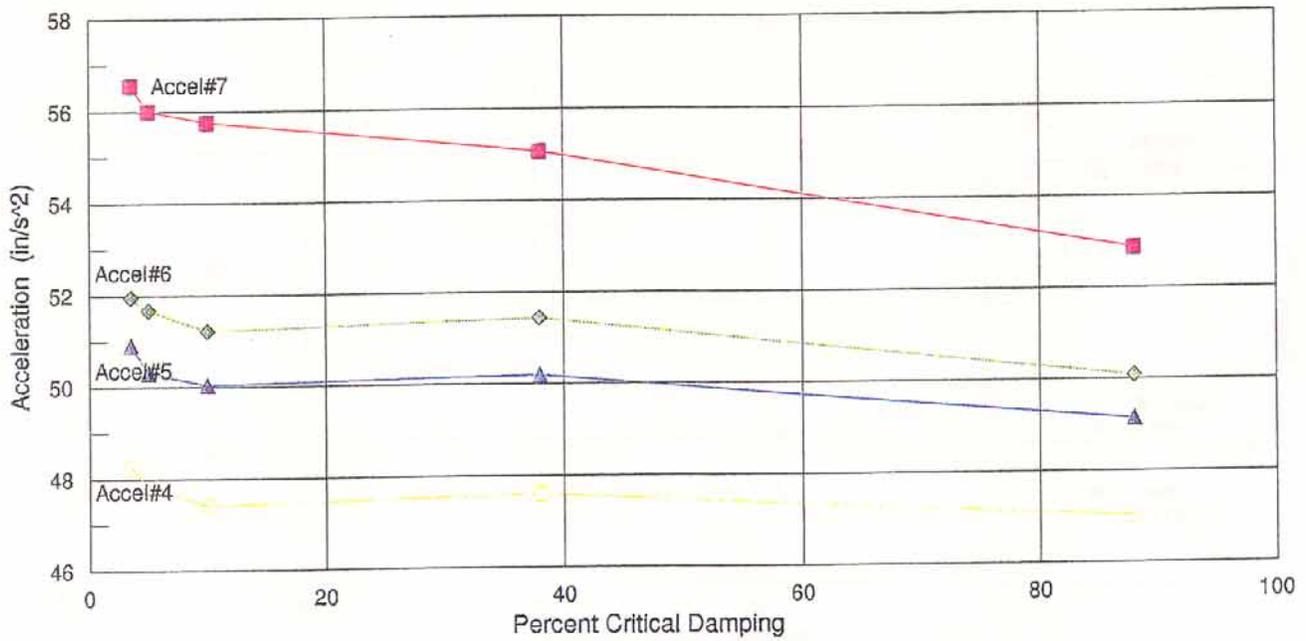
Uncracked Koyna Laboratory Study  
Sensitivity to Variation in Percent Critical Damping

Mesh#3

Modal Damping = ( 3.5%, 5%, 10%, 38% & 88% ) critical

Linear Elastic Material Property Set #4 : Elastic Modulus = 250 ksi; Material Density = 140 pcf

**Peak Accelerations**  
Percent Critical Damping Varied



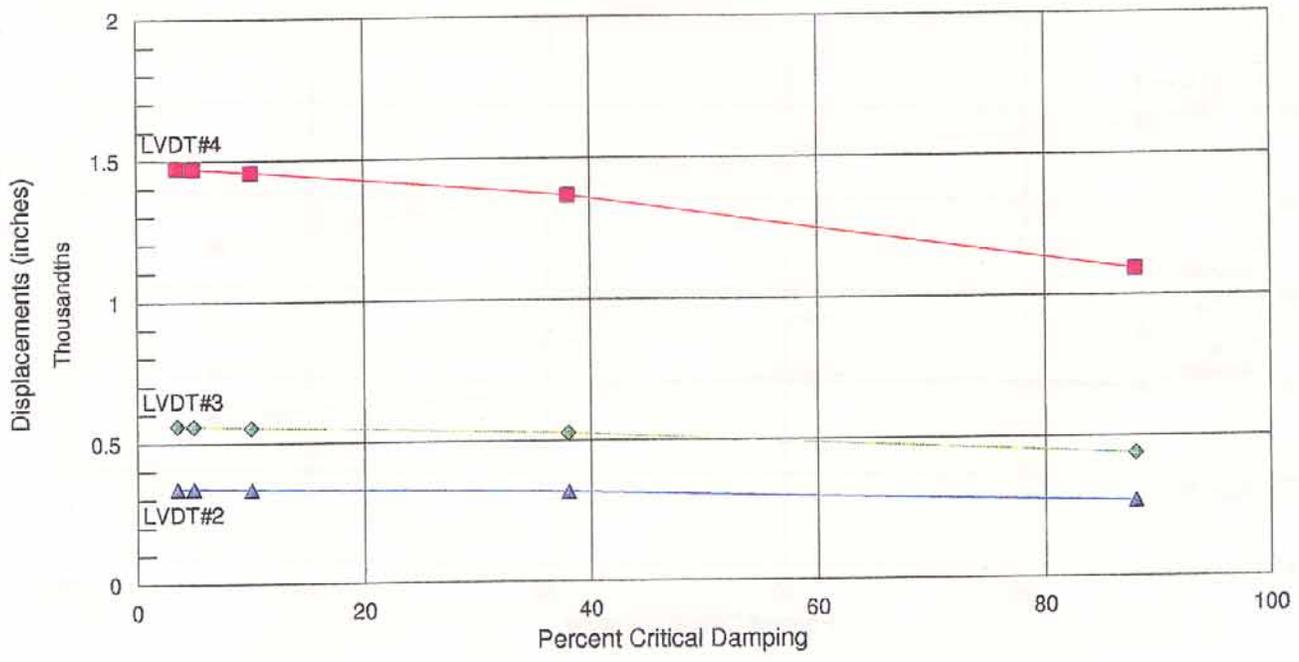
Peak Accelerations ( inch / sec ^ 2 )

Percent Damping	3.5	5	10	38	88	LAB
Accel#7	56.56	56.01	55.76	55.07	52.87	53.26
Accel#6	51.95	51.67	51.22	51.43	50.09	51.72
Accel#5	50.90	50.30	50.04	50.19	49.14	49.26
Accel#4	48.26	47.84	47.41	47.60	47.03	47.72

Uncracked Koyna Laboratory Study  
 Sensitivity to Variation in Percent Critical Damping  
 Mesh#3  
 Modal Damping = (3.5%,5%,10%,38%,&88%) critical

Linear Elastic Material Property Set #1 : Elastic Modulus = 190 ksi; Material Density = 133 pcf

**Peak Displacements**  
 Percent Critical Damping Varied



Peak Displacements ( inches )

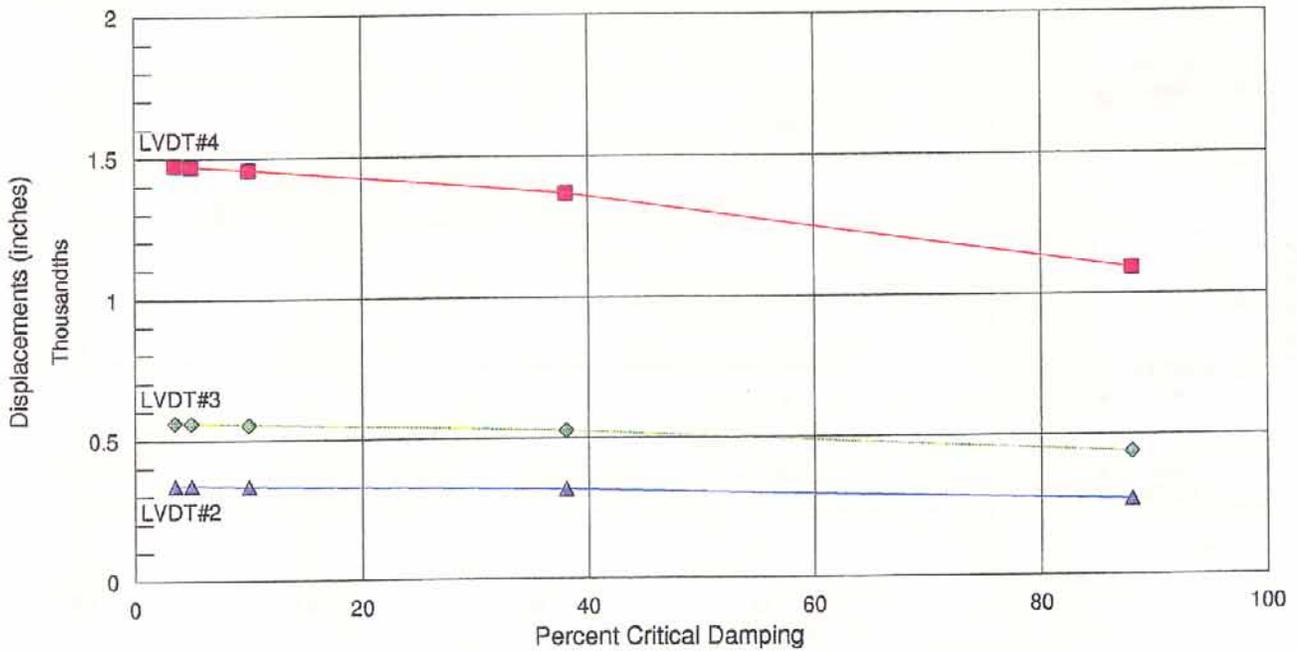
Percent Damping	3.5	5	10	38	88	LAB
LVDT#4	1.5E-03	1.5E-03	1.5E-03	1.4E-03	1.1E-03	7.8E-04
LVDT#3	5.6E-04	5.6E-04	5.5E-04	5.3E-04	4.4E-04	3.0E-04
LVDT#2	3.4E-04	3.4E-04	3.3E-04	3.2E-04	2.7E-04	1.8E-04
CPU seconds	278.83	278.65	278.89	268.59	267.18	

Figure h6

Uncracked Koyna Laboratory Study  
 Sensitivity to Variation in Percent Critical Damping  
 Mesh#3  
 Modal Damping = (3.5%,5%,10%,38%,&88%) critical

Linear Elastic Material Property Set #2 : Elastic Modulus = 200 ksi; Material Density = 140 pcf

**Peak Displacements**  
 Percent Critical Damping Varied



Peak Displacements ( inches )

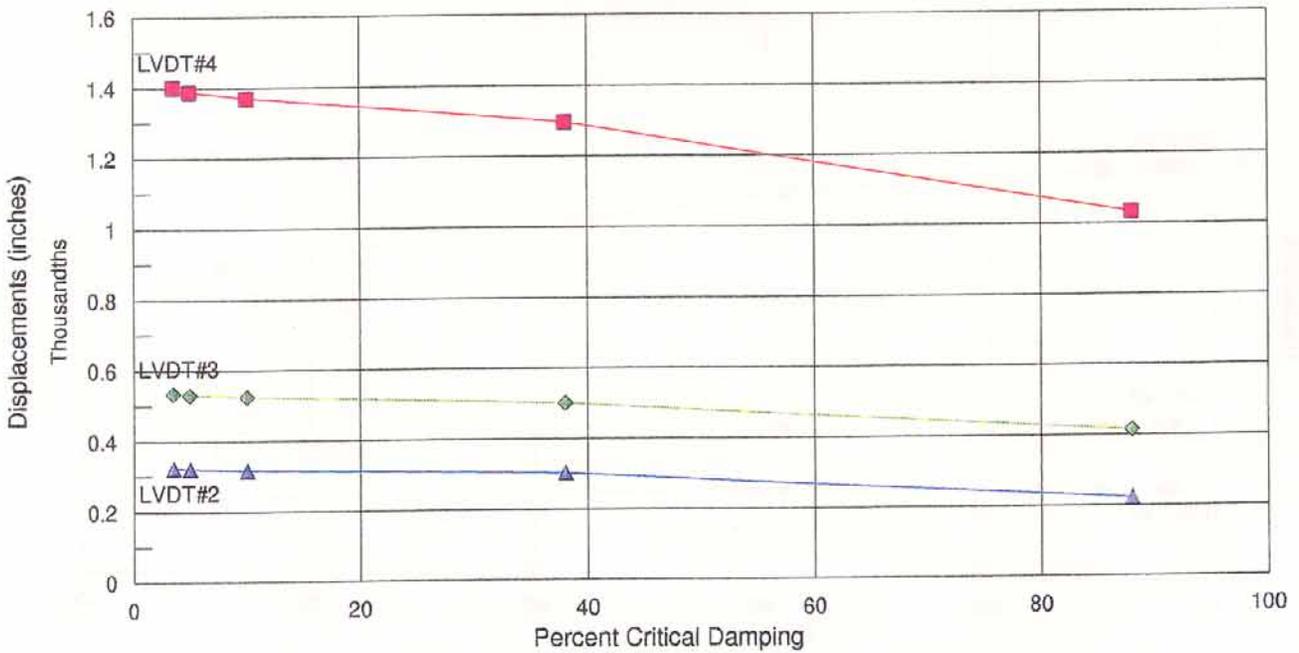
Percent Damping	3.5	5	10	38	88	LAB
LVDT#4	1.5E-03	1.5E-03	1.5E-03	1.4E-03	1.1E-03	7.8E-04
LVDT#3	5.6E-04	5.6E-04	5.5E-04	5.3E-04	4.4E-04	3.0E-04
LVDT#2	3.4E-04	3.4E-04	3.3E-04	3.2E-04	2.7E-04	1.8E-04

Figure h7

Uncracked Koyna Laboratory Study  
Sensitivity to Variation in Percent Critical Damping  
Mesh#3  
Modal Damping = (3.5%,5%,10%,38%,&88%) critical

Linear Elastic Material Property Set #3 : Elastic Modulus = 210 ksi; Material Density = 140 pcf

**Peak Displacements**  
Percent Critical Damping Varied



Peak Displacements ( inches )

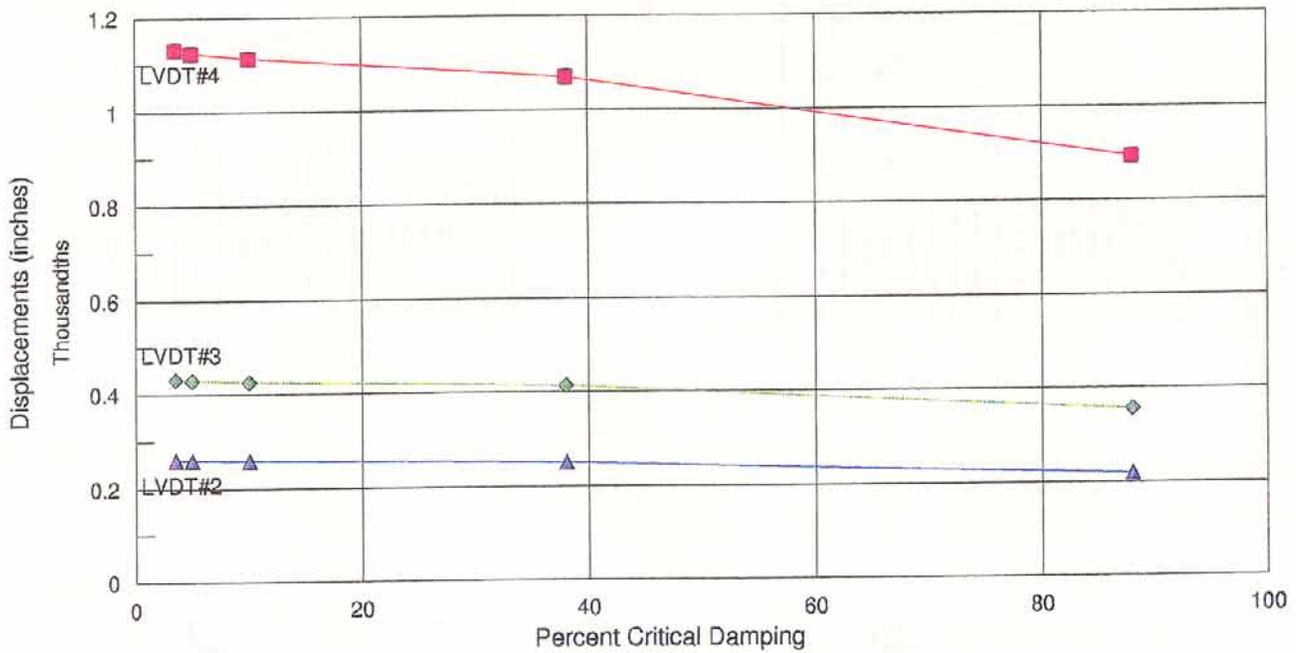
Percent Damping	3.5	5	10	38	88	LAB
LVDT#4	1.4E-03	1.4E-03	1.4E-03	1.3E-03	1.0E-03	7.8E-04
LVDT#3	5.3E-04	5.3E-04	5.2E-04	5.0E-04	4.1E-04	3.0E-04
LVDT#2	3.2E-04	3.2E-04	3.2E-04	3.0E-04	2.2E-04	1.8E-04

Figure h8

Uncracked Koyna Laboratory Study  
Sensitivity to Variation in Percent Critical Damping  
Mesh#3  
Modal Damping = (3.5%,5%,10%,38%,&88%) critical

Linear Elastic Material Property Set #4 : Elastic Modulus = 250 ksi; Material Density = 140 pcf

**Peak Displacements**  
Percent Critical Damping Varied



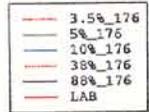
Peak Displacements ( inches )

Percent Damping	3.5	5	10	38	88	LAB
LVDT#4	1.1E-03	1.1E-03	1.1E-03	1.1E-03	8.9E-04	7.8E-04
LVDT#3	4.3E-04	4.3E-04	4.3E-04	4.1E-04	3.6E-04	3.0E-04
LVDT#2	2.6E-04	2.6E-04	2.6E-04	2.5E-04	2.2E-04	1.8E-04

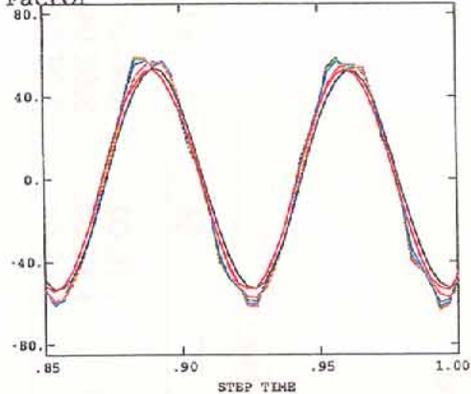
Figure h9

# ABAQUS

Modal Damping Factor Varied



Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model  
Acceleration  
at ACCEL#7  
Elastic Modulus = 190 ksi  
Material Density = 133 pcf  
Filename=SHAKEA  
Total Time = .27975 to .282 sec



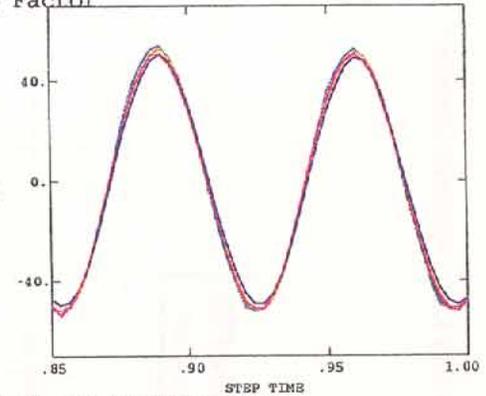
ABAQUS Modal Dynamic Analyses vs Laboratory Measurements

# ABAQUS

Modal Damping Factor Varied



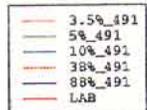
Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model  
Acceleration  
at ACCEL#6  
Material Density = 133 pcf  
Elastic Modulus = 190 ksi  
Filename=SHAKEA  
Total Time = .27975 to .282 sec



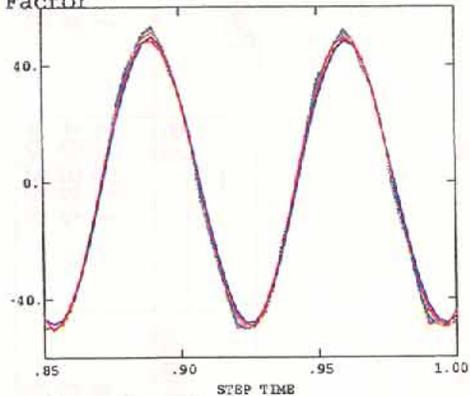
ABAQUS Modal Dynamic Analyses vs Laboratory Measurements

# ABAQUS

Modal Damping Factor Varied



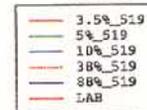
Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model  
Acceleration  
at ACCEL#5  
Elastic Modulus = 190 ksi  
Material Density = 133 pcf  
Filename=SHAKEA  
Total Time = .27975 to .282 sec



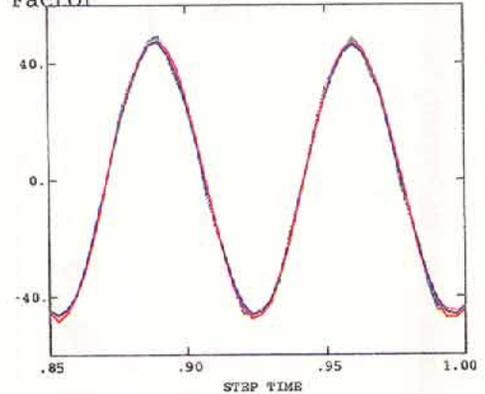
ABAQUS Modal Dynamic Analyses vs Laboratory Measurements

# ABAQUS

Modal Damping Factor Varied



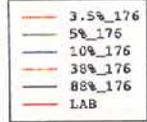
Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model  
Acceleration  
at ACCEL#4  
Elastic Modulus = 190 ksi  
Material Density = 133 pcf  
Filename=SHAKEA  
Total Time = .27975 to .282 sec



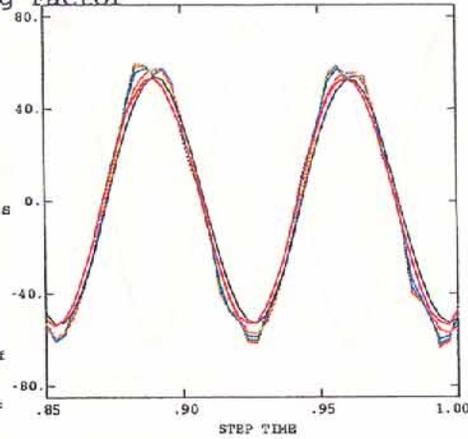
ABAQUS Modal Dynamic Analyses vs Laboratory Measurements

# ABAQUS

Modal Damping Factor  
Varied



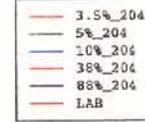
Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model  
Acceleration  
at ACCEL#7  
Elastic Modulus = 200 ksi  
Material Density = 140 pcf  
Filename: SHAKEA  
Total Time = 279.75 to 280 sec



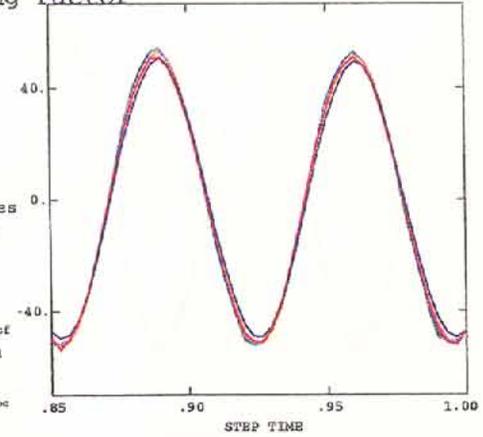
ABAQUS Modal Dynamic Analyses vs Laboratory Measurements

# ABAQUS

Modal Damping Factor  
Varied



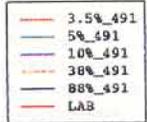
Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model  
Acceleration  
at ACCEL#6  
Material Density = 140 pcf  
Elastic Modulus = 200 ksi  
Filename: SHAKEA  
Total Time = 279.75 to 280 sec



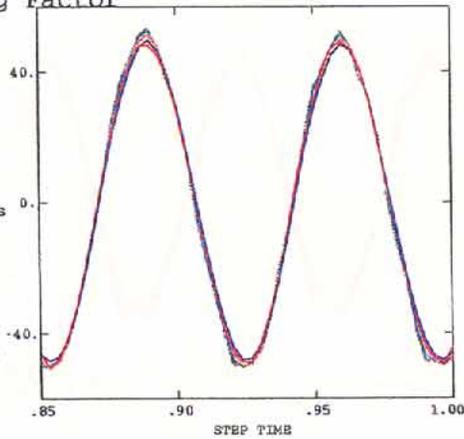
ABAQUS Modal Dynamic Analyses vs Laboratory Measurements

# ABAQUS

Modal Damping Factor  
Varied



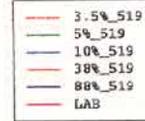
Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model  
Acceleration  
at ACCEL#5  
Elastic Modulus = 200 ksi  
Material Density = 140 pcf  
Filename: SHAKEA  
Total Time = 279.75 to 280 sec



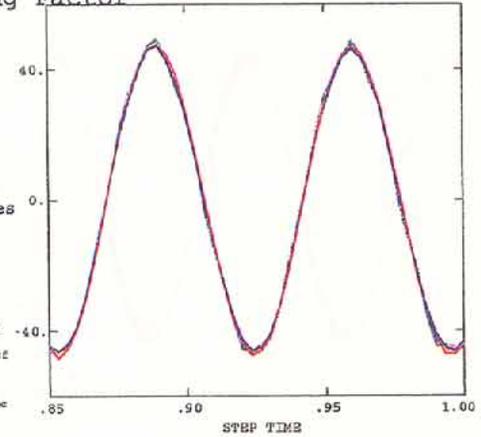
ABAQUS Modal Dynamic Analyses vs Laboratory Measurements

# ABAQUS

Modal Damping Factor  
Varied



Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model  
Acceleration  
at ACCEL#4  
Elastic Modulus = 200 ksi  
Material Density = 140 pcf  
Filename: SHAKEA  
Total Time = 279.75 to 280 sec

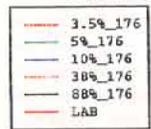


ABAQUS Modal Dynamic Analyses vs Laboratory Measurements

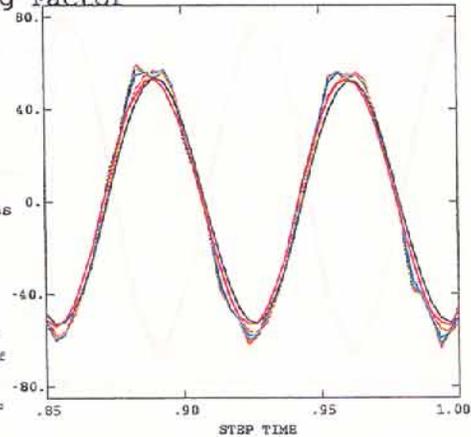
Figure h11

# ABAQUS

## Modal Damping Factor Varied



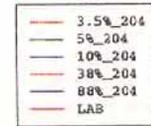
Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model  
Acceleration  
at ACCEL#7  
Elastic Modulus = 210 ksi  
Material Density = 140 pcf  
Filename: SHAKEA  
Total Time : 279.75 to 280 sec



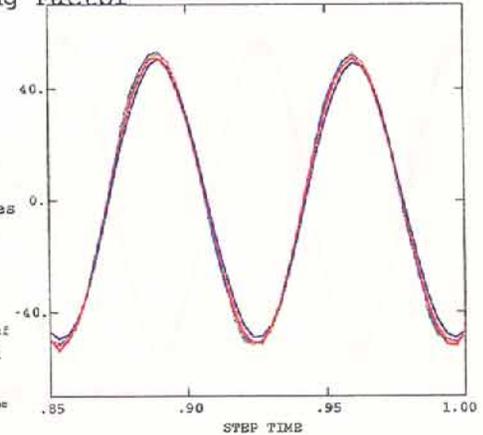
ABAQUS Modal Dynamic Analyses vs Laboratory Measurements

# ABAQUS

## Modal Damping Factor Varied



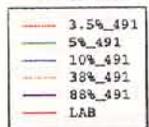
Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model  
Acceleration  
at ACCEL#6  
Material Density = 140 pcf  
Elastic Modulus = 210 ksi  
Filename: SHAKEA  
Total Time : 279.75 to 280 sec



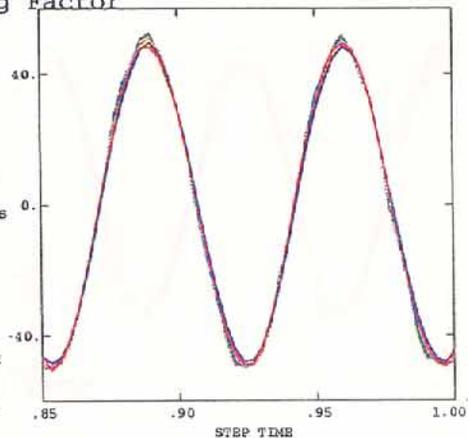
ABAQUS Modal Dynamic Analyses vs Laboratory Measurements

# ABAQUS

## Modal Damping Factor Varied



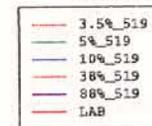
Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model  
Acceleration  
at ACCEL#5  
Elastic Modulus = 210 ksi  
Material Density = 140 pcf  
Filename: SHAKEA  
Total Time : 279.75 to 280 sec



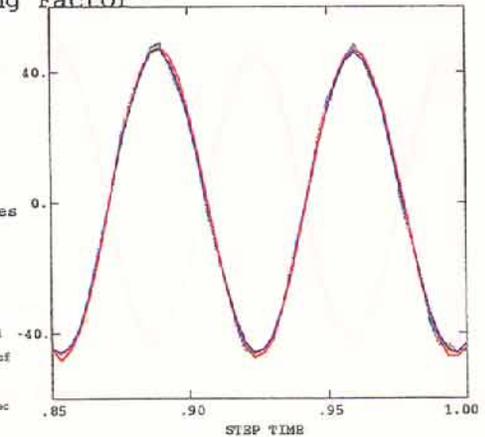
ABAQUS Modal Dynamic Analyses vs Laboratory Measurements

# ABAQUS

## Modal Damping Factor Varied



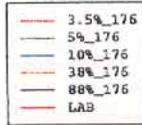
Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model  
Acceleration  
at ACCEL#4  
Elastic Modulus = 210 ksi  
Material Density = 140 pcf  
Filename: SHAKEA  
Total Time : 279.75 to 280 sec



ABAQUS Modal Dynamic Analyses vs Laboratory Measurements

# ABAQUS

Modal Damping Factor  
Varied

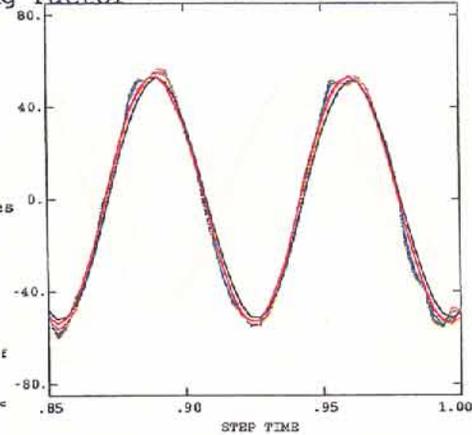


Linear Elastic  
Material Properties  
STANDARD Analyses

Uncracked Model  
Acceleration  
at ACCEL#7

Elastic Modulus = 250 ksi  
Material Density = 140 pcf  
Filename: SHAKEA

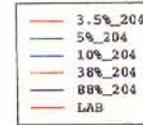
Total Time : 279.75 to 280 sec



ABAQUS Modal Dynamic Analyses vs Laboratory Measurements

# ABAQUS

Modal Damping Factor  
Varied

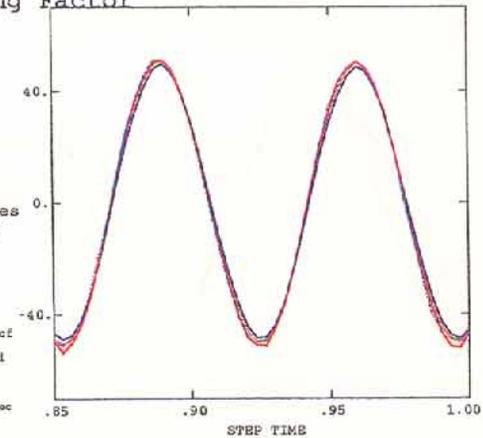


Linear Elastic  
Material Properties  
STANDARD Analyses

Uncracked Model  
Acceleration  
at ACCEL#6

Material Density = 140 pcf  
Elastic Modulus = 250 ksi  
Filename: SHAKEA

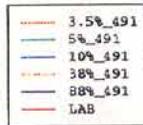
Total Time : 279.75 to 280 sec



ABAQUS Modal Dynamic Analyses vs Laboratory Measurements

# ABAQUS

Modal Damping Factor  
Varied

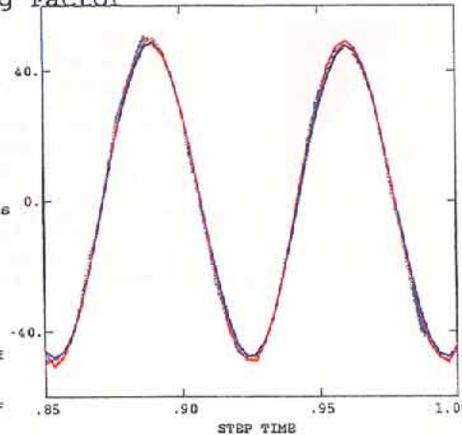


Linear Elastic  
Material Properties  
STANDARD Analyses

Uncracked Model  
Acceleration  
at ACCEL#5

Elastic Modulus = 250 ksi  
Material Density = 140 pcf  
Filename: SHAKEA

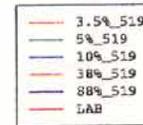
Total Time : 279.75 to 280 sec



ABAQUS Modal Dynamic Analyses vs Laboratory Measurements

# ABAQUS

Modal Damping Factor  
Varied

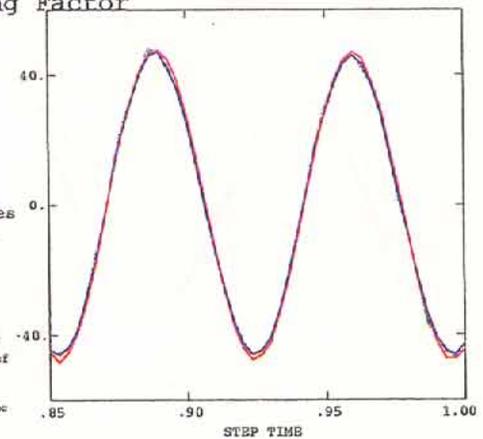


Linear Elastic  
Material Properties  
STANDARD Analyses

Uncracked Model  
Acceleration  
at ACCEL#4

Elastic Modulus = 250 ksi  
Material Density = 140 pcf  
Filename: SHAKEA

Total Time : 279.75 to 280 sec



ABAQUS Modal Dynamic Analyses vs Laboratory Measurements

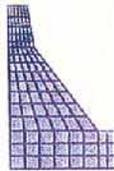
Figure h13

# ABAQUS

Koyna Laboratory Model Study  
 Uncracked Model Study  
 Sensitivity Study  
 Variation of Modal Damping

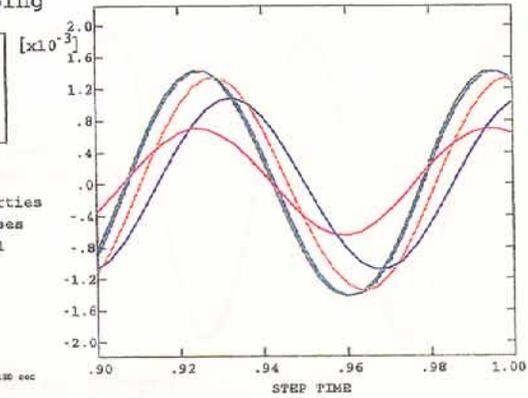
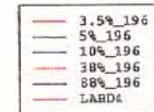
Comparison of Displacements  
 ABAQUS STANDARD  
 Modal Dynamic Analysis

Input Record SHAK6A  
 Elastic Modulus = 190 ksi  
 Density = 133.0 pcf  
 Mesh # 3



# ABAQUS

Modal Damping



Total Time = 279.90 to 280 sec

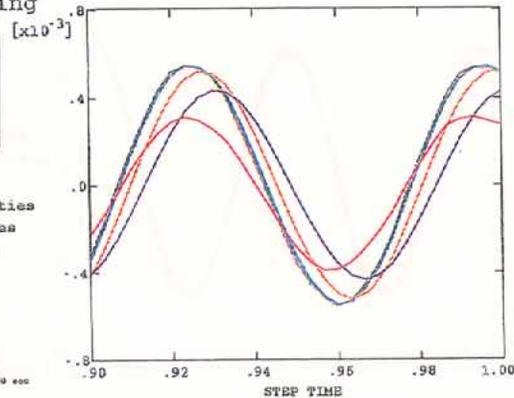
ABAQUS Modal Dynamic Analyses & Laboratory Measurements

# ABAQUS

Modal Damping



Linear Elastic  
 Material Properties  
 STANDARD Analyses  
 Uncracked Model  
 Displacement  
 at LVDT#3

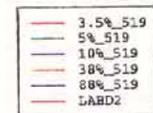


Total Time = 279.90 to 280 sec

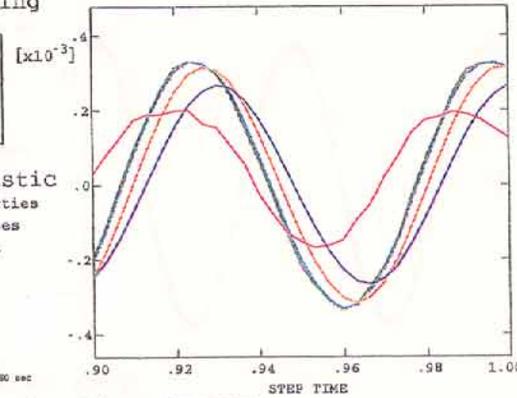
ABAQUS Modal Dynamic Analyses & Laboratory Measurements

# ABAQUS

Modal Damping



Linear Elastic  
 Material Properties  
 STANDARD Analyses  
 Uncracked Model  
 Acceleration  
 at LVDT#2



Total Time = 279.90 to 280 sec

ABAQUS Modal Dynamic Analyses & Laboratory Measurements

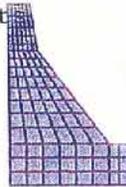
Figure h14

# ABAQUS

Koyna Laboratory Model Study  
 Uncracked Model Study  
 Sensitivity Study  
 Variation of Modal Damping

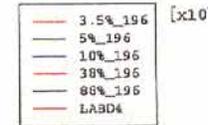
Comparison of Displacement  
 ABAQUS STANDARD  
 Modal Dynamic Analysis

Input Record SHAKEA  
 Elastic Modulus = 200 ksi  
 Density = 140.0 pcf  
 Mesh # 3

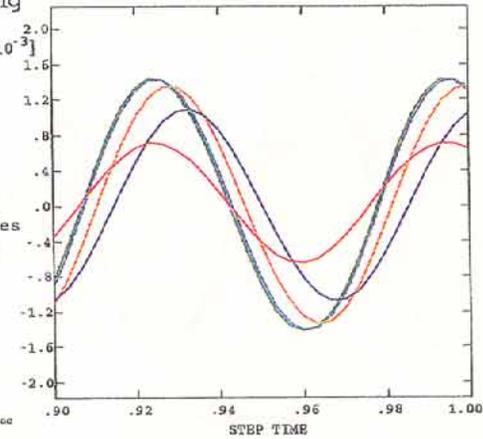


# ABAQUS

Modal Damping



Linear Elastic  
 Material Properties  
 STANDARD Analyses  
 Uncracked Model  
 Displacement  
 at LVDT#4

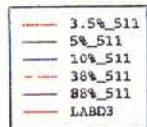


Total Time = 279.90 to 280 sec

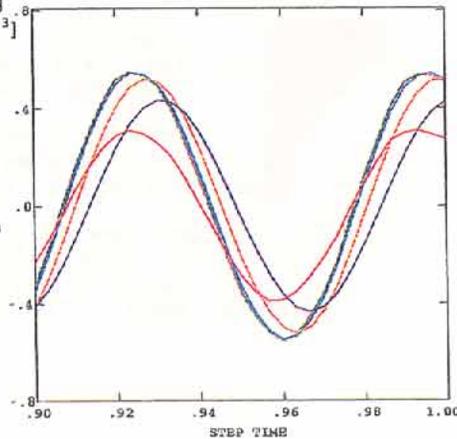
ABAQUS Modal Dynamic Analyses & Laboratory Measurements

# ABAQUS

Modal Damping



Linear Elastic  
 Material Properties  
 STANDARD Analyses  
 Uncracked Model  
 Displacement  
 at LVDT#3

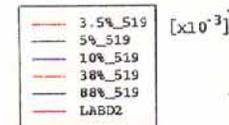


Total Time = 279.90 to 280 sec

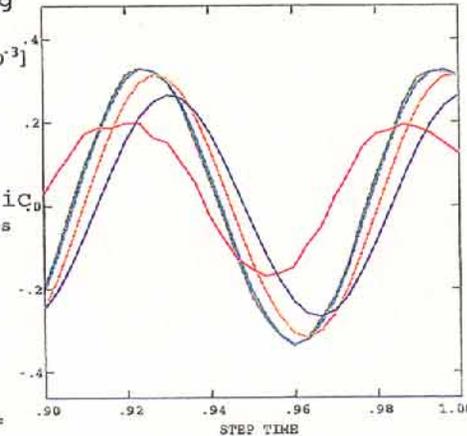
ABAQUS Modal Dynamic Analyses & Laboratory Measurements

# ABAQUS

Modal Damping



Linear Elastic  
 Material Properties  
 STANDARD Analyses  
 Uncracked Model  
 Acceleration  
 at LVDT#2



Total Time = 279.90 to 280 sec

ABAQUS Modal Dynamic Analyses & Laboratory Measurements

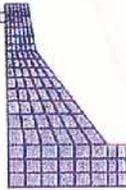
Figure h15

# ABAQUS

Koyna Laboratory Model Study  
 Uncracked Model Study  
 Sensitivity Study  
 Variation of Modal Damping

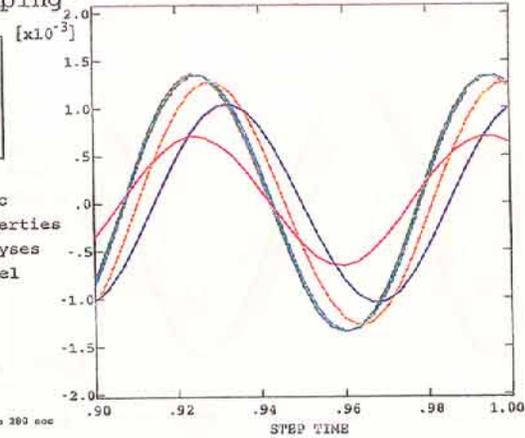
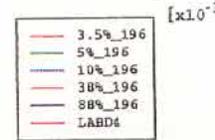
Comparison of Displacement  
 ABAQUS STANDARD  
 Modal Dynamic Analysis

Input Record SHAKEA  
 Elastic Modulus = 210 ksi  
 Density = 140.0 pcf  
 Mesh # 3



# ABAQUS

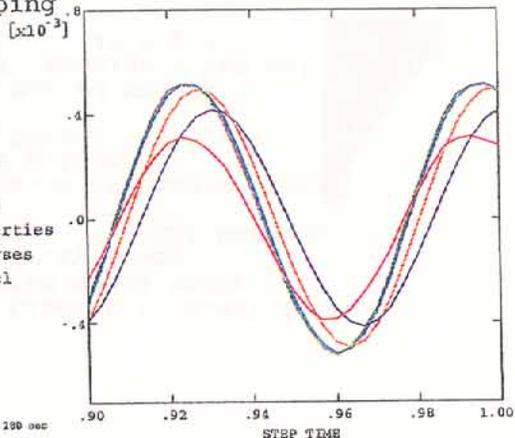
Modal Damping



Total Time = 279.90 to 280 sec  
 ABAQUS Modal Dynamic Analyses & Laboratory Measurements

# ABAQUS

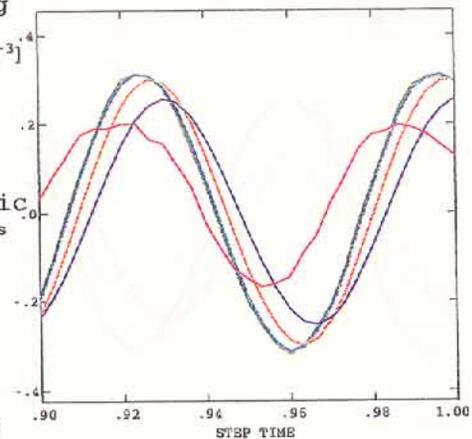
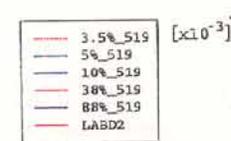
Modal Damping



Total Time = 279.90 to 280 sec  
 ABAQUS Modal Dynamic Analyses & Laboratory Measurements

# ABAQUS

Modal Damping



Total Time = 279.90 to 280 sec  
 ABAQUS Modal Dynamic Analyses & Laboratory Measurements

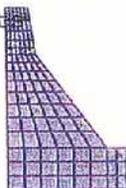
Figure h16

# ABAQUS

Koyna Laboratory Model Study  
 Uncracked Model Study  
 Sensitivity Study  
 Variation of Modal Damping

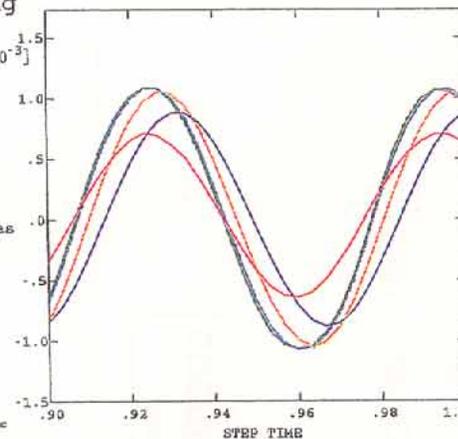
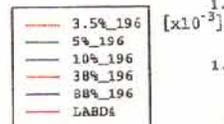
Comparison of Displacement  
 ABAQUS STANDARD  
 Modal Dynamic Analysis

Input Record SHAKEA  
 Elastic Modulus = 250 ksi  
 Density = 140.0 pcf  
 Mesh # 3



# ABAQUS

Modal Damping



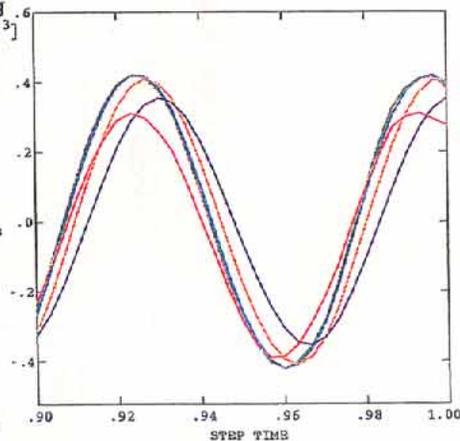
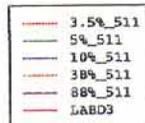
Total Time = 279.90 to 280 sec

ABAQUS Modal Dynamic Analyses & Laboratory Measurements

Linear Elastic  
 Material Properties  
 STANDARD Analyses  
 Uncracked Model  
 Displacement  
 at LVDT#4

# ABAQUS

Modal Damping  
 [x10<sup>-3</sup>]



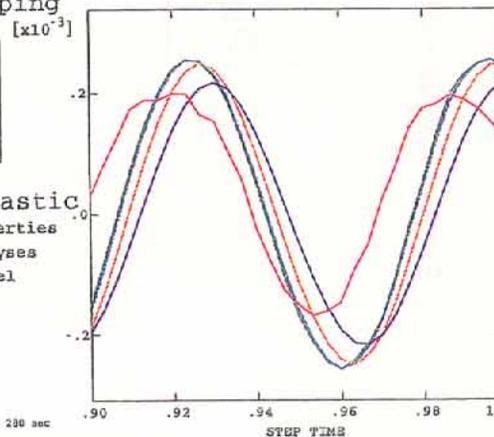
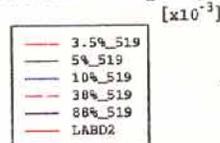
Total Time = 279.90 to 280 sec

ABAQUS Modal Dynamic Analyses & Laboratory Measurements

Linear Elastic  
 Material Properties  
 STANDARD Analyses  
 Uncracked Model  
 Displacement  
 at LVDT#3

# ABAQUS

Modal Damping



Total Time = 279.90 to 280 sec

ABAQUS Modal Dynamic Analyses & Laboratory Measurements

Linear Elastic  
 Material Properties  
 STANDARD Analyses  
 Uncracked Model  
 Acceleration  
 at LVDT#2

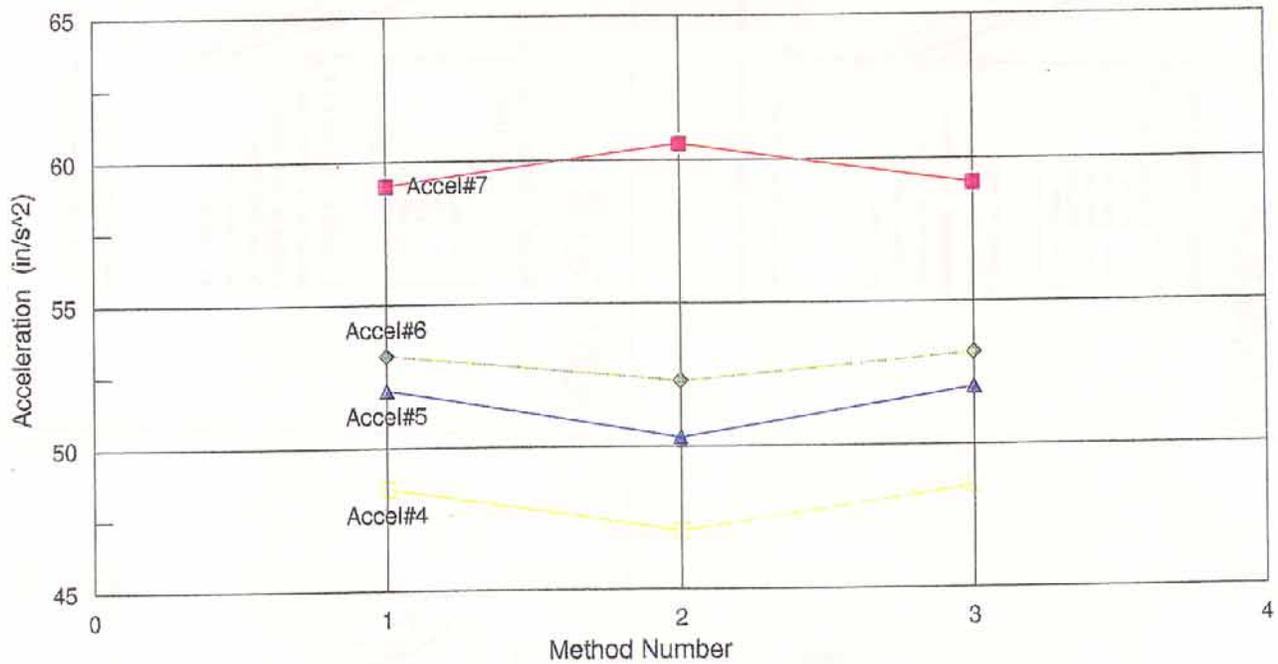
Figure h17

Uncracked Koyna Laboratory Study  
Sensitivity to Variation in Damping Method  
Mesh#3

Modal Damping; Rayleigh Damping; Composite Damping  
10 Percent of Critical Damping

Elastic Modulus = 210 ksi; Material Density = 138.2 pcf

**Peak Accelerations**  
Damping Method Varied



Peak Accelerations ( inch / sec ^ 2 )

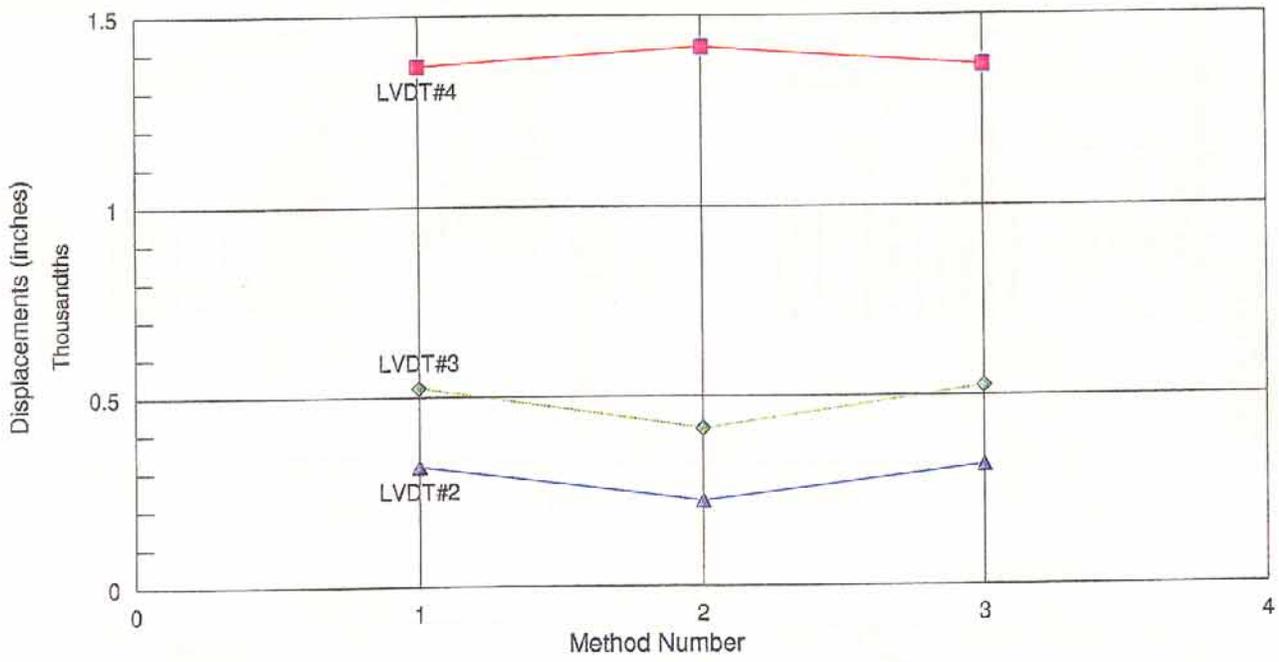
	Modal	Rayleigh	Composite	
Method Number	1	2	3	LAB
Accel#7	59.15	60.57	59.15	53.26
Accel#6	53.21	52.29	53.21	51.72
Accel#5	52.02	50.31	52.02	49.26
Accel#4	48.57	47.06	48.57	47.72
CPU TIME (SEC)	264	264	263	

Figure h18

Uncracked Koyna Laboratory Study  
Sensitivity to Variation in Damping Method  
Mesh#3  
Modal Damping; Rayleigh Damping; Composite Damping  
10 Percent of Critical Damping

Elastic Modulus = 210 ksi; Material Density = 138.2 pcf

**Peak Displacements**  
Damping Method Varied



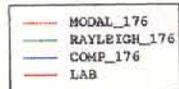
Peak Displacements ( inches )

	Modal	Rayleigh	Composite	
Method Number	1	2	3	LAB
LVDT#4	1.4E-03	1.4E-03	1.4E-03	7.8E-04
LVDT#3	5.2E-04	4.1E-04	5.2E-04	3.0E-04
LVDT#2	3.2E-04	2.2E-04	3.2E-04	1.8E-04
CPU TIME (SEC)	264	264	263	

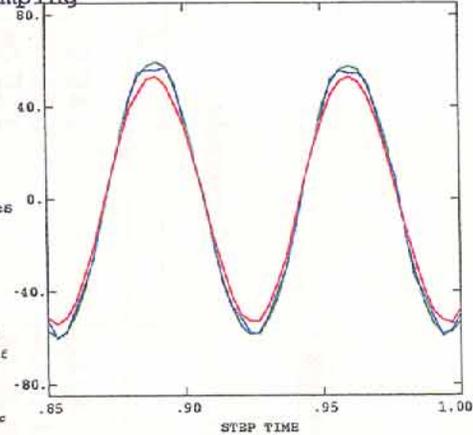
Figure h19

# ABAQUS

Method of Damping  
Varied

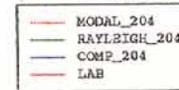


Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model  
Acceleration  
at ACCEL#7  
Elastic Modulus = 210 ksi  
Material Density = 140 pcf  
Filename:SHAKEA  
10% Critical Damping  
Total Time : 279.75 to 280 sec

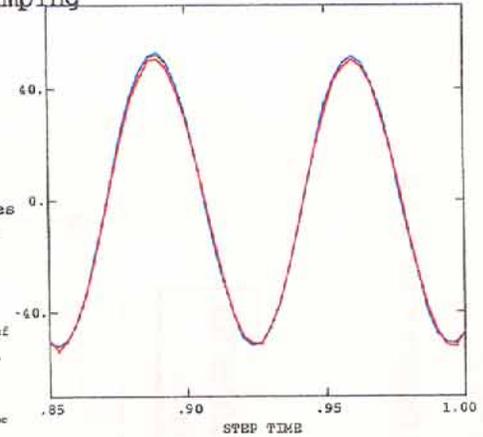


# ABAQUS

Method of Damping  
Varied

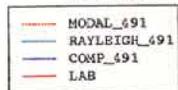


Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model  
Acceleration  
at ACCEL#6  
Material Density = 140 pcf  
Elastic Modulus = 210 ksi  
Filename:SHAKEA  
10% Critical Damping  
Total Time : 279.75 to 280 sec

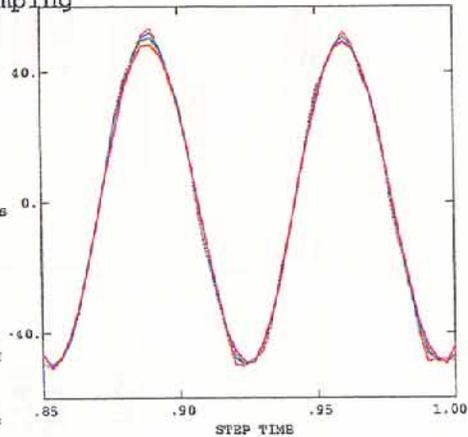


# ABAQUS

Method of Damping  
Varied

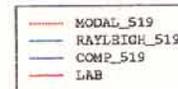


Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model  
Acceleration  
at ACCEL#5  
Elastic Modulus = 210 ksi  
Material Density = 140 pcf  
Filename:SHAKEA  
10% Critical Damping  
Total Time : 279.75 to 280 sec

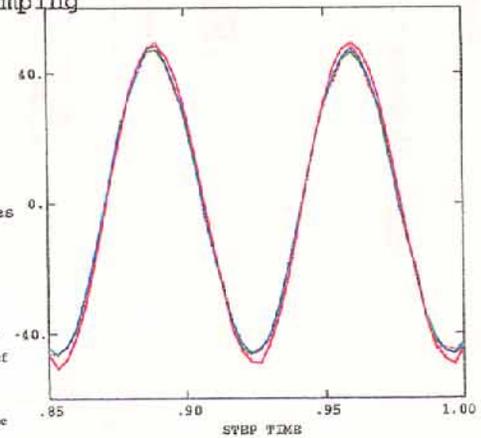


# ABAQUS

Method of Damping  
Varied



Linear Elastic  
Material Properties  
STANDARD Analyses  
Uncracked Model  
Acceleration  
at ACCEL#4  
Elastic Modulus = 210 ksi  
Material Density = 140 pcf  
Filename:SHAKEA  
10% Critical Damping  
Total Time : 279.75 to 280 sec

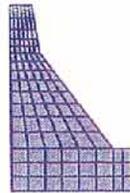


# ABAQUS

Koyna Laboratory Model Study  
 Uncracked Model Study  
 Sensitivity Study  
 Variation of Damping Method

Comparison of Displacements  
 ABAQUS STANDARD  
 Modal Dynamic Analysis

Input Record SHAKKA  
 Elastic Modulus = 210 ksi  
 Density = 140.0 pcf  
 Mesh # 3  
 10 Percent Critical Damping

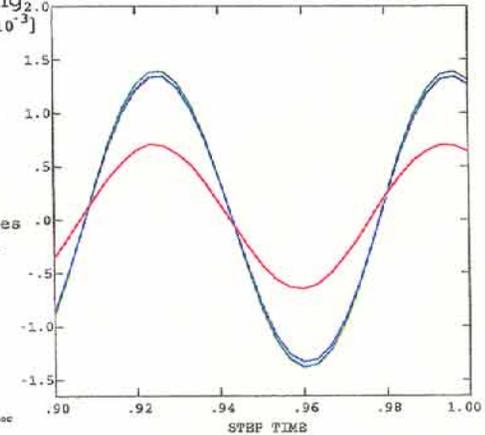


# ABAQUS

Modal Damping<sub>2</sub>  
 [ $\times 10^{-3}$ ]

— MODAL\_196  
 — RAYLEIGH\_196  
 — COMP\_196  
 — LABD4

Linear Elastic  
 Material Properties  
 STANDARD Analyses  
 Uncracked Model  
 Displacement  
 at LVDT#4

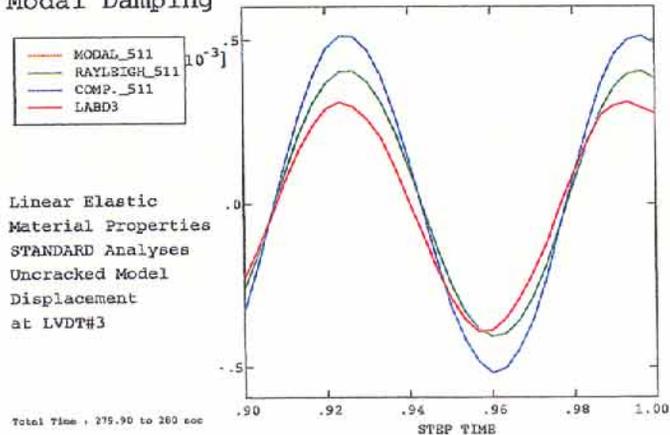


# ABAQUS

Modal Damping

— MODAL\_511  
 — RAYLEIGH\_511  
 — COMP\_511  
 — LABD3

Linear Elastic  
 Material Properties  
 STANDARD Analyses  
 Uncracked Model  
 Displacement  
 at LVDT#3



# ABAQUS

Modal Damping  
 [ $\times 10^{-3}$ ]

— MODAL\_519  
 — RAYLEIGH\_519  
 — COMP\_519  
 — LABD2

Linear Elastic  
 Material Properties  
 STANDARD Analyses  
 Uncracked Model  
 Acceleration  
 at LVDT#2

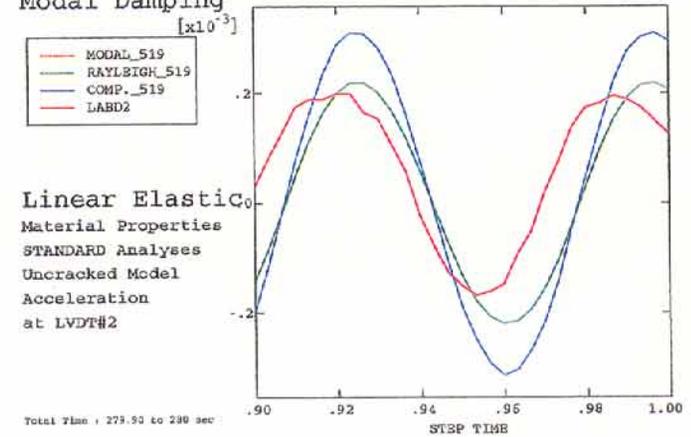


Figure h21

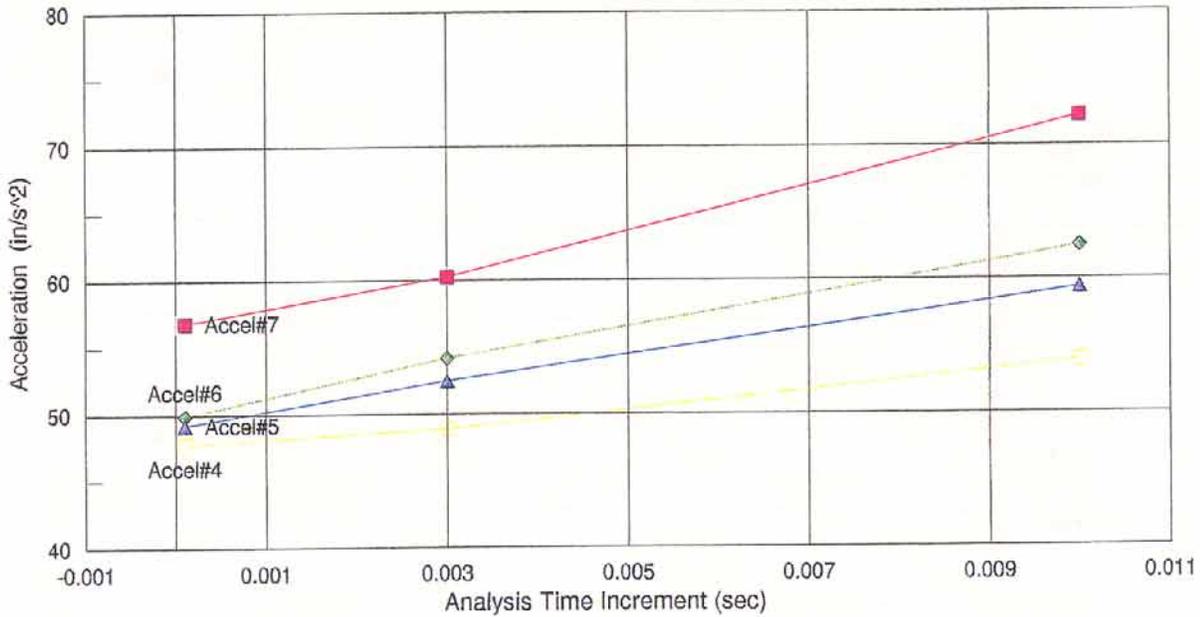
Uncracked Koyna Laboratory Study

Direct Integration Dynamic Analysis  
Sensitivity to Variation in Direct Time Step Parameter  
Mesh#3

Elastic Modulus = 210 ksi;

Material Density = 140 pcf

**Peak Accelerations**  
Direct Time Step Parameter Varied



Peak Accelerations ( inch / sec ^ 2 )

Direct Time Step	0.0001	0.003	0.01	LAB
Accel#7	56.81	60.26	72.18	53.26
Accel#6	49.87	54.17	62.47	51.72
Accel#5	49.19	52.47	59.36	49.26
Accel#4	47.75	48.86	53.94	47.72
CPU Time (sec)	39564	1441	557	

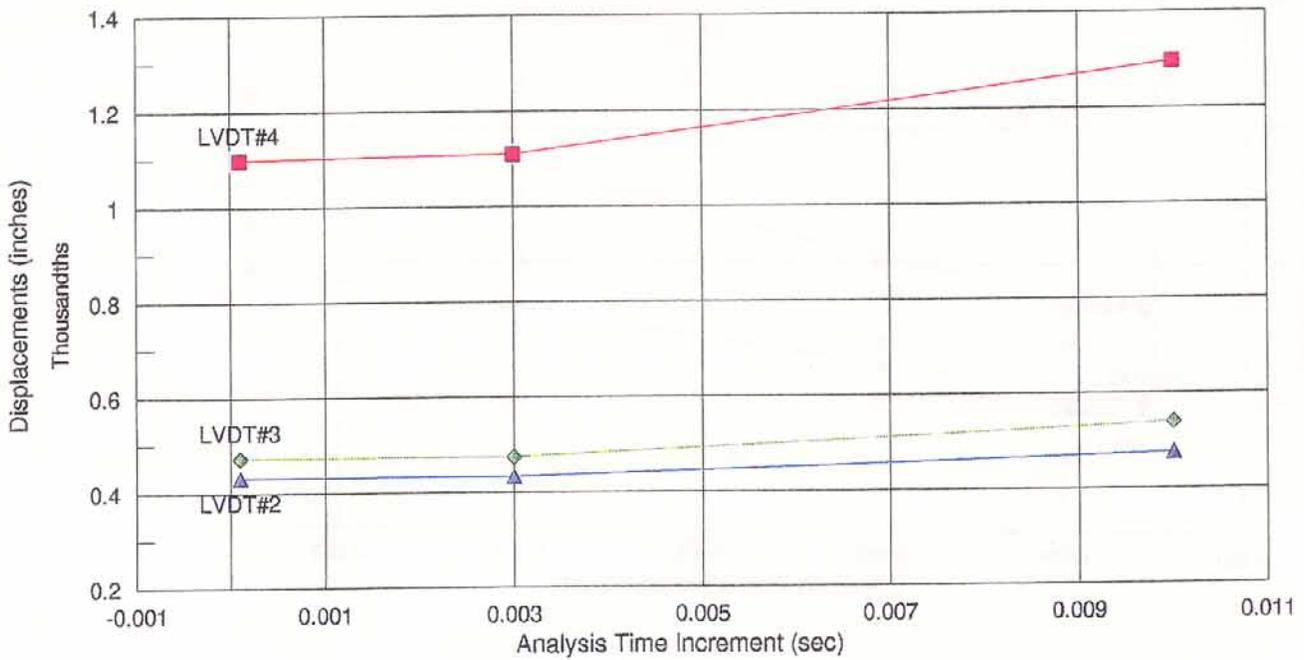
Figure 11

Uncracked Koyna Laboratory Study

Direct Integration Dynamic Analysis  
Sensitivity to Variation in Direct Time Increment Parameter  
Mesh#3

Elastic Modulus = 210 ksi;      Material Density = 140 pcf

**Peak Displacements**  
Direct Time Step Parameter Varied

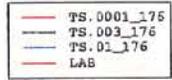


Peak Displacements ( inches )				
Haftol Parameter	0.0001	0.003	0.01	LAB
LVDT#4	1.1E-03	1.1E-03	1.3E-03	7.8E-04
LVDT#3	4.7E-04	4.7E-04	5.4E-04	3.0E-04
LVDT#2	4.3E-04	4.3E-04	4.7E-04	1.8E-04
CPU Time (sec)	39564	1441	557	

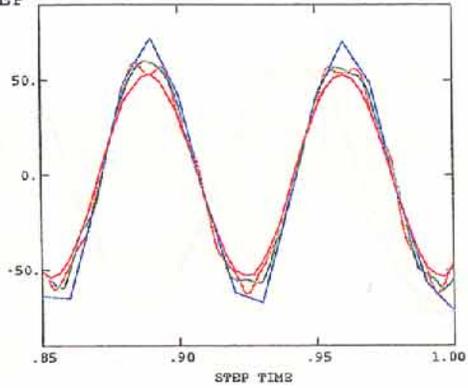
Figure i2

# ABAQUS

DIRECT TIME STEP  
Varied

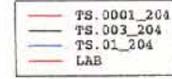


Linear Elastic  
Material Properties  
Uncracked Model  
Acceleration  
at ACCEL#7  
Direct Integration  
Dynamic Analysis  
Material Density = 140 pcf  
Elastic Modulus = 210 ksi  
file:case.01002A

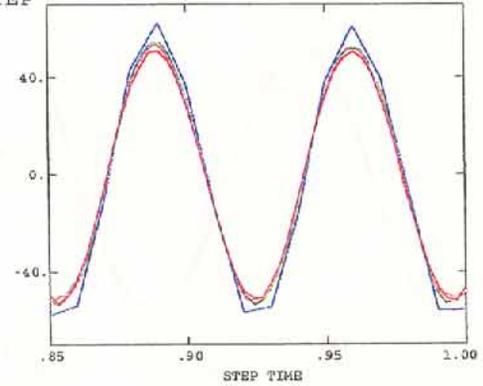


# ABAQUS

DIRECT TIME STEP  
Varied

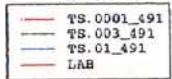


Linear Elastic  
Material Properties  
Uncracked Model  
Acceleration  
at ACCEL#6  
Direct Integration  
Dynamic Analysis  
Material Density = 140 pcf  
Elastic Modulus = 210 ksi  
file:case.01002A

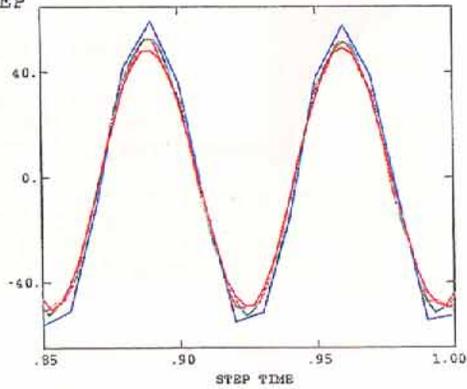


# ABAQUS

DIRECT TIME STEP  
Varied

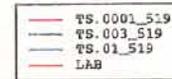


Linear Elastic  
Material Properties  
Uncracked Model  
Acceleration  
at ACCEL#5  
Direct Integration  
Dynamic Analysis  
Material Density = 140 pcf  
Elastic Modulus = 210 ksi  
file:case.01002A

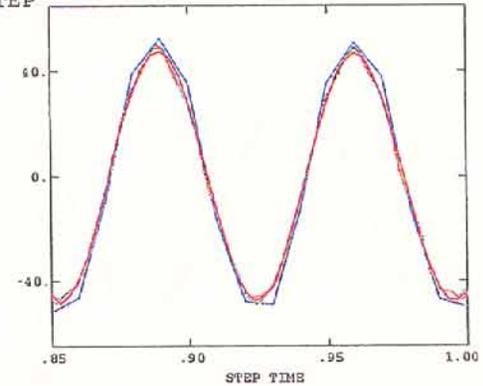


# ABAQUS

DIRECT TIME STEP  
Varied



Linear Elastic  
Material Properties  
Uncracked Model  
Acceleration  
at ACCEL#4  
Direct Integration  
Dynamic Analysis  
Material Density = 140 pcf  
Elastic Modulus = 210 ksi  
file:case.01002A

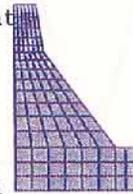


# ABAQUS

Koyna Laboratory Model Study  
 Uncracked Model Study  
 Sensitivity Study  
 Variation of Direct Time Step

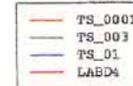
Comparison of Displacement  
 Direct Integration  
 Dynamic Analysis

Input Record SHAKEA  
 Mesh # 3  
 Density = 140 pcf  
 Elastic Modulus = 210 ksi  
 Time Step = .0001, .003, & .01 sec

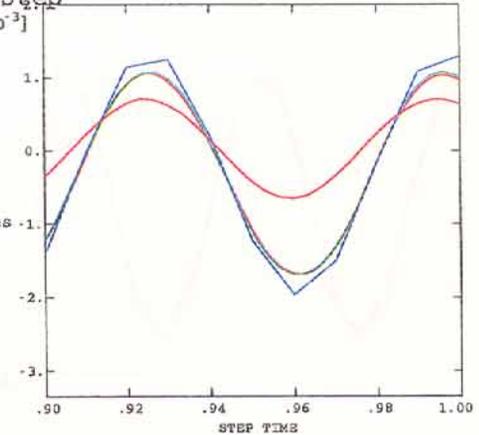


# ABAQUS

Direct Time Step  
 Varied [ $\times 10^{-3}$ ]

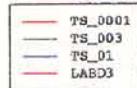


Linear Elastic  
 Material Properties  
 STANDARD Analyses  
 Uncracked Model  
 Displacement  
 at LVDT#4

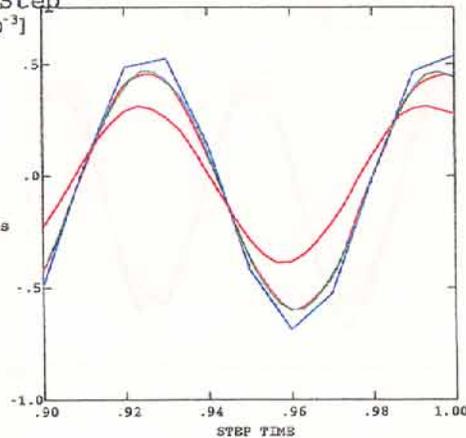


# ABAQUS

Direct Time Step  
 Varied [ $\times 10^{-3}$ ]



Linear Elastic  
 Material Properties  
 STANDARD Analyses  
 Uncracked Model  
 Displacement  
 at LVDT#3



# ABAQUS

Direct Time Step  
 Varied [ $\times 10^{-3}$ ]



Linear Elastic  
 Material Properties  
 STANDARD Analyses  
 Uncracked Model  
 Acceleration  
 at LVDT#2

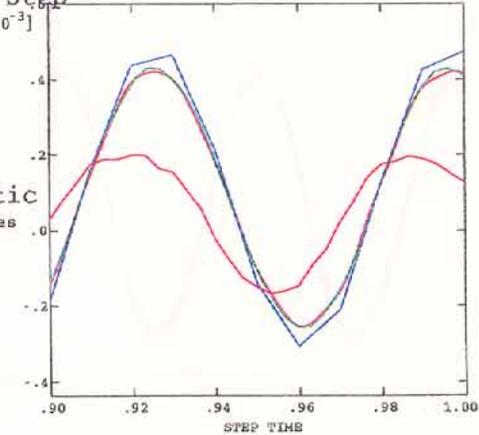


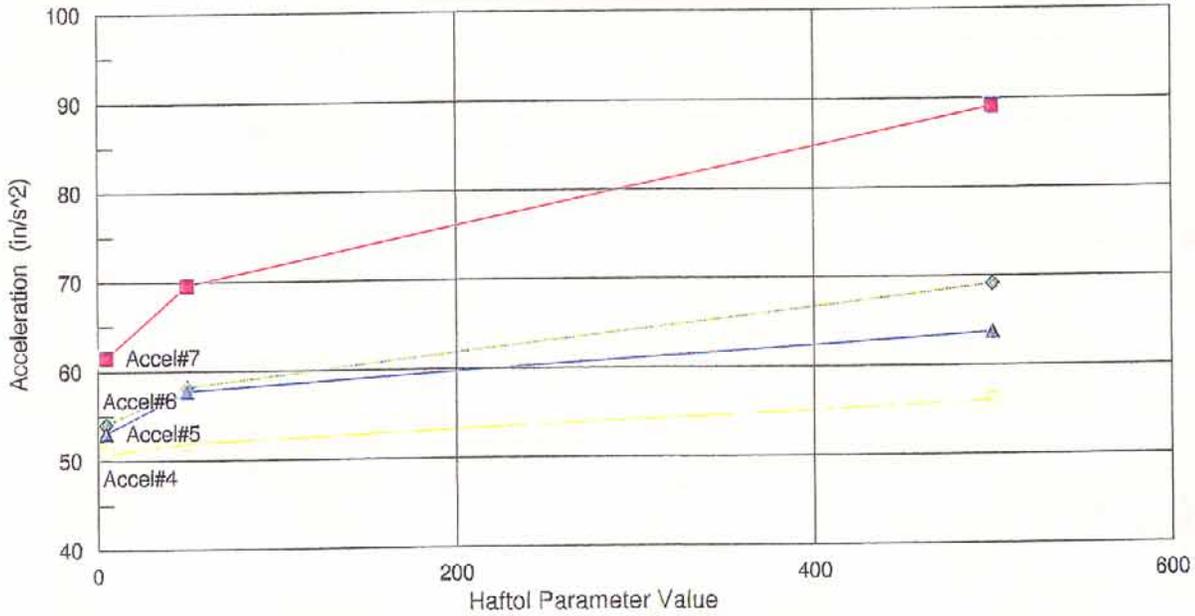
Figure 14

Uncracked Koyna Laboratory Study

Direct Integration Dynamic Analysis  
Sensitivity to Variation in Haftol Parameter  
Mesh#3

Elastic Modulus = 210 ksi;      Material Density = 140 pcf

**Peak Accelerations**  
Haftol Parameter Varied



Peak Accelerations ( Inch / sec ^ 2 )

Haftol Parameter	5	50	500	LAB
Accel#7	61.51	69.62	89.07	53.26
Accel#6	54.09	58.23	69.14	51.72
Accel#5	53.04	57.73	63.71	49.26
Accel#4	50.75	51.88	56.01	47.72
CPU Time (sec)	3179	1230	785	

Uncracked Koyna Laboratory Study

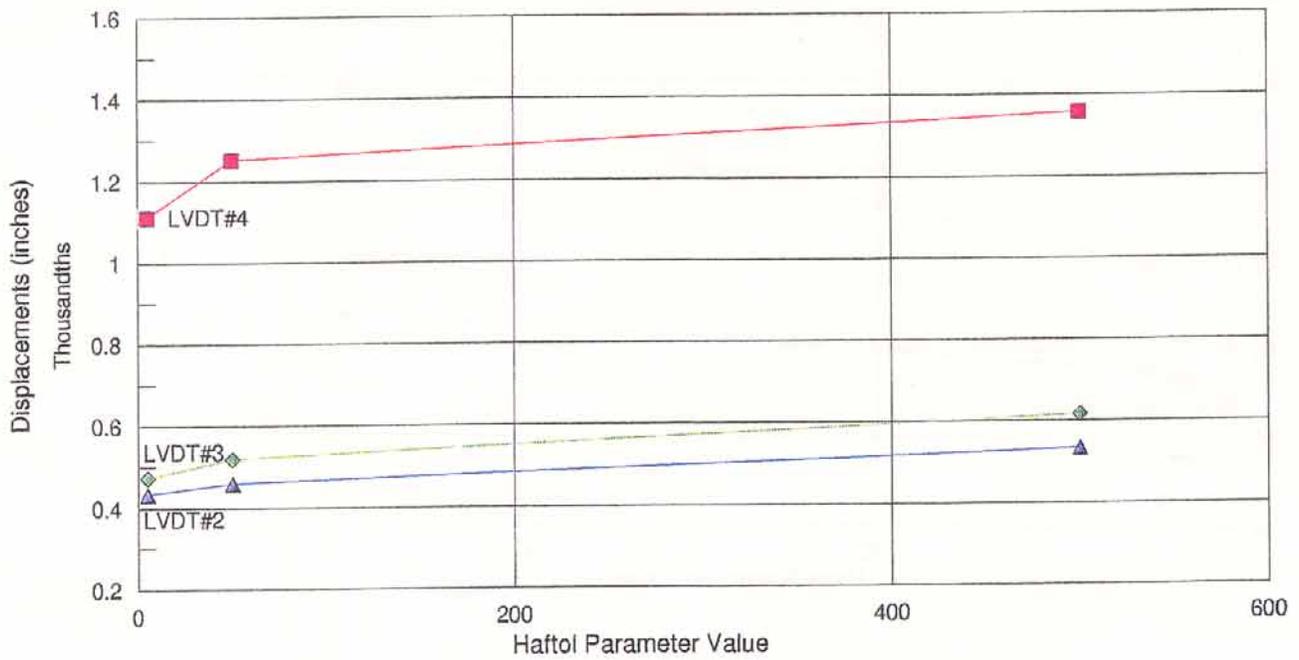
Direct Integration Dynamic Analysis  
Sensitivity to Variation in Haftol Parameter  
Mesh#3

Elastic Modulus = 210 ksi;

Material Density = 140 pcf

Peak Displacements

Haftol Parameter Varied



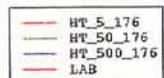
Peak Displacements ( inches )

Haftol Parameter	5	50	500	LAB
LVDT#4	1.1E-03	1.3E-03	1.4E-03	7.8E-04
LVDT#3	4.7E-04	5.2E-04	6.2E-04	3.0E-04
LVDT#2	4.3E-04	4.6E-04	5.3E-04	1.8E-04
CPU Time (sec)	3179	1230	785	

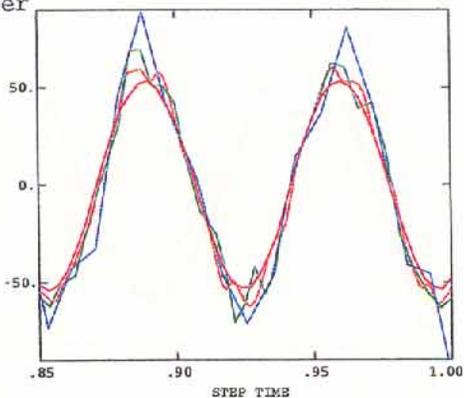
Figure i6

# ABAQUS

Haftol Parameter Varied

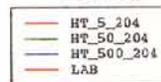


Linear Elastic  
Material Properties  
Uncracked Model  
Acceleration  
at ACCEL#7  
Direct Integration  
Dynamic Analysis  
Material Density = 140 pcf  
Elastic Modulus = 210 ksi  
FILENAME:SHA22A

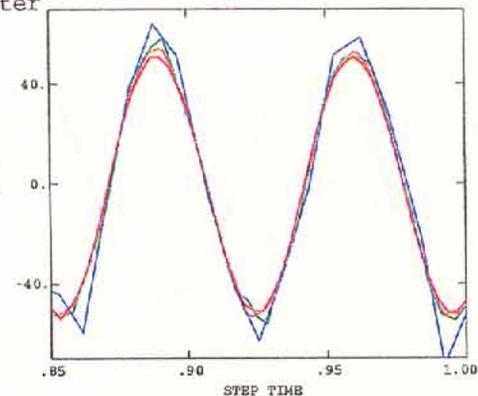


# ABAQUS

Haftol Parameter Varied

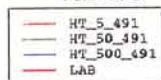


Linear Elastic  
Material Properties  
Uncracked Model  
Acceleration  
at ACCEL#6  
Direct Integration  
Dynamic Analysis  
Material Density = 140 pcf  
Elastic Modulus = 210 ksi  
FILENAME:SHA22A

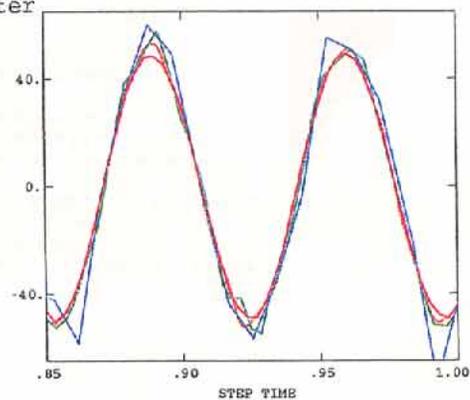


# ABAQUS

Haftol Parameter Varied

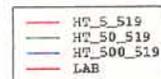


Linear Elastic  
Material Properties  
Uncracked Model  
Acceleration  
at ACCEL#5  
Direct Integration  
Dynamic Analysis  
Material Density = 140 pcf  
Elastic Modulus = 210 ksi  
FILENAME:SHA22A

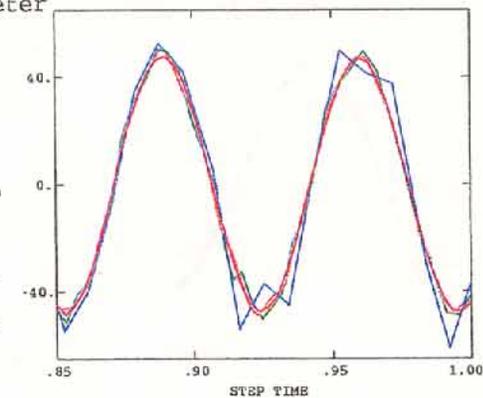


# ABAQUS

Haftol Parameter Varied



Linear Elastic  
Material Properties  
Uncracked Model  
Acceleration  
at ACCEL#4  
Direct Integration  
Dynamic Analysis  
Material Density = 140 pcf  
Elastic Modulus = 210 ksi  
FILENAME:SHA22A

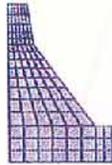


# ABAQUS

Koyna Laboratory Model Study  
 Uncracked Model Study  
 Sensitivity Study  
 Variation of Haftol Parameter

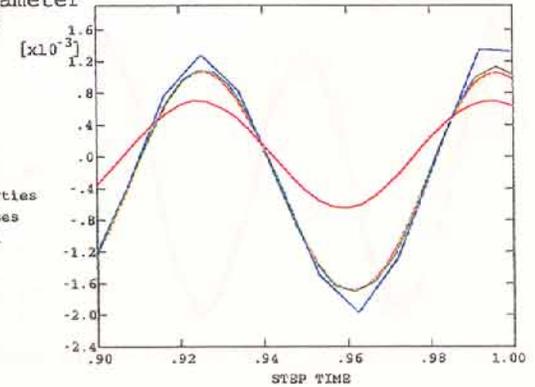
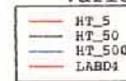
Comparison of Displacements  
 Direct Integration  
 Dynamic Analysis

Input Record SHAKEA  
 Haftol = 5, 50, & 500  
 Density = 140 pcf  
 Elastic Modulus = 210 ksi  
 Mesh # 3



# ABAQUS

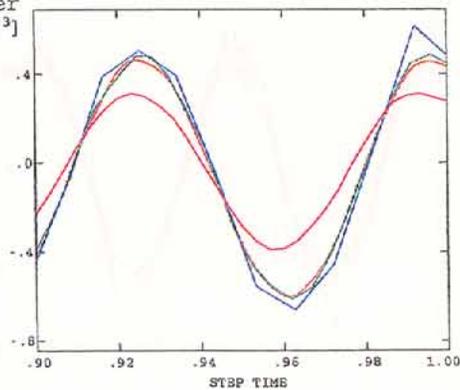
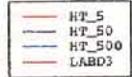
Haftol Parameter  
 Varied



Linear Elastic  
 Material Properties  
 STANDARD Analyses  
 Uncracked Model  
 Displacement  
 at LVD7#4

# ABAQUS

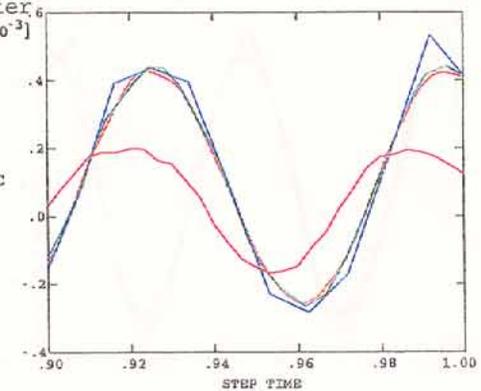
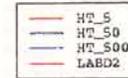
Haftol Parameter  
 Varied [ $\times 10^{-3}$ ]



Linear Elastic  
 Material Properties  
 STANDARD Analyses  
 Uncracked Model  
 Displacement  
 at LVD7#3

# ABAQUS

Haftol Parameter  
 Varied [ $\times 10^{-3}$ ]

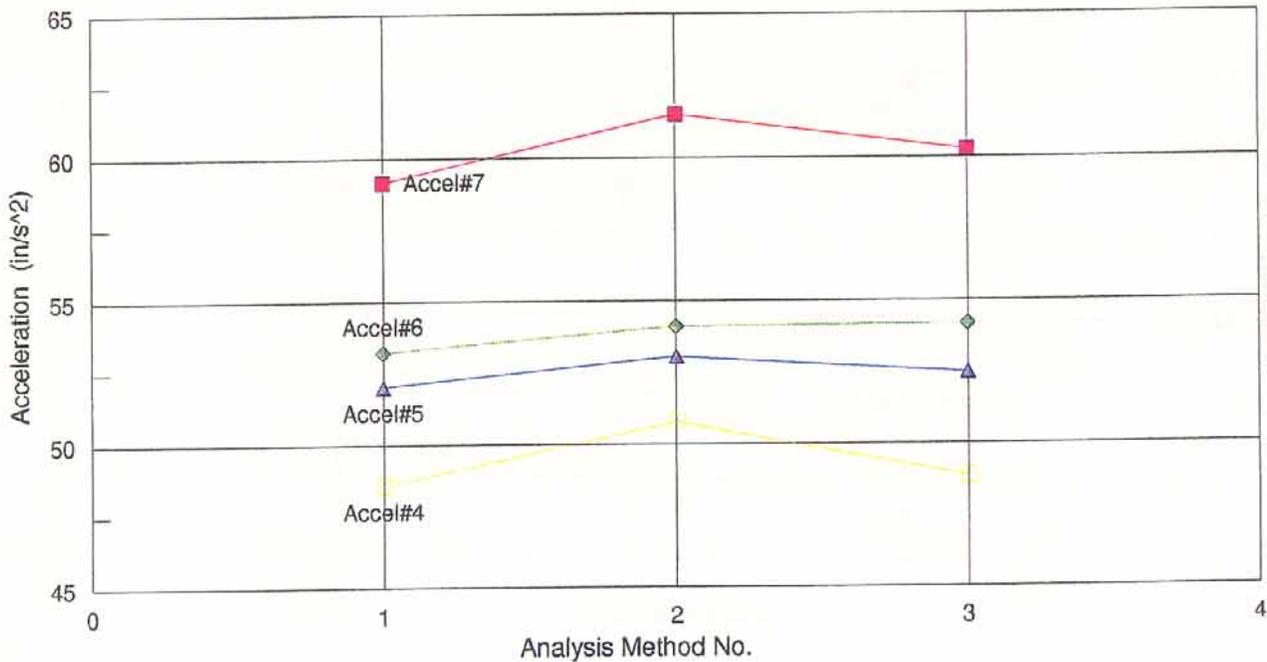


Linear Elastic  
 Material Properties  
 STANDARD Analyses  
 Uncracked Model  
 Acceleration  
 at LVD7#2

Figure 18

Uncracked Koyna Laboratory Study  
 Sensitivity to Variation Analysis Method  
 Mesh#3  
 Modal Analysis Methods  
 Direct Integration using Haftol Parameter = 5  
 Direct Integration using Direct time Step = .003 sec  
 Modal Analysis  
 10 Percent of Critical Damping  
 Elastic Modulus = 210 ksi; Material Density = 139 pcf

**Peak Accelerations**  
 Analysis Method Varied



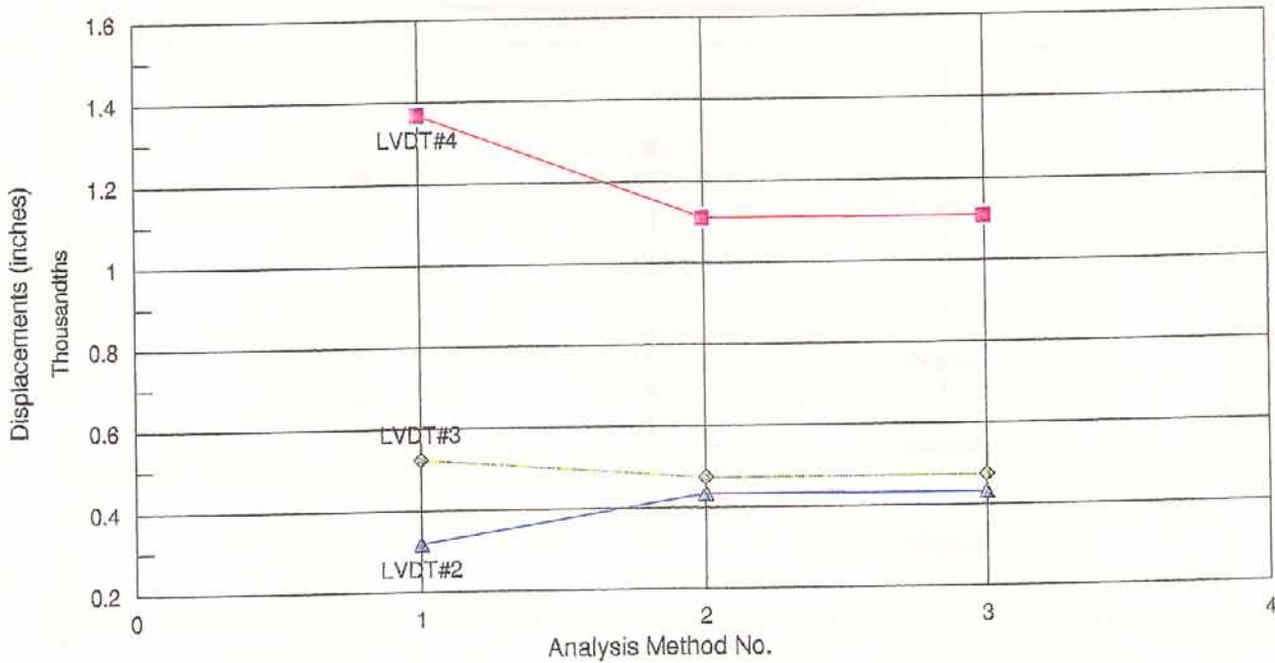
Peak Accelerations ( inch / sec ^ 2 )

	Modal	Direct Haftol=5	Direct Time Step=.003	
Method Number	1	2	3	LAB
Accel#7	59.15	61.51	60.26	53.26
Accel#6	53.21	54.09	54.17	51.72
Accel#5	52.02	53.04	52.47	49.26
Accel#4	48.57	50.75	48.86	47.72
CPU TIME (SEC)	264	3179	1441	

Figure j1

Uncracked Koyna Laboratory Study  
 Sensitivity to Variation Analysis Method  
 Mesh#3  
 Modal Analysis Methods  
 Direct Integration using Haftol Parameter = 5  
 Direct Integration using Direct time Step = .003 sec  
 Modal Analysis  
 10 Percent of Critical Damping  
 Elastic Modulus = 210 ksi; Material Density = 139 pcf

**Peak Displacements**  
 Analysis Method Varied



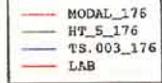
Peak Displacements ( inches )

	Modal	Direct Haftol=5	Direct Time Step=.003	LAB
Method Number	1	2	3	
LVDT#4	1.4E-03	1.1E-03	1.1E-03	7.8E-04
LVDT#3	5.2E-04	4.7E-04	4.7E-04	3.0E-04
LVDT#2	3.2E-04	4.3E-04	4.3E-04	1.8E-04
CPU TIME (SEC)	264	3179	1441	

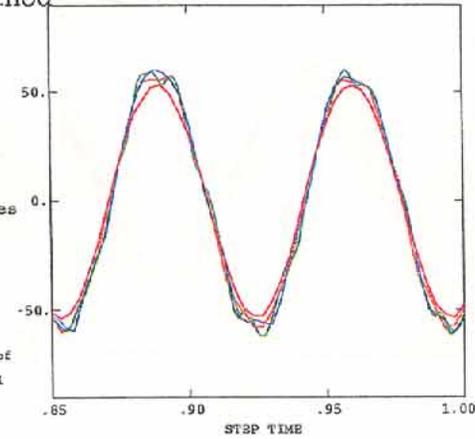
Figure j2

# ABAQUS

Analysis Method Varied

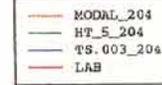


Linear Elastic  
Material Properties  
Uncracked Model  
Acceleration  
at ACCEL#7  
Modal & Direct  
Dynamic Analyses  
Material Density = 140 pcf  
Elastic Modulus = 210 ksi  
Filename: SHAKZA

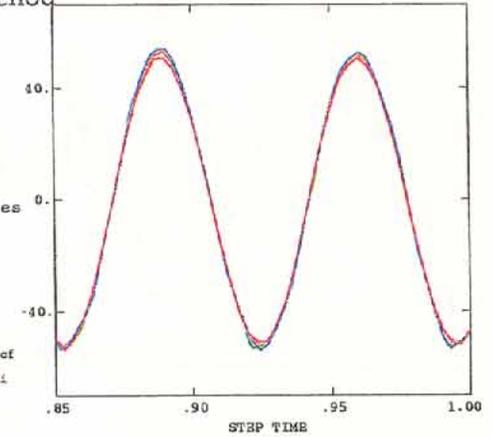


# ABAQUS

Analysis Method Varied

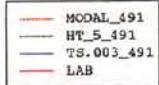


Linear Elastic  
Material Properties  
Uncracked Model  
Acceleration  
at ACCEL#6  
Modal & Direct  
Dynamic Analysis  
Material Density = 140 pcf  
Elastic Modulus = 210 ksi  
Filename: SHAKZA

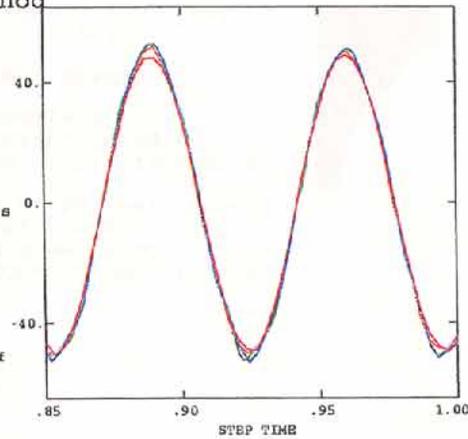


# ABAQUS

Analysis Method Varied

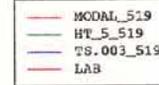


Linear Elastic  
Material Properties  
Uncracked Model  
Acceleration  
at ACCEL#5  
Modal & Direct  
Dynamic Analysis  
Material Density = 140 pcf  
Elastic Modulus = 210 ksi  
Filename: SHAKZA

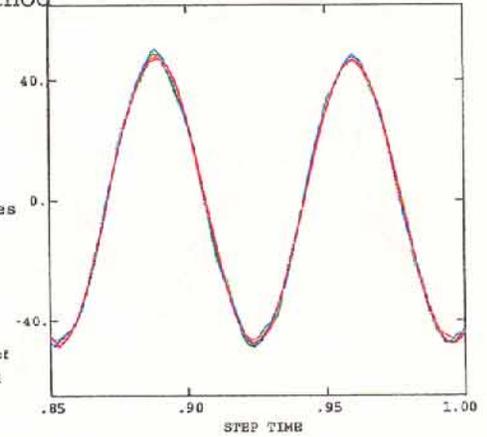


# ABAQUS

Analysis Method Varied



Linear Elastic  
Material Properties  
Uncracked Model  
Acceleration  
at ACCEL#4  
Modal & Direct  
Dynamic Analysis  
Material Density = 140 pcf  
Elastic Modulus = 210 ksi  
Filename: SHAKZA

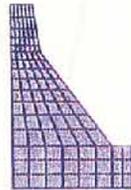


# ABAQUS

Koyna Laboratory Model Study  
 Uncracked Model Study  
 Sensitivity Study  
 Variation of Analysis Method

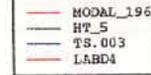
Comparison of Displacements  
 Modal & Direct Integration  
 Dynamic Analysis

Input Record SHAKEA  
 Mesh # 3  
 Density = 140 pcf  
 Elastic Modulus = 210 ksi

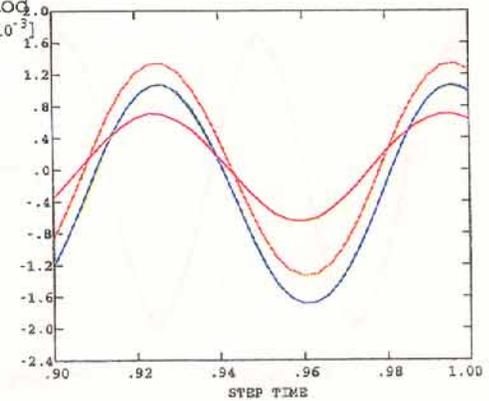


# ABAQUS

Analysis Method  
 Varied [ $\times 10^{-3}$ ]

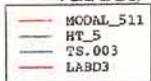


Linear Elastic  
 Material Properties  
 STANDARD Analyses  
 Uncracked Model  
 Displacement  
 at LVDT#4

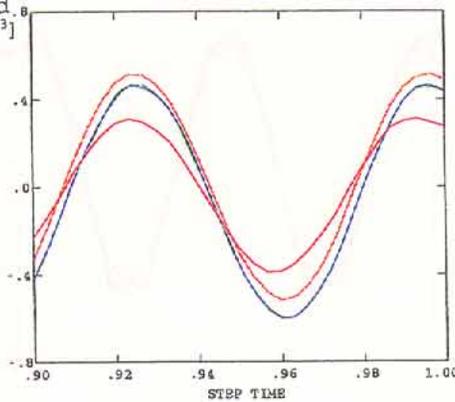


# ABAQUS

Analysis Method  
 Varied [ $\times 10^{-3}$ ]



Linear Elastic  
 Material Properties  
 STANDARD Analyses  
 Uncracked Model  
 Displacement  
 at LVDT#3



# ABAQUS

Analysis Method  
 Varied [ $\times 10^{-3}$ ]



Linear Elastic  
 Material Properties  
 STANDARD Analyses  
 Uncracked Model  
 Acceleration  
 at LVDT#2

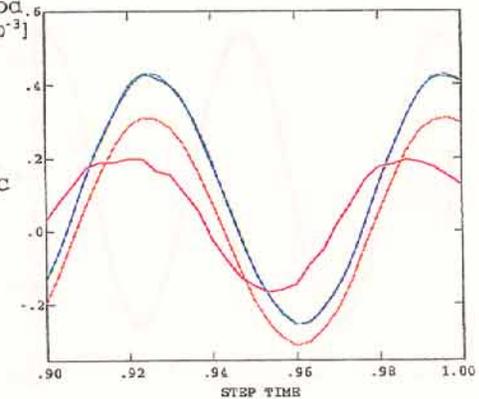


Figure j4

# ABAQUS

Koyna Laboratory Model Study  
Uncracked Model Study

Determination of Mesh Sensitivity  
Non-linear Material Propertys  
Failure Stress = 55 psi  
Mode I Fracture Energy = 0.2012  
Crack Opening Strain = .001375

Explicit Analysis  
with Mesh #3

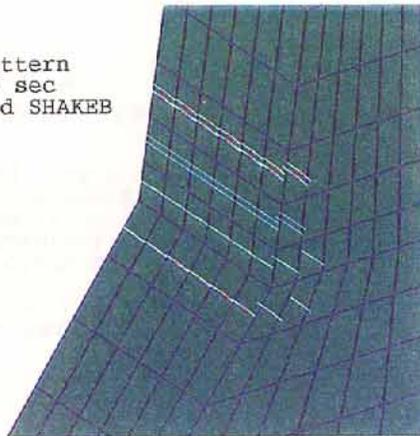
# ABAQUS

Cracking Initiated  
at 401.3 sec  
Input Record SHAKEB



# ABAQUS

Cracking Pattern  
at 401.5 sec  
Input Record SHAKEB



# ABAQUS

Cracking Pattern  
at 401.6 sec  
Input Record SHAKEB



Figure K1

# ABAQUS

Koyna Laboratory Model Study  
Uncracked Model Study

Determination of Mesh Sensitivity  
Non-linear Material Propertys  
Failure Stress = 55 psi  
Mode I Fracture Energy = 0.2012  
Crack Opening Strain = .001375

Explicit Analysis  
with Mesh #5

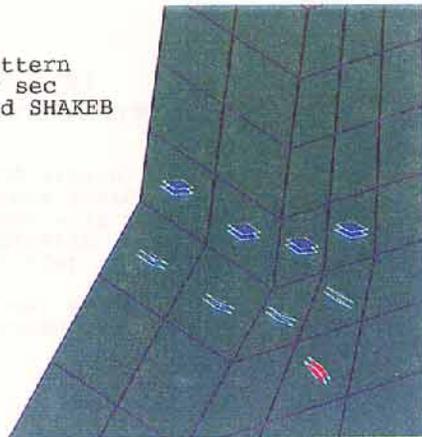
# ABAQUS

Cracking Initiated  
at 407.6 sec  
Input Record SHAKEB



# ABAQUS

Cracking Pattern  
at 407.7 sec  
Input Record SHAKEB



# ABAQUS

Cracking Pattern  
at 407.75 sec  
Input Record SHAKEB



Figure k2

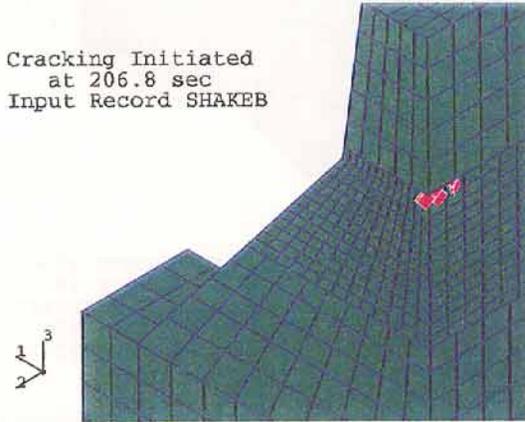
# ABAQUS

Koyna Laboratory Model Study  
Uncracked Model Study  
Determination of Mesh Sensitivity  
Non-linear Material Propertys  
Failure Stress = 55 psi  
Mode I Fracture Energy = 0.2012  
Crack Opening Strain = .001375

Explicit Analysis  
with Mesh #1

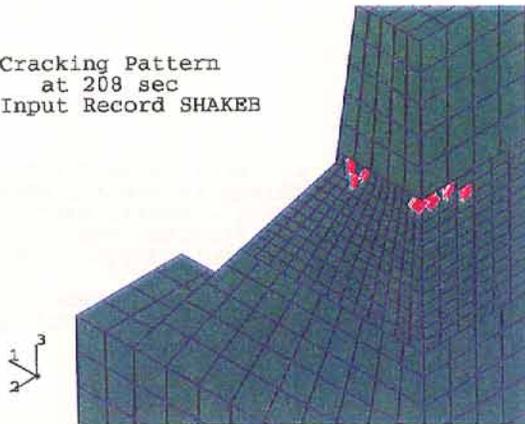
# ABAQUS

Cracking Initiated  
at 206.8 sec  
Input Record SHAKEB



# ABAQUS

Cracking Pattern  
at 208 sec  
Input Record SHAKEB



# ABAQUS

Cracking Pattern  
at 210.5 sec  
Input Record SHAKEB

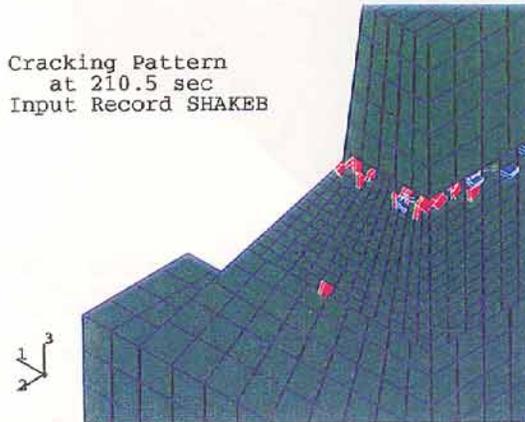


Figure k3

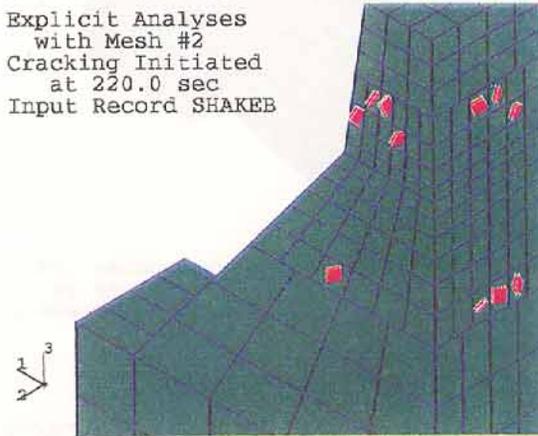
# ABAQUS

Koyna Laboratory Model Study  
Uncracked Model Study

Determination of Mesh Sensitivity  
Non-linear Material Propertys  
Failure Stress = 55 psi  
Mode I Fracture Energy = 0.2012  
Crack Opening Strain = .001375

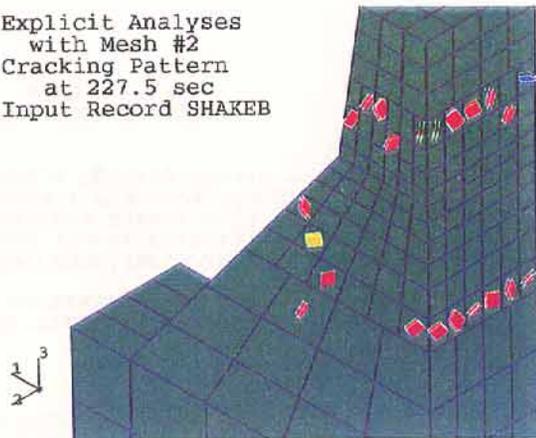
# ABAQUS

Explicit Analyses  
with Mesh #2  
Cracking Initiated  
at 220.0 sec  
Input Record SHAKEB



# ABAQUS

Explicit Analyses  
with Mesh #2  
Cracking Pattern  
at 227.5 sec  
Input Record SHAKEB



# ABAQUS

Explicit Analyses  
with Mesh #2  
Cracking Failure  
at 232.5 sec  
Input Record SHAKEB

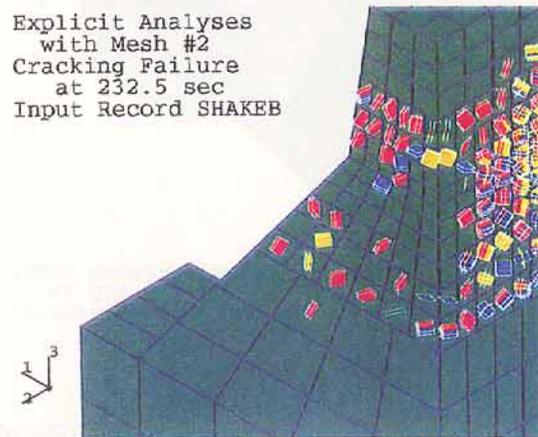


Figure k4